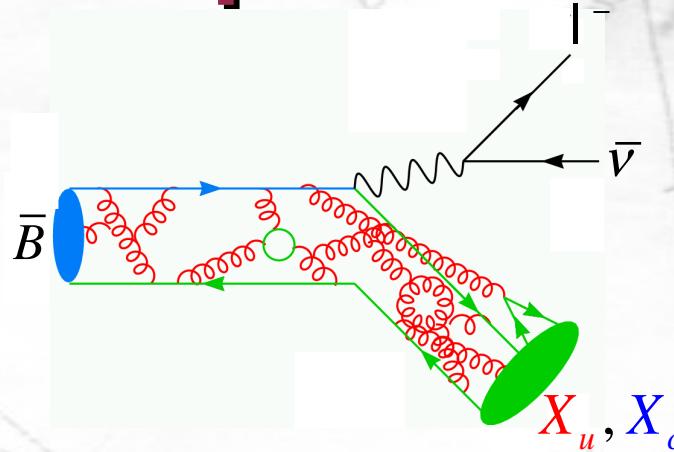


# Semileptonic B Decays at BaBar



Francesca Di Lodovico  
Queen Mary University of London

representing the *BaBar* Collaboration

KEK, January 10 2008

# Outline

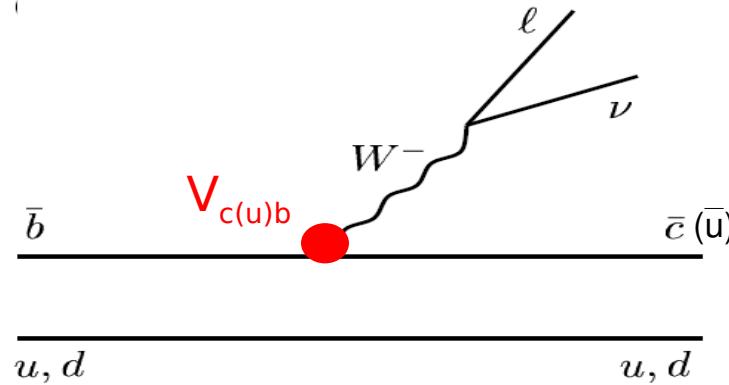
- Introduction
  - ▶ Motivations
  - ▶ BaBar
  - ▶ Experimental approach
- Inclusive decays
  - ▶ Determination of  $|V_{cb}|$
  - ▶ Determination of  $|V_{ub}|$
- Exclusive Decays
  - ▶  $D^{(*)}(\ell\nu)$
  - ▶  $\pi(\eta^{'})\ell\nu$
- Conclusions

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# Semileptonic Decays

$b \rightarrow c \ell \nu, u \ell \nu$



- Semileptonic decays are an important tool to study:
  - CKM matrix elements
  - Heavy quark parameters (eg.  $b$ ,  $c$  quark masses)
  - QCD Form Factors
  - New Physics

# Framework: the CKM Matrix

- $B^+$  and  $B^0$  are the most accessible 3<sup>rd</sup>-generation particles
- Their decays allow detailed studies of the CKM matrix

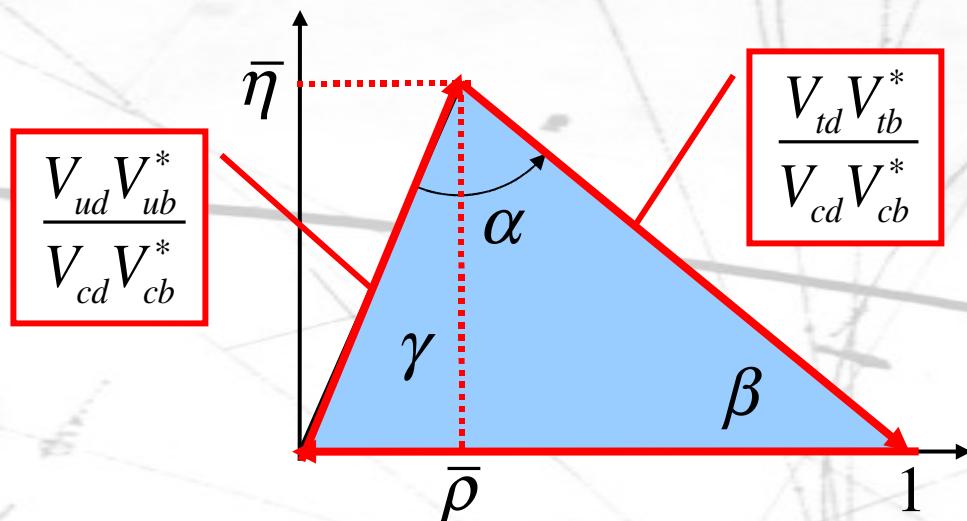
$$L = -\frac{g}{\sqrt{2}} (\bar{u}_L \quad \bar{c}_L \quad \bar{t}_L) \gamma^\mu \begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{bmatrix} \begin{bmatrix} d_L \\ s_L \\ b_L \end{bmatrix} W_\mu^+ + h.c.$$

- Unitary matrix
- $V_{CKM}$  connects the weak to the mass eigenstates
- 3 real parameters + 1 complex phase
- Is this the complete description of the CP violation?
  - Is everything consistent with a single unitary matrix?

