

KEK連携コロキウム・研究会エディション
「量子多体系の素核・物性クロスオーバー」

1.15 .2019

ワイル半金属における 軸性アノマリーと磁化ダイナミクス

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ワイル半金属における 軸性アノマリーと磁化ダイナミクス

Collaborators



Daichi Kurebayashi
(RIKEN)



Yasu Araki
(JAEA)

Outline

- Introduction – Spintronics and Weyl fermions
- Chiral anomaly and magnetization dynamics
- Axial Hall effect and domain-wall dynamics

Outline

- Introduction – Spintronics and Weyl fermions
- Chiral anomaly and magnetization dynamics
- Axial Hall effect and domain-wall dynamics

Spintronics

Main purpose:

Electrical control of **spin magnetization**

Spintronics

Topological materials for spintronics



- ✓ Robust against perturbations
- ✓ Less-dissipation devices
- ✓ Strong spin-orbit coupling

What is a Weyl semimetal?

3-dimensional analogue of graphene

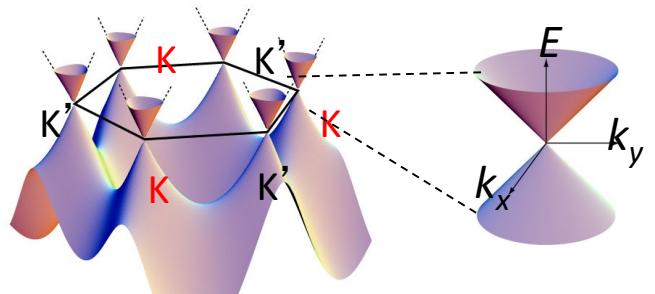
2D (Graphene)

$$H^{2D} = p_x \sigma_x + p_y \sigma_y$$

3D (Weyl semimetal)

$$H^{3D} = p_x \sigma_x + p_y \sigma_y + p_z \sigma_z$$

$$E(p) = \pm v_F \sqrt{p_x^2 + p_y^2} \quad \text{Wallace (1947)}$$



$$E(p) = \pm v_F \sqrt{p_x^2 + p_y^2 + p_z^2}$$

Murakami (2007)
Wan et al. (2011)
Burkov&Balents (2012)
Halasz&Balents (2012)
....

What is a Weyl semimetal?

3-dimensional analogue of graphene

2D (Graphene)

$$H^{2D} = p_x \sigma_x + p_y \sigma_y$$

σ_i : **pseudo**-spin

sublattice degrees of freedom

(Weak SOC)

3D (Weyl semimetal)

$$H^{3D} = p_x \sigma_x + p_y \sigma_y + p_z \sigma_z$$

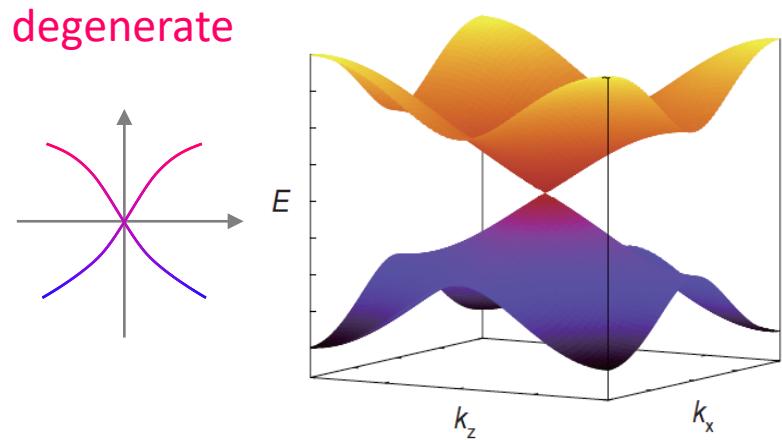
σ_i : **real**-spin

magnetic degrees of freedom

(Strong SOC)

Dirac-Weyl semimetals

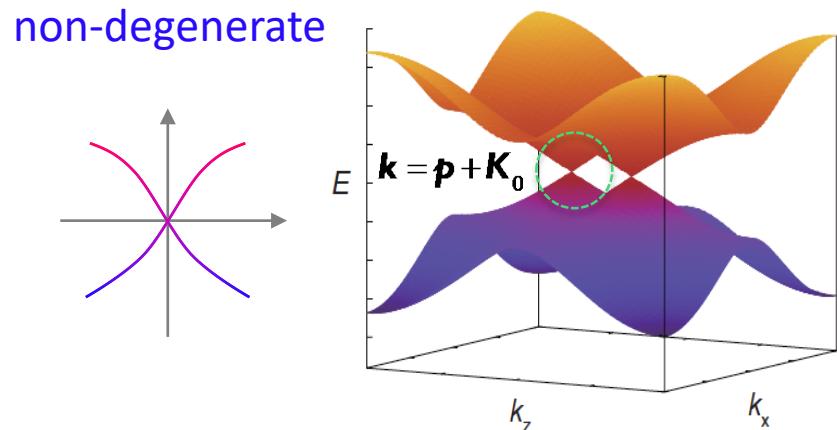
- Dirac semimetals



$$H = p_x \alpha_1 + p_y \alpha_2 + p_z \alpha_3$$

α_i : 4x4 Dirac matrix

- Weyl semimetals



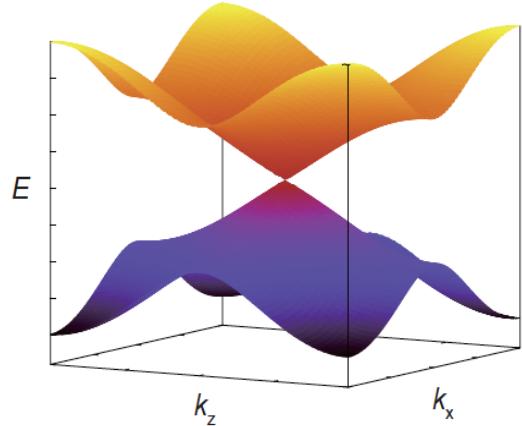
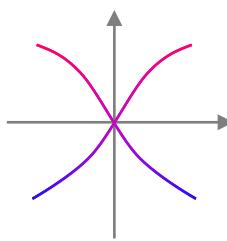
$$H = p_x \sigma_1 + p_y \sigma_2 + p_z \sigma_3$$

σ_i : 2x2 Pauli matrix

Dirac-Weyl semimetals

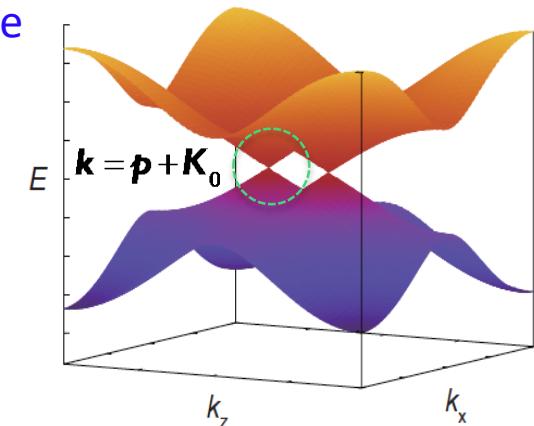
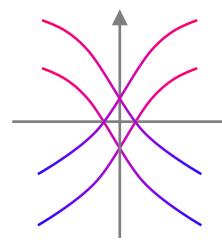
- Dirac semimetals

degenerate



- Weyl semimetals

non-degenerate



$$H = p_x \alpha_1 + p_y \alpha_2 + p_z \alpha_3$$

Breaking of

- Inversion symmetry
- Time-reversal symmetry

α_i : 4x4

$$H = p_x \alpha_1 + p_y \sigma_2 + p_z \sigma_3$$

σ_i : 2x2 Pauli matrix

Weyl semimetals

Weyl semimetals

with broken inversion sym.

TaAs, TaP, NbAs, NbP

(Non-magnetic)



Weyl semimetals

with broken time-reversal sym.

$A_2\text{Ir}_2\text{O}_7$

Magnetically doped TI

Mn_3Sn , $\text{Co}_3\text{Sn}_2\text{S}_2$

(magnetic)



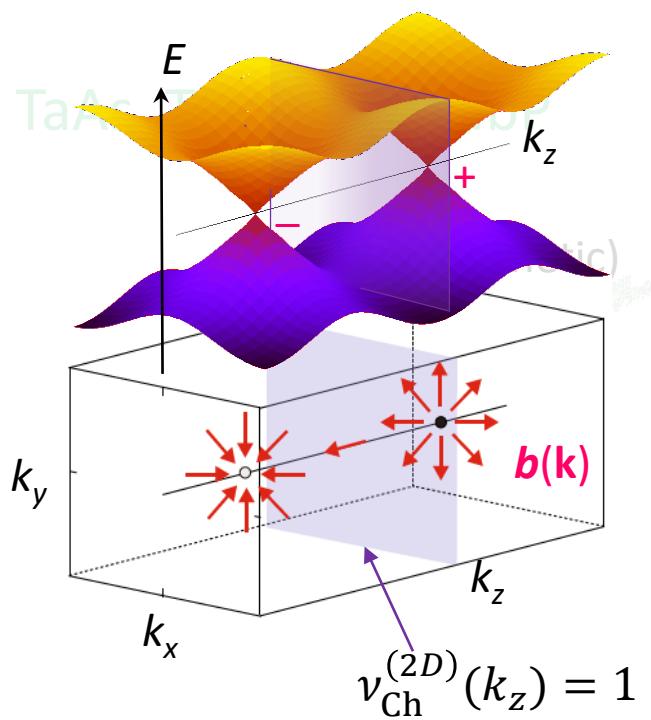
Breaking of

- Inversion symmetry
- Time-reversal symmetry

Weyl semimetals

Weyl semimetals

with broken inversion sym.



