A Metallic Pipe with Small Corrugations Used as a Dechirper

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Outline

- Motivation
- Analytical wake formulas
- Numerical comparisons
- Commissioning measurements at the LCLS

Note: the theoretical work presented here was originally performed together with G. Stupakov, I. Zagorodnov, and/or E. Gjonaj

• References:

K. Bane and G. Stupakov, "Corrugated Pipe as a Beam Dechirper," Nucl Inst Meth A 690 (2012) 106

K. Bane, G. Stupakov, "Dechirper Wakefields for Short Bunches," Nucl Inst Meth A 820 (2016) 156

K. Bane, G. Stupakov, I. Zagorodnov, "Analytical formulas for short bunch wakes in a flat dechirper," Phys Rev Accel Beams 19 (2016) no. 8, 084401

K. Bane, G. Stupakov, I. Zagorodnov, "Wakefields of a Beam near a Single Plate in a Flat Dechirper," SLAC-PUB-16881, Nov 2016

Why a Dechirper?

• After the last bunch compressor in a linac-based, X-ray FEL, the beam is typically left with an energy–longitudinal position correlation (an energy "chirp"), with the bunch tail at higher energy than the head

• A typical value might be h = 40 MeV/mm. To cancel this chirp, one can run off-crest in downstream RF cavities. Running the beam on the zero crossing of the wave, we would need length $L = h/(G_{rf}k_{rf})$ of extra RF. Or with peak RF gradient $G_{rf} = 20 \text{ MeV/m}$, $k_{rf} = 27/\text{m}$ (for f = 1.3 GHz), we would need L = 74 m of extra active RF

• Can we use the wakefields induced in a few meters of structure to passively accomplish the same result?

• We would like a low frequency wake (compared to the bunch; capacitive) with strong amplitude

• A passive RF cavity does not work well, since many high frequency modes are also excited by a short bunch

Corrugated Pipe in Round Geometry

A short bunch generates a strong synchronous mode in a pipe with rough surfaces (A. Novokhatski & A. Mosnier, 1997; K. Bane & A. Novokhatski, 1999)



Consider a short bunch exciting mode in corrugated pipe, with $p \leq h \ll a$; for simplicity let p = 2g:

• Wave number
$$k \equiv \left(\frac{2\pi f}{c}\right) = \frac{2}{\sqrt{ah}}$$

• Wave number far above cut off,

low compared to inverse size of corrugation

• Amplitude of mode,

$$W(0^+) \approx rac{Z_0 c}{\pi a^2}$$
 (where $Z_0 = 377 \ \Omega$)

• Dielectric-lined, metallic pipe has an equivalent effect

Corrugated Pipe as Dechirper

• In theory, for any cavity-like structure, point charge wake can be written $w(s) = 2 \sum_{n} \varkappa_{n} \cos k_{n} s$ (s > 0)

Also, in a periodic structure $w(0^+) \equiv w_0 = 2 \sum_n \varkappa_n$ only depends on the shape of the beam pipe; in a round structure, $w_0 = Z_0 c / (\pi a^2) \Rightarrow \max$. wake in structure with aperture a

• Attractiveness of using structure with small corrugations as a dechirper is that the wake is almost all in the first, relatively low frequency mode: $w(s) \approx w_0 \cos k_1 s \ (s > 0)$

• Bunch wake by convolution: $W_\lambda(s) = -\int_0^\infty w(s')\lambda(s-s')\,ds'$

• Normally want to compensate tail of beam at higher energy than head, or want dechirper that is capacitive $\Rightarrow k\sigma_z$ small

If
$$k\sigma_z \ll 1 \Rightarrow W_\lambda(s) \approx -2\varkappa \int_{-\infty}^s \lambda(x) \, dx$$

• If bunch distribution is uniform of length $\ell~(=2\sqrt{3}\sigma_z),$ then over bunch

$$W_{\lambda}(s) = -2\varkappa\sin[k(s+\ell/2)]/k\ell \approx -2\varkappa s/\ell$$

Numerical Example-NGLS

• We performed a time-domain wake calculation using I. Zagorodnov's ECHO program; found good agreement with analytical model



Dechirper for NGLS: wake of model of NGLS bunch distribution (blue). The dashed, red line gives the linear chirp approximation. The bunch shape λ , with the head to the left, is given in black

• If beam moves off-axis, dipole wake induced, $w_y(s) \sim 1/a^4 \Rightarrow$ limits how small an aperture can be chosen. For uniform bunch distribution, bunch dipole wake $W_{\lambda y}(s) \sim s^2$

• For flexibility, choose flat geometry. (Longitudinal wake will be $\pi^2/16 \approx 0.6$ weaker for same full aperture.) With driving and test particles at (x_0, y_0) and (x, y) near axis, you excite dipole and quad wakes (quad wakes even with beam centered on axis):

$$w_y = y_0 w_{yd}(s) + y w_{yq}(s)$$
, $w_x = (x_0 - x) w_{yq}(s)$;

 $w_q(s)$ will result in focusing/defocusing varying from head to tail of bunch \Rightarrow projected emittance growth

To mitigate this, build dechirper in two parts, one oriented horizontally, the other vertically

• Neither LCLS at SLAC, nor the upgrade LCLS-II, need a dechirper for chirp control. However, the ability to give a strong differential transverse kick to the beam, by passing it near one jaw, has drawn much interest and is, in fact, in use for generating *e.g.* two colors of x-rays for pump-probe experiments.



Sketch of two color generation using the dechirper (C. Emma)

• The transverse kick ~ s^2 . An example calculation yields a 3 MV differential over a 30 μ m length. For an X-band (11.4 GHz) transverse cavity, that is equivalent to 420 MV peak voltage

Table: RadiaBeam/LCLS Dechirper parameters. The dechirper comprises a vertical and a horizontal unit, each of which consists of two flat, corrugated plates.