The only source of ~~CP~~ in the Minimal SM

# Representation: the Unitarity Triangle

- Unitarity of  $V_{\text{CKM}}$   $\rightarrow V_{\text{CKM}}^\dagger V_{\text{CKM}} = 1 \rightarrow V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$ 
  - This is neatly represented by the familiar Unitarity Triangle



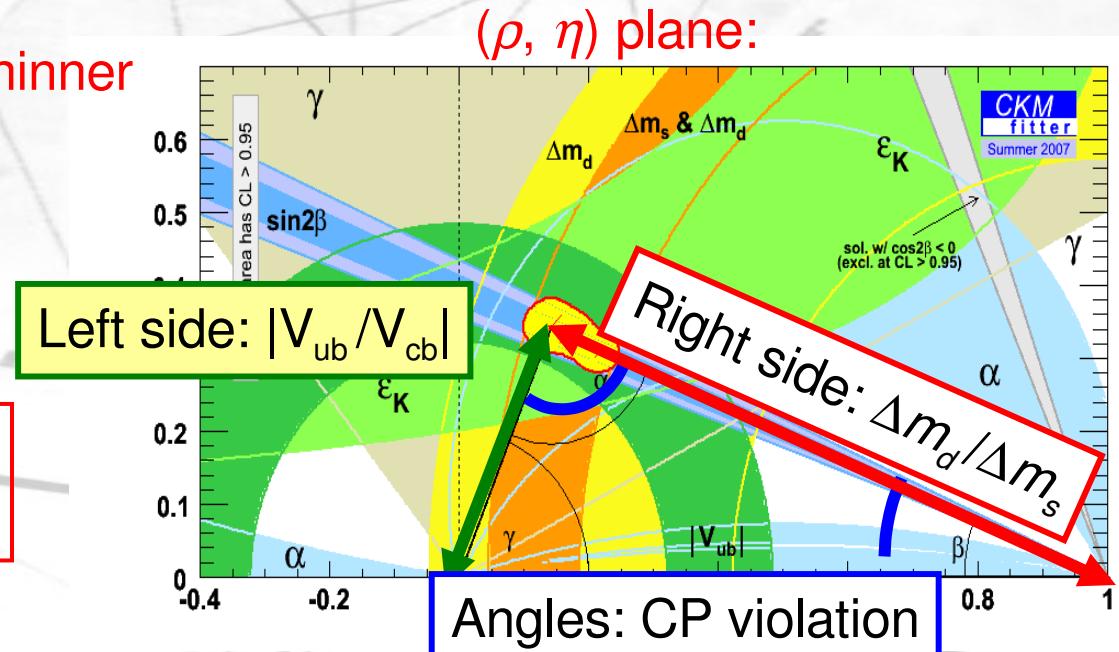
- Angles  $\alpha, \beta, \gamma$  can be measured with ~~CP~~ of  $B$  decays

# $|V_{ub}/V_{cb}|$

- Compare the measurements on the  $(\rho, \eta)$  plane
  - The **yellow oval** tells us this is true as of today: still large enough to hide new physics!
  - **We need the green ring thinner**
- Left side of the Triangle is

$$\left| \frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*} \right| = \left| \frac{V_{ub}}{V_{cb}} \right| \frac{1}{\tan \theta_C}$$

Measurement of  $|V_{ub}/V_{cb}|$  is complementary to  $\sin 2\beta$

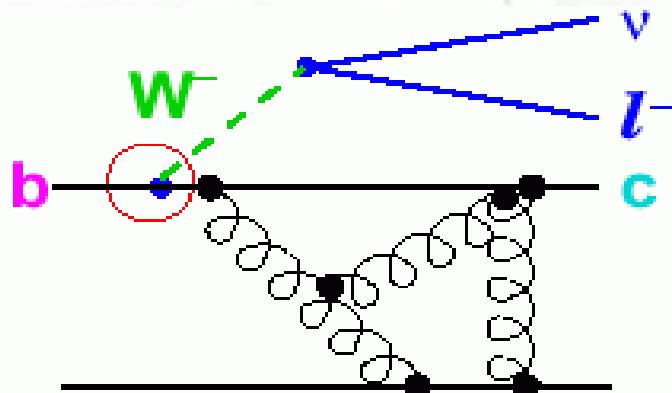


Goal: Accurate determination of both  $|V_{ub}/V_{cb}|$  and  $\sin 2\beta$

$\sin \beta$  (all charmonium) =  $0.680 \pm 0.025$  ~ percentage error: 3.7% (HFAG)