Weyl semimetals

with broken time-reversal sym.



Magnetically doped TI

Mn_3Sn , $\text{Co}_3\text{Sn}_2\text{S}_2$

(magnetic)

$b(\mathbf{k})$: Berry curvature

Weyl points = “magnetic monopoles”

$$\sigma_{xy}^{\text{AHE}} = \frac{e^2}{4\pi^2\hbar} \Delta K_z$$

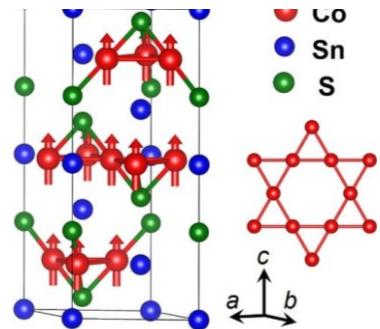
Weyl semimetals

Weyl semimetals

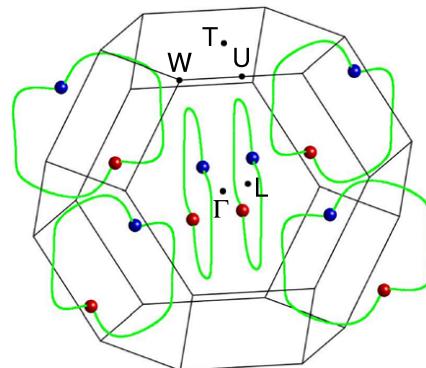
with broken inversion sym.

TaAs, TaP, NbAs, NbP

$\text{Co}_3\text{Sn}_2\text{S}_2$



(Non-magnetic)

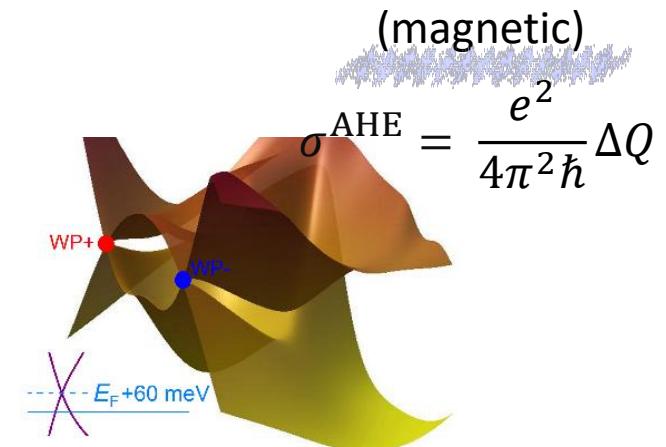


Weyl semimetals

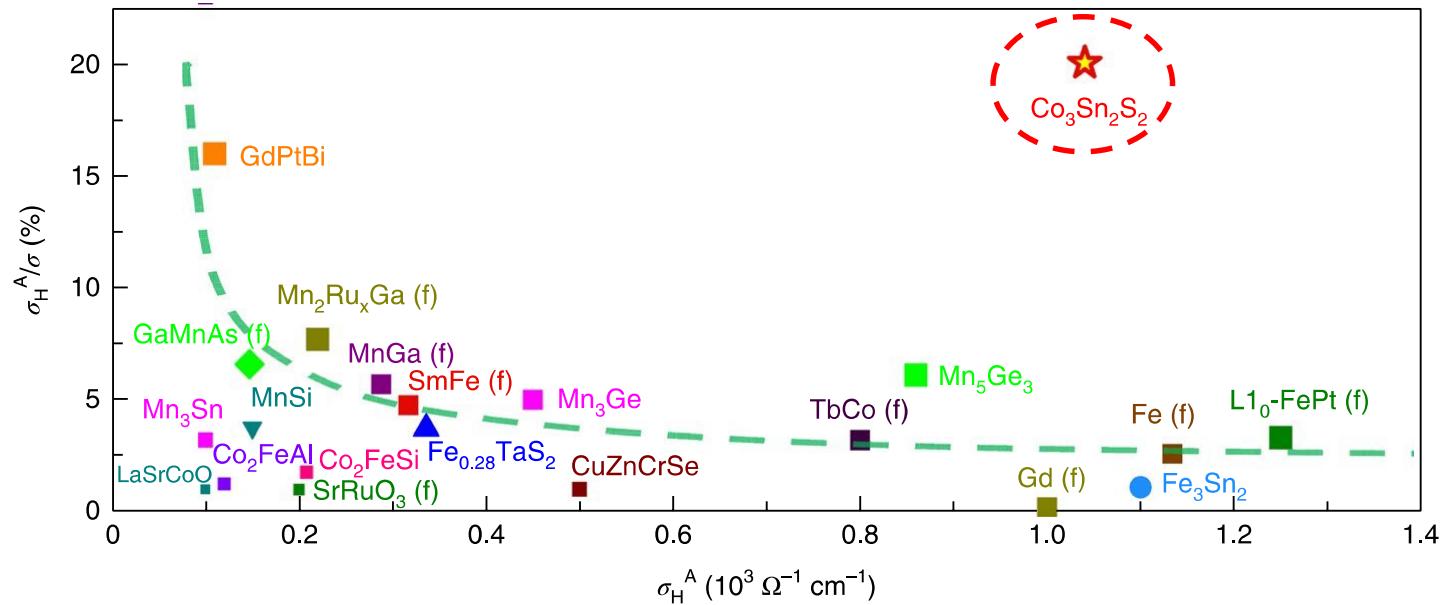
with broken time-reversal sym.

$A_2\text{Ir}_2\text{O}_7$

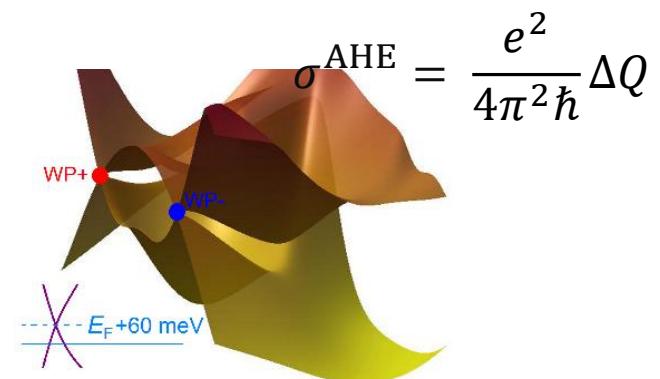
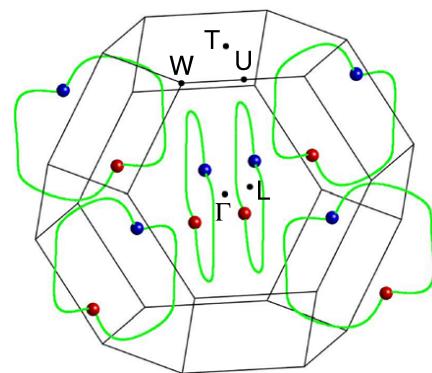
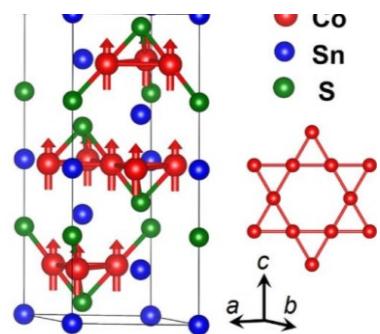
Magnetically doped TI
 $\text{Mn}_3\text{Sn}, \text{Co}_3\text{Sn}_2\text{S}_2$