Parameter name	Value	Units
Period, <i>p</i>	0.50	mm
Longitudinal gap, <i>t</i>	0.25	mm
Depth, <i>h</i>	0.50	mm
Nominal half aperture, a	0.70	mm
Plate width, <i>w</i>	12.7	mm
Plate length, <i>L</i>	2	m

Analytical Calculation of Wakes of Dechirper

• Analytical formulas for the wakes are desirable for *e.g.* parameter studies, simulations of novel lasing schemes using dechirper, etc.

• There are time domain, finite difference programs that can find the wakes in a flat dechirper, *e.g.* ECHO, NOVO...

• We have used a surface impedance approach in field matching to find the generalized wakes between two (horizontally orientated) dechirper plates

$$Z_{I}(k) = \frac{2\zeta}{c} \int_{-\infty}^{\infty} dq \, q \operatorname{csch}^{3}(2qa) f(q, y, y_{0}) e^{-iq(x-x_{0})} , \qquad (1)$$

with $k = \omega/c$, the surface impedance is $\zeta(k)$, the full gap is 2*a*, the drive beam is at (x_0, y_0) , the test beam at (x, y), *f* is an analytical function; surface impedance approach: at boundary let $\tilde{E}_z(k) = \zeta(k)\tilde{H}_x(k)$, an approach that is valid when h/a small

• We can numerically perform the integral, and inverse Fourier transform, to find the generalized wakes [for usual wakes and impedances, $x \approx x_0$, $y \approx y_0$]

Analytical Calculations Cont'd

• To obtain the result for a beam passing by a *single* plate at distance b, take the two-plate result, let $y \to a - b$, then let $a \to \infty$

• The high frequency impedance of a periodic structure $Z(k) \sim i/k$, and the transverse impedance, $Z_y(k) \sim i/k^2$. Thus the longitudinal wake at the origin, and the slope of the transverse wake at the origin, can be obtained from the high frequency impedances as ("zeroth order approximation"):

$$w_0 = -ic \lim_{k \to \infty} k Z_I(k) , \qquad w'_{y0} = -ic \lim_{k \to \infty} k^2 Z_Y(k)$$

From result of field matching we find *e.g.* for a beam offset at y from the axis between two plates separated by 2a; or for a beam offset by b from a single plate

$$w_0 = \frac{\pi^2}{16} \left(\frac{Z_0 c}{\pi a^2} \right) \sec^2 \left(\frac{\pi y}{2a} \right) ; \quad w'_{y0} = \frac{Z_0 c}{4\pi b^3}$$

Analytical First Order Approximation

• For better accuracy we need to go to the next, "first order approximation"

• For a periodic accelerating structure, the high frequency impedance can be written in the form (Gluckstern; Yokoya, Bane)

$$Z_I(k) \approx i \frac{w_0}{kc} \left[1 - \frac{(1+i)}{\sqrt{2ks_0}} \right] , \qquad (2)$$

and this corresponds to a short-range wake approximation

$$w_l(s) \approx w_0 e^{-\sqrt{s/s_0}}$$
 (s > 0) (3)

• For the dechirper, we take as (high frequency) surface impedance $\zeta(k) = (2it/\pi k)^{1/2} / (\alpha p)$; then we expand our field matching solution of Z(k) [Eq. 1] to second order in 1/k; comparing with Eq. 2, we can pick out w_0 and s_0 ; the wake is given by Eq. 3

Analytical Approximation Cont'd

• Similarly for the short-range transverse wakes, with analytic w'_{0y} , s_{0y} :

$$w_{y}(s) = 2w_{0y}'s_{0y}\left[1 - \left(1 + \sqrt{s/s_{0y}}\right)e^{-\sqrt{s/s_{0y}}}\right]$$

• Have analytical solutions of short-range wakes, for single and double plates, for longitudinal, dipole, and quad components

• At LCLS we measured *e.g.* the average (over the bunch) kick angle, given by $\langle y'_w \rangle = eQL\varkappa_y/E$, with Q the charge of the bunch, L the length of the dechirper plates, E the bunch energy; For a bunch with a uniform distribution of length ℓ , the kick factor is

$$\varkappa_y = \frac{1}{\ell} \int_0^\ell w_y(s) \left(1 - \frac{s}{\ell} \right) \, ds = w_{0y}' s_{0y} f_y \left(\frac{\ell}{s_{0y}} \right) \; ,$$

with

$$f_{y}(x) = 1 - \frac{12}{x} + \frac{120}{x^{2}} - 8e^{-\sqrt{x}} \left(\frac{1}{x^{1/2}} + \frac{6}{x} + \frac{15}{x^{3/2}} + \frac{15}{x^{2}} \right) .$$

Example Numerical Comparison

• Longitudinal bunch wake of Gaussian beam offset by y from axis of a two-plate dechirper of gap 2a



Example calculation for LCLS dechirper: a = 0.7 mm, y = 0.5 mm. The above analytical result is given by green dashes, numerical ECHO(2D) results by the blue curve. The Gaussian bunch shape ($\sigma_z = 10 \text{ }\mu\text{m}$), with head to the left, is given in black dashes

Example Numerical Comparison Cont'd

• Dipole bunch wake of Gaussian beam offset by y from axis of a two-plate dechirper of gap 2a



Example calculation for LCLS dechirper: a = 0.7 mm, y = 0.5 mm. The above analytical result is given by green dashes, numerical ECHO(2D) results by the blue curve. The Gaussian bunch shape ($\sigma_z = 10 \text{ }\mu\text{m}$), with head to the left, is given in black dashes