# Semileptonic B Decays

- Natural probe for  $|V_{ub}|$  and  $|V_{cb}|$
- Decay rate  $\Gamma_{c(u)} \equiv \Gamma(b \rightarrow c(u)\ell\nu) \propto |V_{c(u)b}|^2$



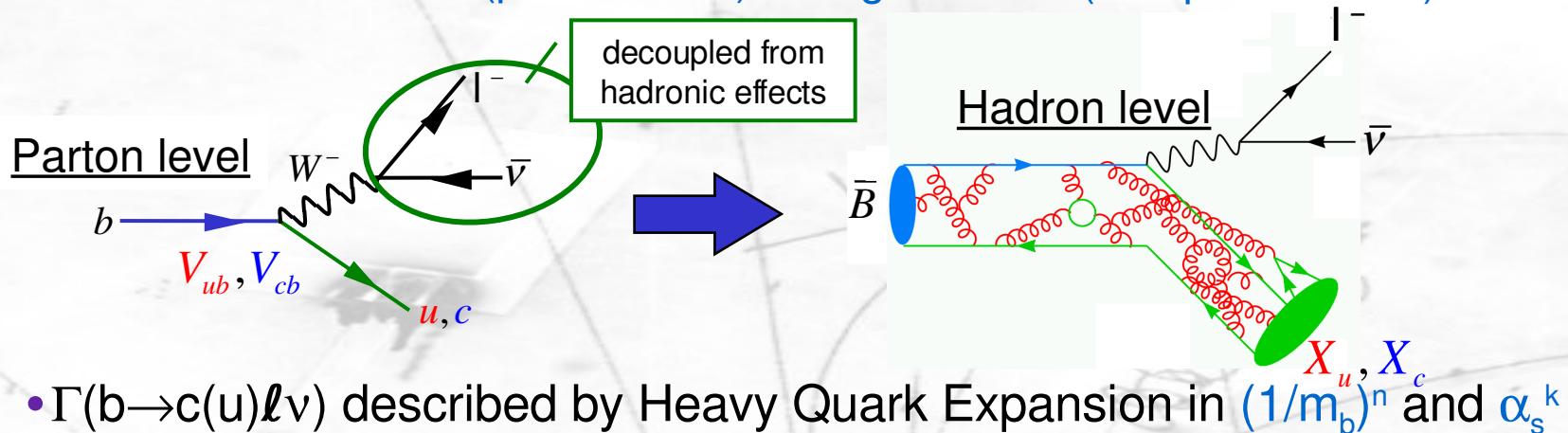
PDG 2006

Decay Mode	Branching Fraction
$B^+ \rightarrow l^+ \nu_l + \text{anything}$	$10.9 \pm 0.4 \%$
$B^+ \rightarrow \bar{D}^*(2007)^0 \ell^+ \nu_\ell$	$(6.5 \pm 0.5) \%$
$B^+ \rightarrow \bar{D}^0 \ell^+ \nu_\ell$	$(2.15 \pm 0.22) \%$
$B^+ \rightarrow \bar{D}_1(2420)^0 \ell^+ \nu_\ell$	$(0.56 \pm 0.16) \%$
$B^+ \rightarrow \bar{D}_2(2460)^0 \ell^+ \nu_\ell$	$< 0.8\% @90\text{CL}$
$B^+ \rightarrow D^- \pi^+ \ell^+ \nu_\ell$	$(0.53 \pm 0.10) \%$
$B^+ \rightarrow D^{*+} \pi^+ \ell^+ \nu_\ell$	$(0.64 \pm 0.15) \%$
$B^+ \rightarrow \bar{D}^{(*)} n \pi \ell^+ \nu_\ell$	??

- $\Gamma_c$  larger than  $\Gamma_u$  by a factor  $\sim 50$ 
  - Extracting  $b \rightarrow u\ell\nu$  signal challenging
- Sensitive to hadronic effects
  - Must understand them to extract  $|V_{ub}|$ ,  $|V_{cb}|$

# Total $b \rightarrow c(u) \ell v$ Rate

Tree level, short distance (perturbative) + long distance (non perturbative):



$$\Gamma(B \rightarrow X_{c(u)} \ell v) = G_F^2 m_b^5 / 192\pi^3 |V_{c(u)b}|^2 [1 + A_{ew}] A_{pert} A_{nonpert}$$

free quark decay
perturbative corrections ( $\alpha_s^k$  dependent)
Non-perturbative power corrections (( $1/m_b$ ) $^n$  dependent)

- Non-perturbative parameters need to be measured.
- They depend on the expansion, which depends on the  $m_b$  definition
- Similar expression for  $b \rightarrow s \gamma$ .