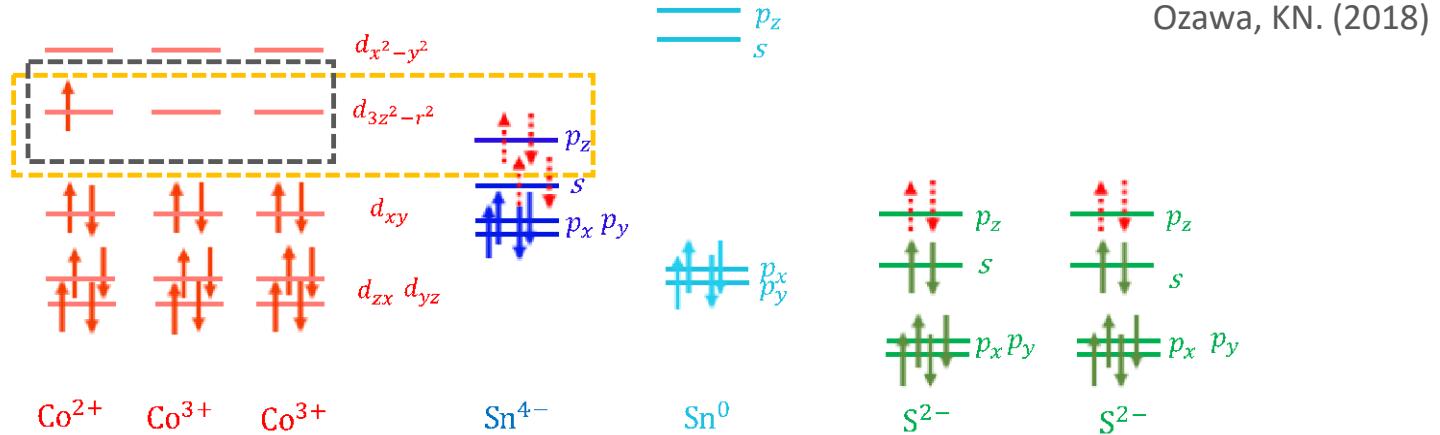
Weyl semimetals



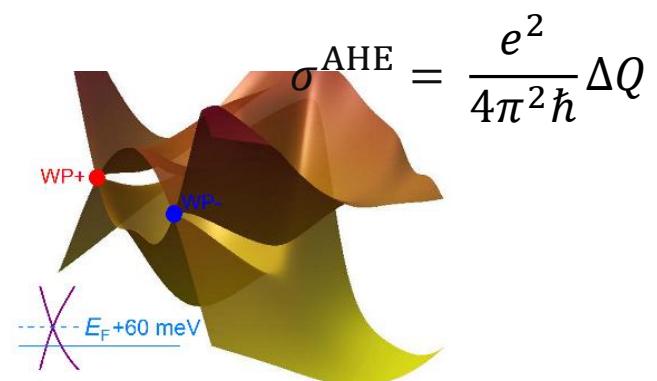
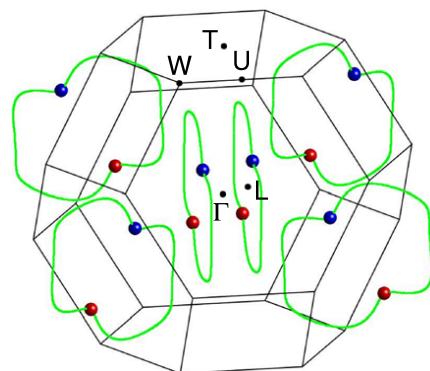
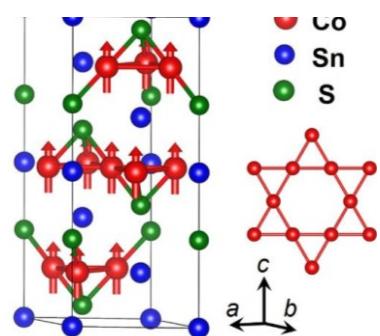
$\text{Co}_3\text{Sn}_2\text{S}_2$



Weyl semimetals

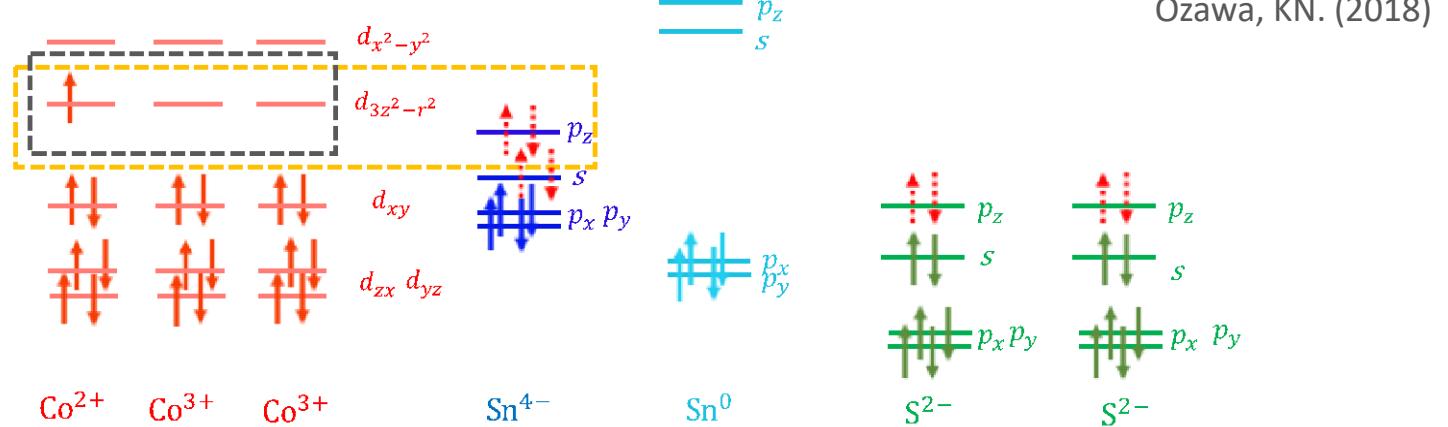


$Co_3Sn_2S_2$

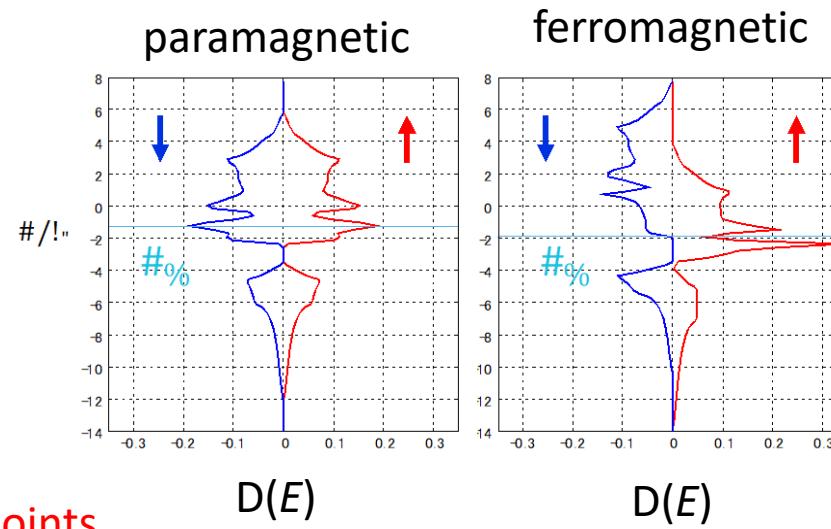
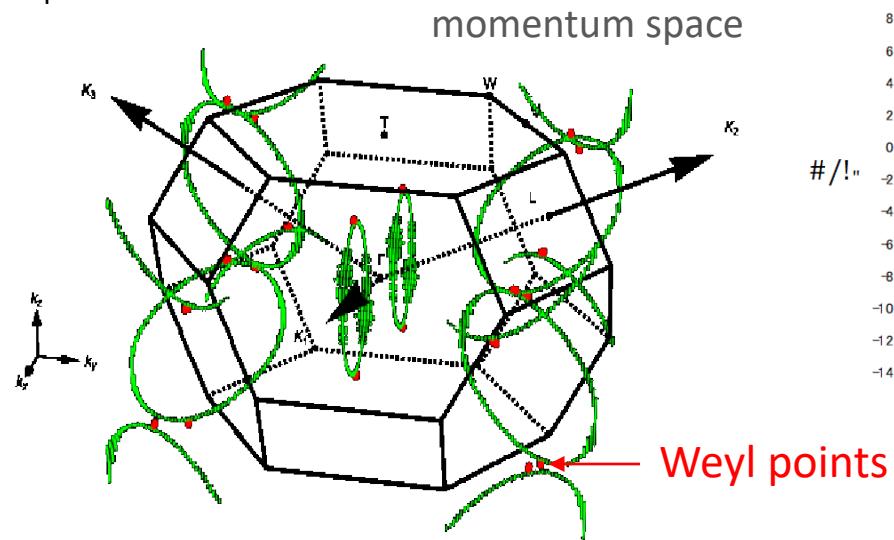


Liu et al. (2018)

Weyl semimetals



$$H = H_{\text{dp}} + H_{\text{exc}} + H_{\text{so}} + H_U$$

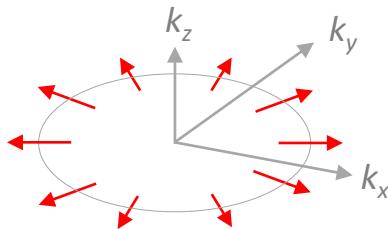


Types of spin-orbit coupling

Weyl-type

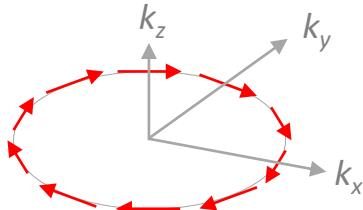
$$k_x \sigma_x \tau_z + k_y \sigma_y \tau_z + k_z \sigma_z \tau_z$$

σ : spin



Rashba-type

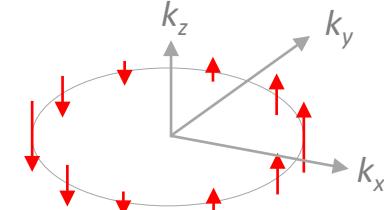
$$k_x \sigma_y \tau_x - k_y \sigma_x \tau_x + k_z \tau_y$$



Topological insulator
(Bi_2Se_3 , Bi_2Te_3 , etc)

BHZ-type

$$k_x \sigma_z \tau_x - k_y \tau_y + k_z \tau_z$$



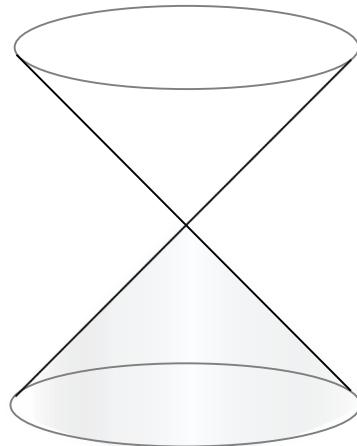
HgTe/CdTe , Cd_3As_2 , $\text{Co}_3\text{Sn}_2\text{S}_2$

Chiral anomaly

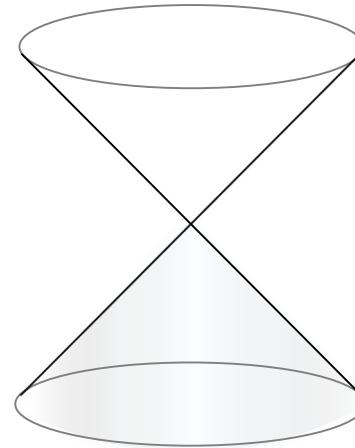
Chiral anomaly

$B = 0$

left handed



right handed



$$H = \begin{pmatrix} H_R & 0 \\ 0 & H_L \end{pmatrix}$$

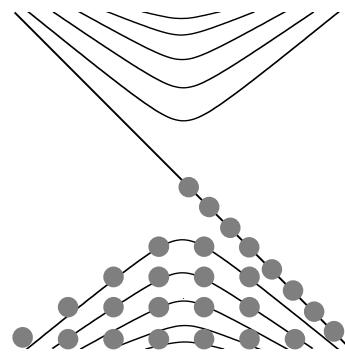
$$H_L = -\boldsymbol{\sigma} \cdot (\mathbf{p} + e\mathbf{A} + JM)$$

$$H_R = +\boldsymbol{\sigma} \cdot (\mathbf{p} + e\mathbf{A} - JM)$$

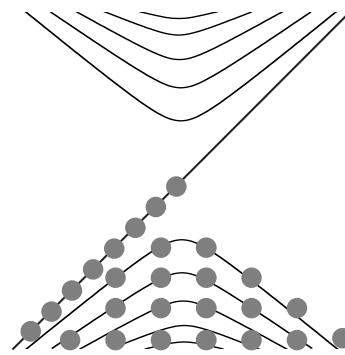
Chiral anomaly

$B \neq 0$

left handed



right handed



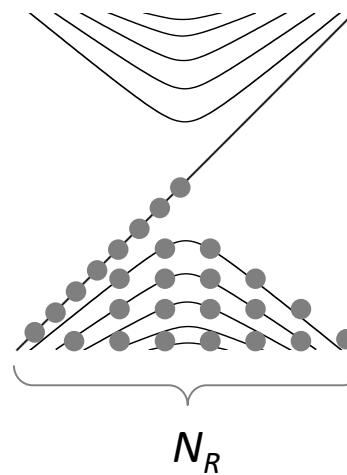
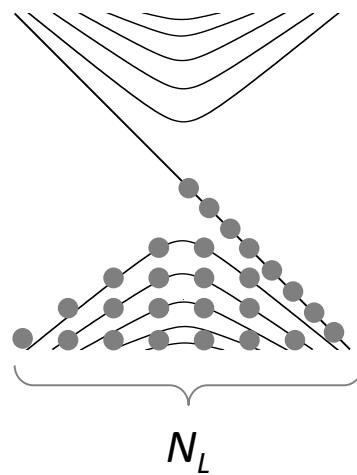
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Chiral anomaly

$B \neq 0$



$$n_\Phi = \frac{BL_xL_y}{\phi_0}$$

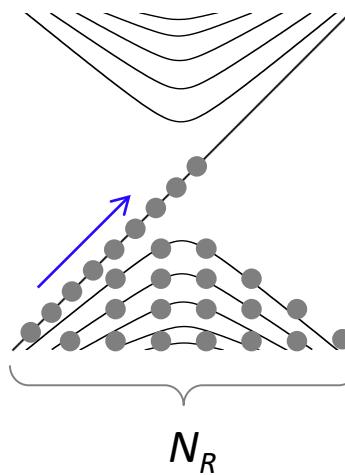
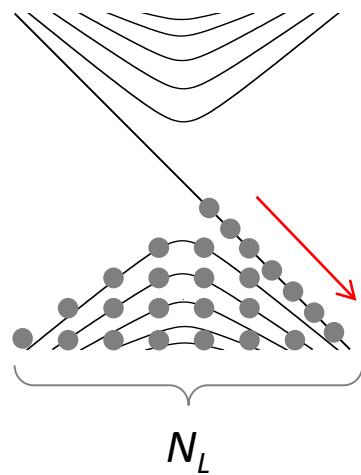
Landau level degeneracy

Chiral anomaly

$B \neq 0$

$E \neq 0$

$$\dot{k} = eE$$



$$n_\Phi = \frac{BL_xL_y}{\phi_0}$$

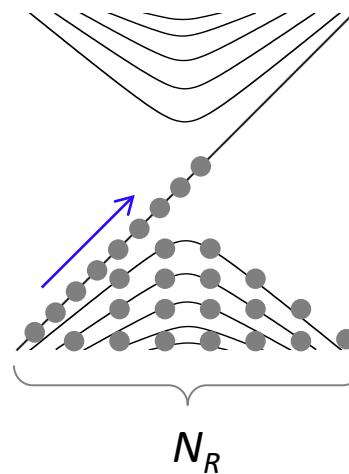
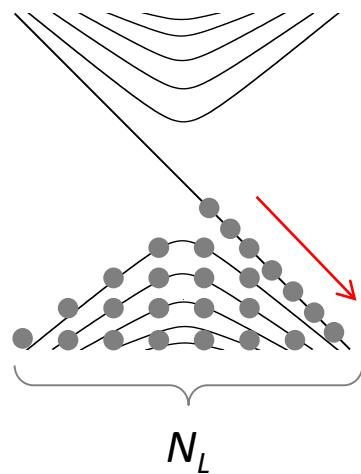
Landau level degeneracy

Chiral anomaly

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$$\dot{k} = eE$$



$$n_\Phi = \frac{BL_xL_y}{\phi_0}$$

Landau level degeneracy

$$\frac{dN_L}{dt} = -n_\Phi \frac{L}{2\pi} eE$$

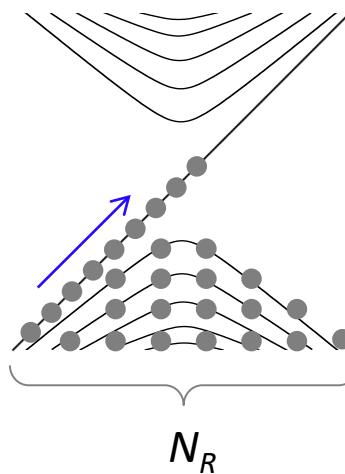
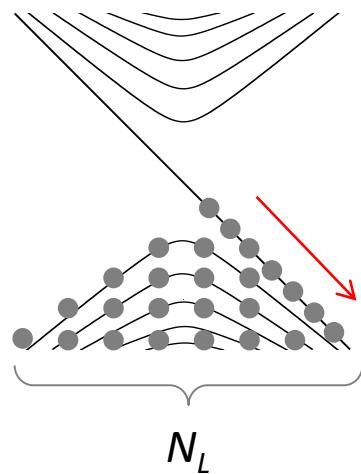
$$\frac{dN_R}{dt} = +n_\Phi \frac{L}{2\pi} eE$$

Chiral anomaly

$$B \neq 0$$

$$E \neq 0$$

$$\dot{k} = eE$$



$$n_\Phi = \frac{BL_x L_y}{\phi_0}$$

Landau level degeneracy

$$\begin{aligned}\frac{dN_L}{dt} &= -n_\Phi \frac{L}{2\pi} eE \\ &= -\frac{L^3}{(2\pi)^2} e^2 \mathbf{E} \cdot \mathbf{B}\end{aligned}$$

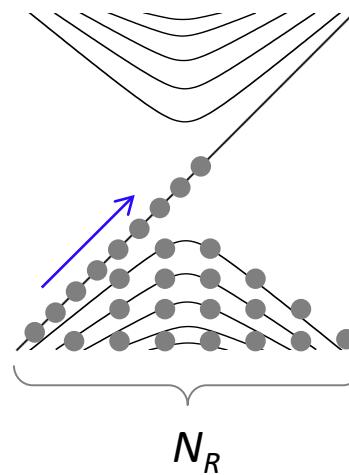
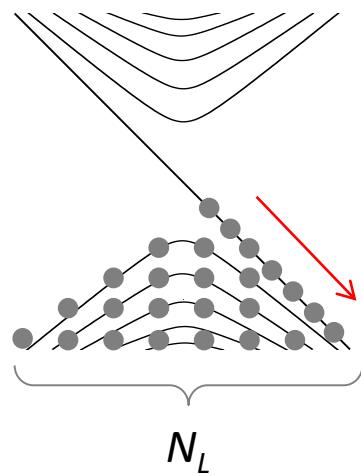
$$\begin{aligned}\frac{dN_R}{dt} &= +n_\Phi \frac{L}{2\pi} eE \\ &= +\frac{L^3}{(2\pi)^2} e^2 \mathbf{E} \cdot \mathbf{B}\end{aligned}$$

Chiral anomaly

$$B \neq 0$$

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$$\dot{k} = eE$$



$$n_\Phi = \frac{BL_xL_y}{\phi_0}$$

Landau level degeneracy

$$\begin{aligned} \frac{dN_L}{dt} &= -n_\Phi \frac{L}{2\pi} eE \\ &= -\frac{L^3}{(2\pi)^2} e^2 \mathbf{E} \cdot \mathbf{B} \end{aligned}$$

$$\begin{aligned} \frac{dN_R}{dt} &= +n_\Phi \frac{L}{2\pi} eE \\ &= +\frac{L^3}{(2\pi)^2} e^2 \mathbf{E} \cdot \mathbf{B} \end{aligned}$$

total charge

$$\frac{d(N_R + N_L)}{dt} = 0$$

axial charge

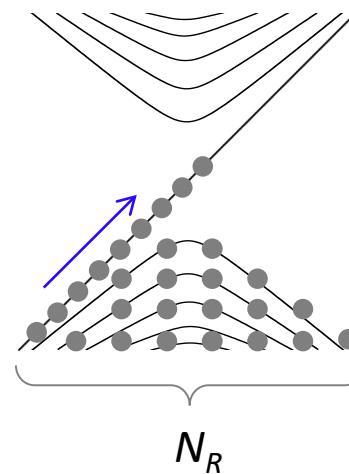
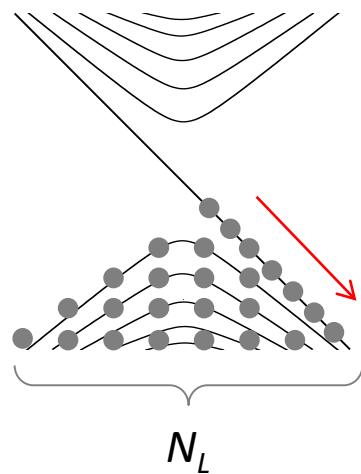
$$\frac{d(N_R - N_L)}{dt} = \int d^3x \frac{e^2}{2\pi^2} \mathbf{E} \cdot \mathbf{B}$$

Chiral anomaly

$$B \neq 0$$

$$E \neq 0$$

$$\dot{k} = eE$$



$$n_\Phi = \frac{BL_x L_y}{\phi_0}$$

Landau level degeneracy

$$\begin{aligned} \frac{dN_L}{dt} &= -n_\Phi \frac{L}{2\pi} eE \\ &= -\frac{L^3}{(2\pi)^2} e^2 \mathbf{E} \cdot \mathbf{B} \end{aligned}$$

$$\begin{aligned} \frac{dN_R}{dt} &= +n_\Phi \frac{L}{2\pi} eE \\ &= +\frac{L^3}{(2\pi)^2} e^2 \mathbf{E} \cdot \mathbf{B} \end{aligned}$$

total charge

$$\partial_\mu j^\mu = 0$$

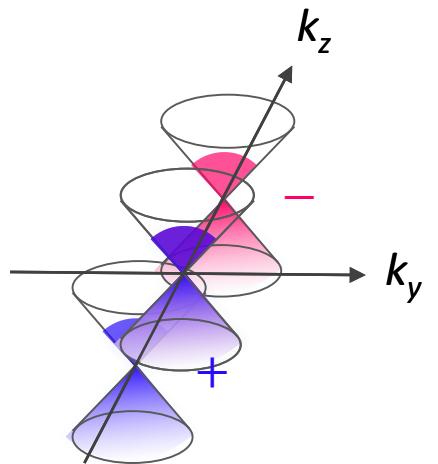
axial charge

$$\partial_\mu j_5^\mu = \frac{e^2}{2\pi^2} \mathbf{E} \cdot \mathbf{B}$$

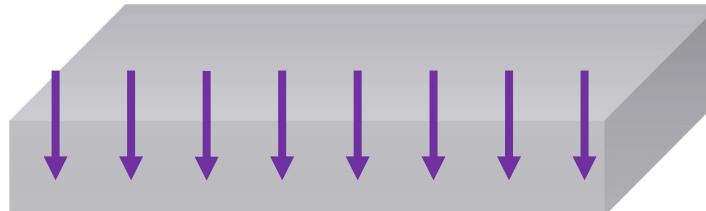
Chiral anomaly

Dirac fermions + exchange interaction

$$H = \begin{pmatrix} \boldsymbol{\sigma} \cdot (\mathbf{p} + e\mathbf{A} + \mathbf{J}\mathbf{M}) & 0 \\ 0 & -\boldsymbol{\sigma} \cdot (\mathbf{p} + e\mathbf{A} - \mathbf{J}\mathbf{M}) \end{pmatrix}$$



total charge



axial charge

$$\partial_\mu j^\mu = 0$$

$$\partial_\mu j_5^\mu = \frac{e^2}{2\pi^2} \mathbf{E} \cdot \mathbf{B}$$

Chiral anomaly

Dirac fermions + exchange interaction

$$H = \begin{pmatrix} \boldsymbol{\sigma} \cdot (\mathbf{p} + e\mathbf{A} + \mathbf{J}\mathbf{M}) & 0 \\ 0 & -\boldsymbol{\sigma} \cdot (\mathbf{p} + e\mathbf{A} - \mathbf{J}\mathbf{M}) \end{pmatrix}$$
$$= \tau_z \boldsymbol{\sigma} \cdot \mathbf{p} + \mathbf{j} \cdot \mathbf{A} + \mathbf{j}_5 \cdot \mathbf{A}_5$$

total charge

$$\partial_\mu j^\mu = 0$$

axial charge

$$\partial_\mu j_5^\mu = \frac{e^2}{2\pi^2} \mathbf{E} \cdot \mathbf{B}$$

Chiral anomaly

Dirac fermions + exchange interaction

$$H = \begin{pmatrix} \boldsymbol{\sigma} \cdot (\mathbf{p} + e\mathbf{A} + \mathbf{J}\mathbf{M}) & 0 \\ 0 & -\boldsymbol{\sigma} \cdot (\mathbf{p} + e\mathbf{A} - \mathbf{J}\mathbf{M}) \end{pmatrix}$$

$$= \tau_z \boldsymbol{\sigma} \cdot \mathbf{p} + \mathbf{j} \cdot \mathbf{A} + \mathbf{j}_5 \cdot \mathbf{A}_5$$

$$\mathbf{E}_5 = -\dot{\mathbf{A}}_5$$

$$\mathbf{B}_5 = \nabla \times \mathbf{A}_5$$

total charge

$$\partial_\mu j^\mu = \frac{e^2}{2\pi^2} (\mathbf{E}_5 \cdot \mathbf{B} + \mathbf{E} \cdot \mathbf{B}_5)$$

axial charge

$$\partial_\mu j_5^\mu = \frac{e^2}{2\pi^2} (\mathbf{E} \cdot \mathbf{B} + \mathbf{E}_5 \cdot \mathbf{B}_5)$$

Anomalous transport phenomena

$$\partial_\mu j^\mu = \frac{e^2}{2\pi^2} (\mathbf{E}_5 \cdot \mathbf{B} + \mathbf{E} \cdot \mathbf{B}_5)$$

$\underbrace{\phantom{\partial_\mu j^\mu = \frac{e^2}{2\pi^2} (\mathbf{E}_5 \cdot \mathbf{B} + \mathbf{E} \cdot \mathbf{B}_5)}}$

$$-\partial_\mu j^\mu_{\text{anomaly}}$$

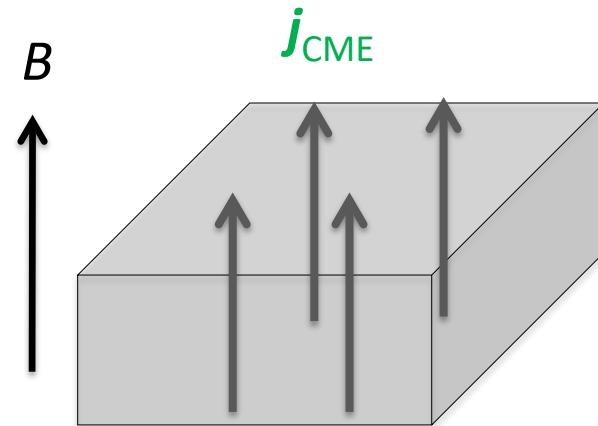
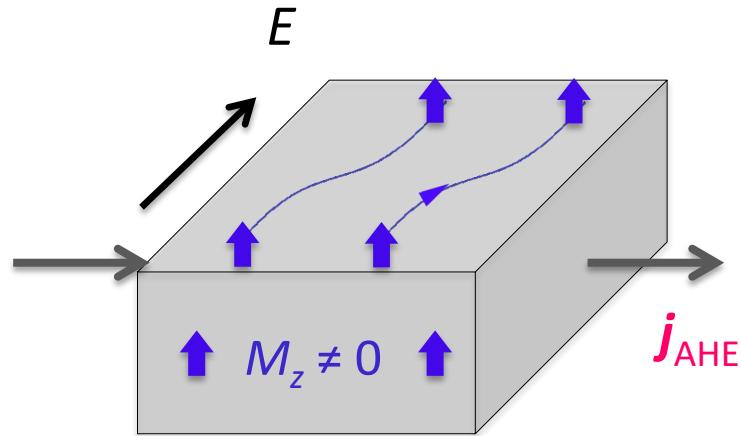
$$\mathbf{E}_5 = -\dot{\mathbf{A}}_5 - \nabla \mu_5 / e \quad \mathbf{B}_5 = \nabla \times \mathbf{A}_5$$

$$\mathbf{j}_{\text{anomaly}} = \frac{e^2}{2\pi^2} \mathbf{A}_5 \times \mathbf{E} + \frac{e^2}{2\pi^2} \mu_5 \mathbf{B}$$

↑
Anomalous Hall effect ↑
Chiral magnetic effect

$$\rho_{\text{anomaly}} = \frac{e^2}{2\pi^2} \mathbf{A}_5 \cdot \mathbf{B}$$

Anomalous transport phenomena



Fukushima, Kharzeev, and Warringa (2008)

$$\mathbf{j}_{\text{anomaly}} = \frac{e^2}{2\pi^2} \mathbf{A}_5 \times \mathbf{E} + \frac{e^2}{2\pi^2} \mu_5 \mathbf{B}$$

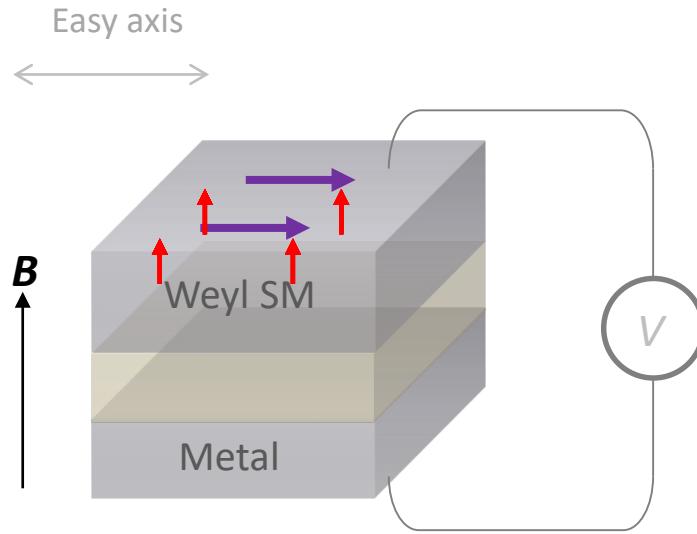
↑
Anomalous Hall effect ↑
Chiral magnetic effect

$$\rho_{\text{anomaly}} = \frac{e^2}{2\pi^2} \mathbf{A}_5 \cdot \mathbf{B}$$

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- Axial Hall effect and domain-wall dynamics

Voltage induced spin torque



$\hat{\mathbf{M}}$: local magnetization

σ : spin of Weyl electrons

Kurebayashi, KN (2016)

$$H_{\text{exc}} = J \hat{\mathbf{M}} \cdot \boldsymbol{\sigma}$$

$$\langle \boldsymbol{\sigma} \rangle = \frac{e^2}{2\pi^2 \hbar^2 v_F} V \mathbf{B}$$

Voltage induced spin torque

$$\langle \sigma \rangle = \frac{e^2}{2\pi^2 \hbar^2 v_F} V B$$

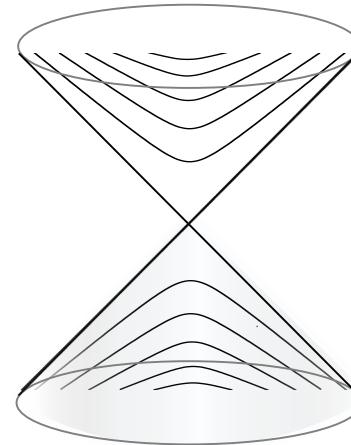
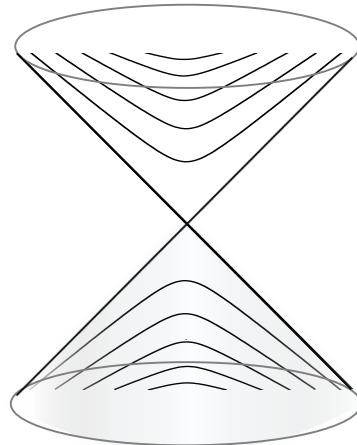
Weyl fermions in B field

$$H = \begin{pmatrix} H_{\textcolor{blue}{R}} & 0 \\ 0 & H_{\textcolor{red}{L}} \end{pmatrix}$$

$$H_{\textcolor{red}{L}} = -\boldsymbol{\sigma} \cdot (\boldsymbol{p} + e\boldsymbol{A} + JM) \quad H_{\textcolor{blue}{R}} = +\boldsymbol{\sigma} \cdot (\boldsymbol{p} + e\boldsymbol{A} - JM)$$

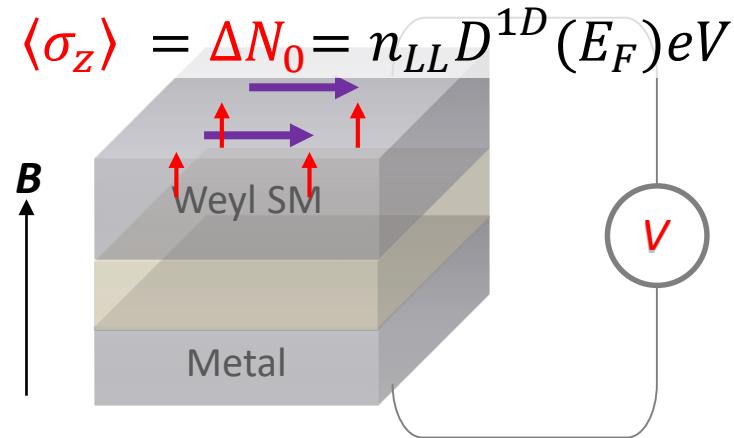
$B \neq 0$

left handed



$$\langle \boldsymbol{\sigma} \rangle = \frac{e^2}{2\pi^2 \hbar^2 v_F} VB$$

Weyl fermions in B field



$$\frac{d\hat{\mathbf{M}}}{dt} = -\gamma \hat{\mathbf{M}} \times \mathbf{H}_{\text{eff}} + \alpha \hat{\mathbf{M}} \times \frac{d\hat{\mathbf{M}}}{dt} + J \hat{\mathbf{M}} \times \langle \boldsymbol{\sigma} \rangle$$

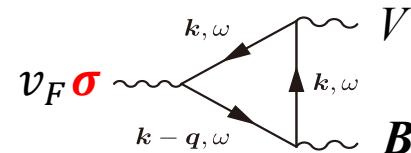
$$\langle \boldsymbol{\sigma} \rangle = \frac{e^2}{2\pi^2 \hbar^2 v_F} V \mathbf{B}$$

Relation to chiral anomaly

Anomaly equation of the axial current

$$\nabla \cdot \mathbf{j}_5 = \frac{e^2}{2\pi^2 \hbar^2} (-\nabla V) \cdot \mathbf{B}$$

$$\mathbf{j}_5 = \frac{\partial H}{\partial A_5} = -e v_F \boldsymbol{\sigma}$$



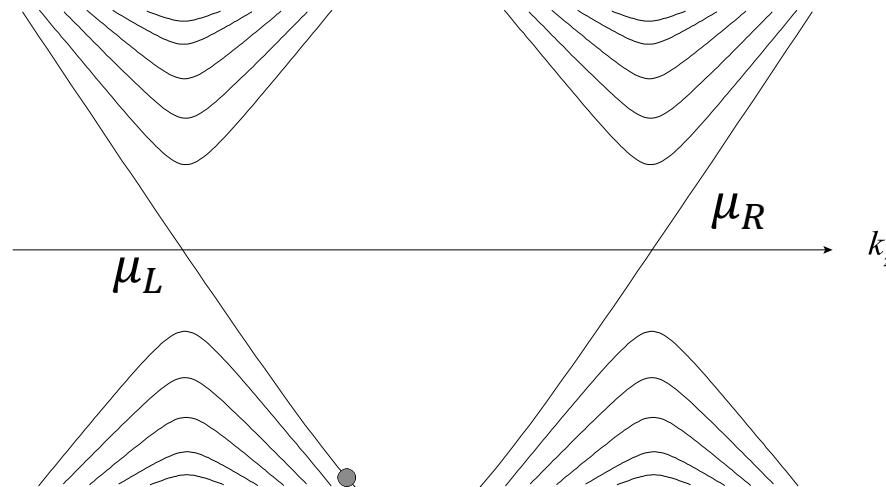
$$\langle \boldsymbol{\sigma} \rangle = \frac{e^2}{2\pi^2 \hbar^2 v_F} V \mathbf{B}$$

Chiral magnetic effects

$$\mathbf{j}_L = -\frac{e^2}{2\pi^2} \mu_L \mathbf{B}_L \quad \mathbf{j}_R = +\frac{e^2}{2\pi^2} \mu_R \mathbf{B}_R$$

$$\left\{ \begin{array}{l} \mathbf{B}_{R/L} = \mathbf{B} \pm \mathbf{B}_5 \\ \mu_{R/L} = \mu \pm \mu_5 \end{array} \right.$$

Fukushima, Kharzeev, and Warringa (2008)



Chiral magnetic effects

$$\mathbf{j}_L = -\frac{e^2}{2\pi^2} \mu_L \mathbf{B}_L$$

$$\mathbf{j}_R = +\frac{e^2}{2\pi^2} \mu_R \mathbf{B}_R$$

$$\left\{ \begin{array}{l} \mathbf{B}_{R/L} = \mathbf{B} \pm \mathbf{B}_5 \\ \mu_{R/L} = \mu \pm \mu_5 \end{array} \right.$$

$$\mathbf{j} = \mathbf{j}_R + \mathbf{j}_L$$

Electrical current

Fukushima, Kharzeev, and Warringa (2008)

$$\mathbf{j} = \frac{e^2}{2\pi^2} \mu_5 \mathbf{B}$$

$$\mathbf{j} = \frac{e^2}{2\pi^2} \mu \mathbf{B}_5$$

Chiral magnetic effects

$$\mathbf{j}_L = -\frac{e^2}{2\pi^2} \mu_L \mathbf{B}_L$$

$$\mathbf{j}_R = +\frac{e^2}{2\pi^2} \mu_R \mathbf{B}_R$$

$$\left. \begin{array}{l} \mathbf{B}_{R/L} = \mathbf{B} \pm \mathbf{B}_5 \\ \mu_{R/L} = \mu \pm \mu_5 \end{array} \right\}$$

$$\mathbf{j} = \mathbf{j}_R + \mathbf{j}_L$$

Electrical current

$$\mathbf{j} = \frac{e^2}{2\pi^2} \mu_5 \mathbf{B}$$

$$\mathbf{j} = \frac{e^2}{2\pi^2} \mu \mathbf{B}_5$$

$$\mathbf{j}_5 = \mathbf{j}_R - \mathbf{j}_L$$

Axial current

$$\mathbf{j}_5 = \frac{e^2}{2\pi^2} \mu \mathbf{B}$$

Chiral magnetic effects

Axial current

$$\mathbf{j}_5 = \frac{e^2}{2\pi^2} \mu \mathbf{B}$$

Chiral magnetic effects

$$H = \begin{pmatrix} H_+ & 0 \\ 0 & H_- \end{pmatrix} \quad H_{\pm} = \pm v \boldsymbol{\sigma} \cdot (\mathbf{p} + e\mathbf{A} \pm e\mathbf{A}_5) + eA^0 \pm eA_5^0$$

$$\mathbf{j}_5 = -\frac{\partial H}{\partial \mathbf{A}_5} = -ev\boldsymbol{\sigma}$$

Spin density

Axial current

$$\langle \boldsymbol{\sigma} \rangle = \frac{-e}{2\pi^2 v} \mu \mathbf{B}$$

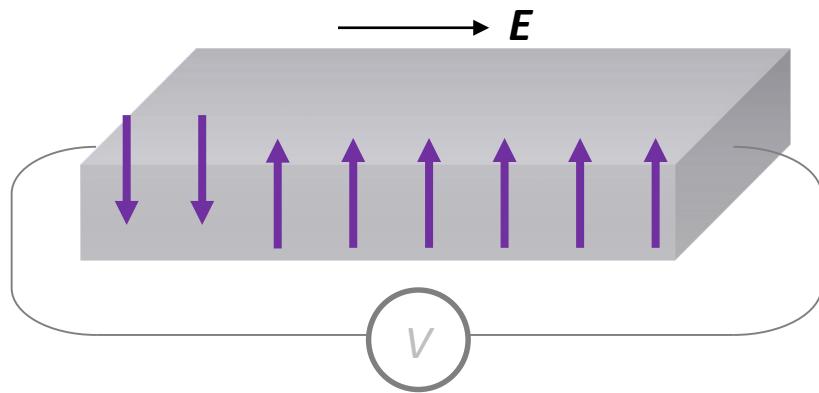


$$\mathbf{j}_5 = \frac{e^2}{2\pi^2} \mu \mathbf{B}$$

Outline

- Introduction – Spintronics and Weyl fermions
- Chiral anomaly and magnetization dynamics
- Axial Hall effect and domain-wall dynamics

Domain wall in Weyl semimetal



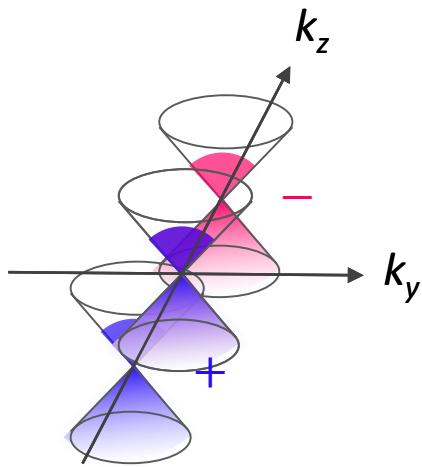
Spin torques in conventional metals

$$\mathbf{T}_E = (\nabla \cdot \mathbf{v}_s) \hat{\mathbf{M}} + \beta \hat{\mathbf{M}} \times (\nabla \cdot \mathbf{v}_s) \hat{\mathbf{M}}$$

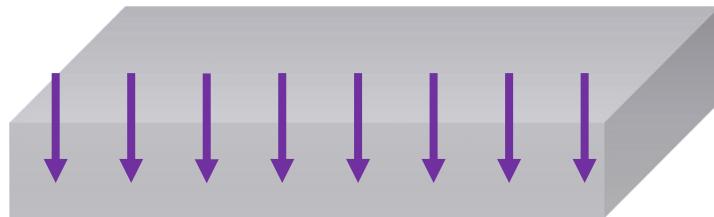
adiabatic

non-adiabatic ($\beta \sim 0.01$)

Domain wall in Weyl semimetal

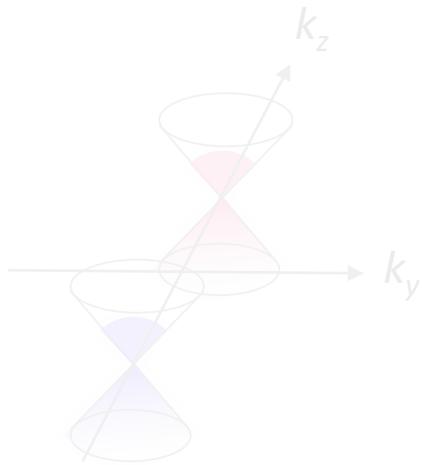


$$\begin{aligned} H_{\pm} &= \pm \boldsymbol{\sigma} \cdot \mathbf{p} + \textcolor{violet}{J}\mathbf{M} \cdot \boldsymbol{\sigma} \\ &= \pm \boldsymbol{\sigma} \cdot (\mathbf{p} \pm e\textcolor{violet}{A}_5) \end{aligned}$$

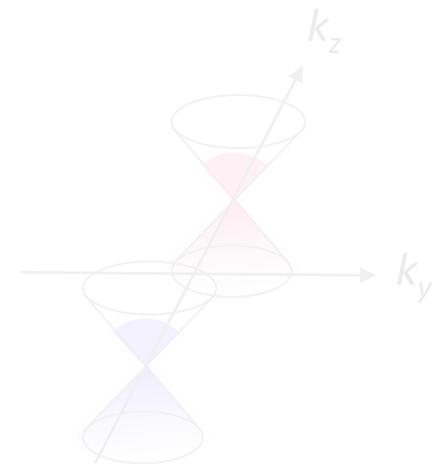
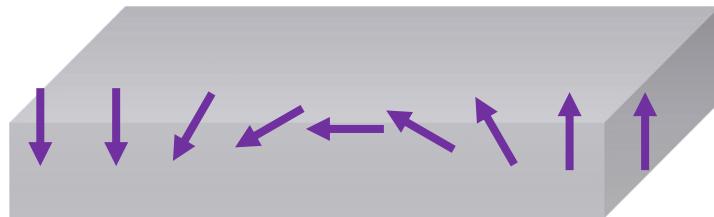


Magnetic Weyl semimetal

Domain wall in Weyl semimetal



$$\begin{aligned} H_{\pm} &= \pm \boldsymbol{\sigma} \cdot \mathbf{p} + \textcolor{violet}{J}\mathbf{M} \cdot \boldsymbol{\sigma} \\ &= \pm \boldsymbol{\sigma} \cdot \mathbf{p} + \textcolor{violet}{A}_5 \cdot \mathbf{j}_5 \end{aligned}$$



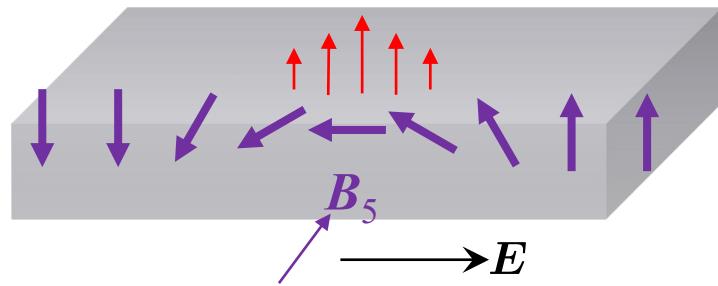
$$\mathbf{B} = \nabla \times \mathbf{A}$$

$$\mathbf{B}_5 = \nabla \times \mathbf{A}_5 \propto \nabla \times \mathbf{M}$$

Domain wall in Weyl semimetal

$$H_{\pm} = \pm \boldsymbol{\sigma} \cdot \boldsymbol{p} + \textcolor{violet}{J}\boldsymbol{M} \cdot \boldsymbol{\sigma}$$

$$= \pm \boldsymbol{\sigma} \cdot \boldsymbol{p} + \textcolor{red}{A}_5 \cdot \textcolor{red}{j}_5$$

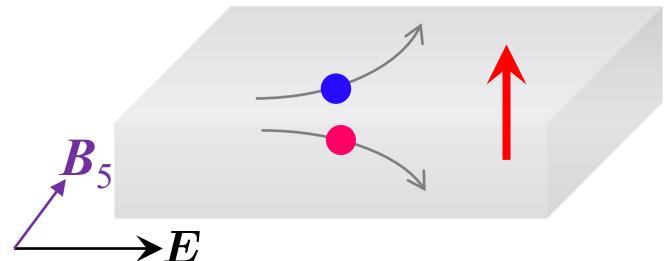


$$\boldsymbol{B}_5 = \nabla \times \boldsymbol{A}_5 \propto \nabla \times \boldsymbol{M}$$

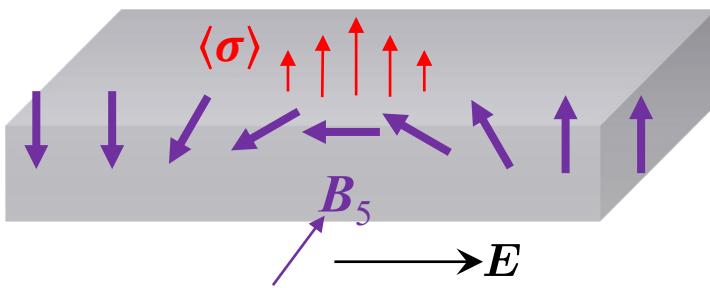
$$\textcolor{red}{j}_5 = \sigma_H \hat{\boldsymbol{B}}_5 \times \boldsymbol{E}$$

$$= \frac{\sigma_H}{e\nu_F} \frac{\nabla \times \hat{\boldsymbol{M}}}{|\nabla \times \hat{\boldsymbol{M}}|} \times \boldsymbol{E}$$

$$\textcolor{red}{j}_5 = j_+ - j_- \propto \boldsymbol{\sigma}$$



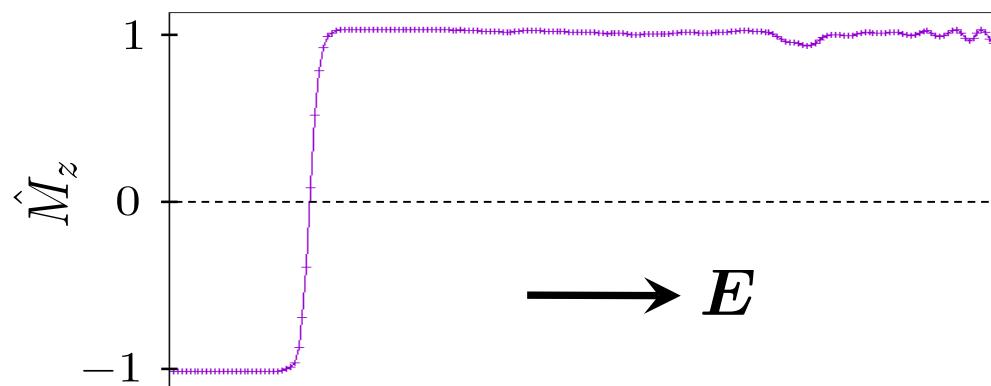
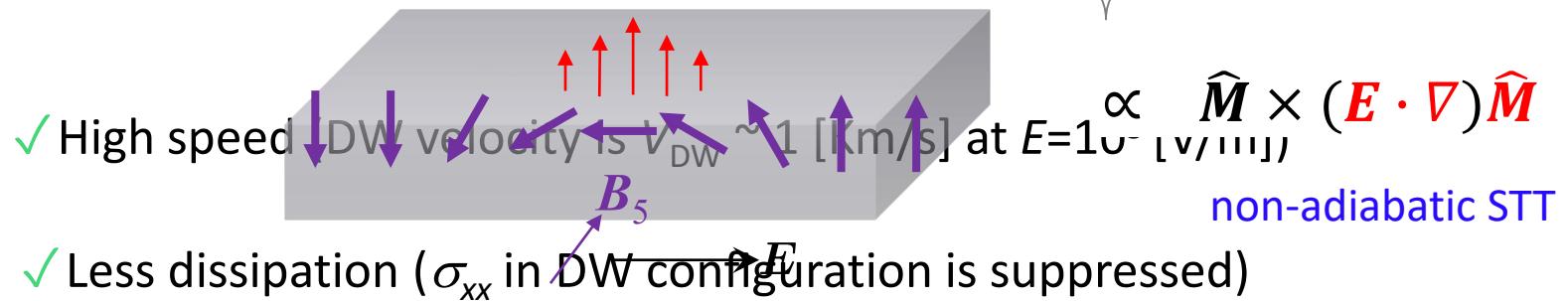
Domain wall in Weyl semimetal

$$\frac{d\hat{\mathbf{M}}}{dt} = -\gamma \hat{\mathbf{M}} \times \mathbf{H}_{\text{eff}} + \alpha \hat{\mathbf{M}} \times \frac{d\hat{\mathbf{M}}}{dt} + J \hat{\mathbf{M}} \times \underbrace{\frac{\sigma_H}{e\nu_F} \frac{\nabla \times \hat{\mathbf{M}}}{|\nabla \times \hat{\mathbf{M}}|} \times \mathbf{E}}_{\propto \hat{\mathbf{M}} \times (\mathbf{E} \cdot \nabla) \hat{\mathbf{M}}} \quad \text{non-adiabatic STT}$$


$$\begin{aligned}\langle \boldsymbol{\sigma} \rangle &= \frac{\mathbf{j}_5}{e\nu_F} = \frac{\sigma_H \hat{\mathbf{B}}_5 \times \mathbf{E}}{e\nu_F} \\ &= \frac{\sigma_H}{e\nu_F} \frac{\nabla \times \hat{\mathbf{M}}}{|\nabla \times \hat{\mathbf{M}}|} \times \mathbf{E}\end{aligned}$$

Domain wall in Weyl semimetal

$$\frac{d\hat{\mathbf{M}}}{dt} = -\gamma \hat{\mathbf{M}} \times \mathbf{H}_{\text{eff}} + \alpha \hat{\mathbf{M}} \times \frac{d\hat{\mathbf{M}}}{dt} + J \hat{\mathbf{M}} \times \underbrace{\frac{\sigma_H}{ev_F} \frac{\nabla \times \hat{\mathbf{M}}}{|\nabla \times \hat{\mathbf{M}}|} \times \mathbf{E}}$$



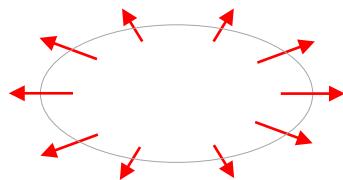
Daichi Kurebayashi

Types of SO coupling

Weyl-type SOC

Weyl nodes

$$p_x \tau_z \sigma_x + p_y \tau_z \sigma_y + p_z \tau_z \sigma_z$$



Rashba-type SOC

Rashba nodes

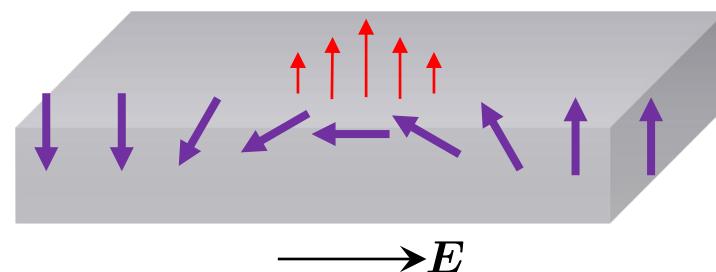
$$p_x \tau_x \sigma_y - p_y \tau_x \sigma_x + p_z \tau_y$$



BHZ-type SOC

BHZ nodes

$$p_x \tau_x \sigma_z - p_y \tau_y + p_z \tau_z$$



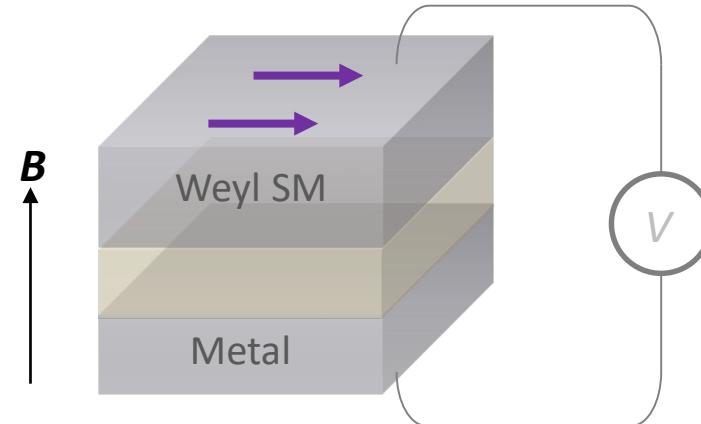
Daichi Kurebayashi

Spin torque is insensitive to the type of SOC

Summary

- Voltage induced spin switching

$$\langle \sigma \rangle = \frac{e^2}{2\pi^2 \hbar^2 v_F} V B$$



Axial anomaly $\nabla \cdot \mathbf{j}_5 \propto \mathbf{E} \cdot \mathbf{B}$

- Current induced domain-wall motion

$$\langle \sigma \rangle = \frac{\sigma_H \hat{\mathbf{B}}_5 \times \mathbf{E}}{e v_F}$$

Axial Hall effect $\mathbf{j}_5 = \sigma_H \hat{\mathbf{B}}_5 \times \mathbf{E}$