# Moments in $B \rightarrow X_{c(u)} \ell \nu$ decays

Moments evaluated on the full lepton/mass spectrum or part of it:  $p_\ell > p_{\min}$  in the B rest frame

Lepton moments:

$$\langle E_l^n \rangle = \frac{1}{\Gamma_{c(u)}} \int (E_l - \langle E_l \rangle)^n \frac{d\Gamma_{c(u)}}{dE_l} dE_l$$

Hadronic mass moments:

$$\langle m_X^n \rangle = \frac{1}{\Gamma_{c(u)}} \int m_X^n \frac{d\Gamma_{c(u)}}{dm_X} dm_X$$

Moments are related to **non-perturbative parameters**

For comparison with data, use low-order moments of inclusive distributions over large ranges on phase space to avoid problem with quark-hadron duality

Similarly, moments in the photon energy are calculated for  $b \rightarrow s\gamma$

Calculations available in “kinetic” (Benson, Bigi, Gambino, Mannel, Uraltsev, Nucl. Phys. B665:367) and “1S” (Bauer, Ligeti, Luke, Manohar, Trott, Phys. Rev. D70:094017,2004) mass schemes

> 60 measured moments available from DELPHI, CLEO, BABAR, Belle, CDF

# Exclusive Measurements

- Matrix element for semileptonic decays:

$$\mathcal{M}(M_{Q\bar{q}} \rightarrow X_{q'\bar{q}} \ell^- \bar{\nu}_\ell) = -i \frac{G_F}{\sqrt{2}} V_{q'Q} L^\mu H_\mu$$

- Leptonic current exactly known:

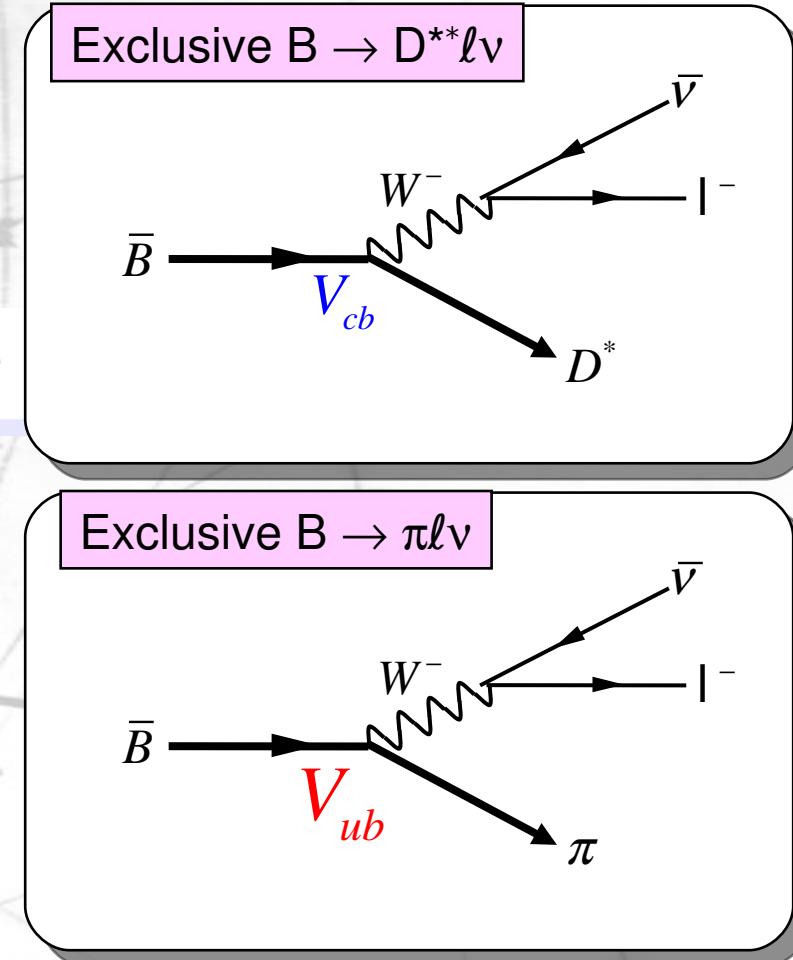
$$L^\mu = \bar{u}_\ell \gamma^\mu (1 - \gamma_5) v_\nu$$

- Hadronic current described by Form Factors (FF), functions of squared momentum transfer  $q^2$ :

$$\langle P'(p') | V^\mu | P(p) \rangle = f_+(q^2) (p + p')^\mu + f_-(q^2) (p - p')^\mu$$

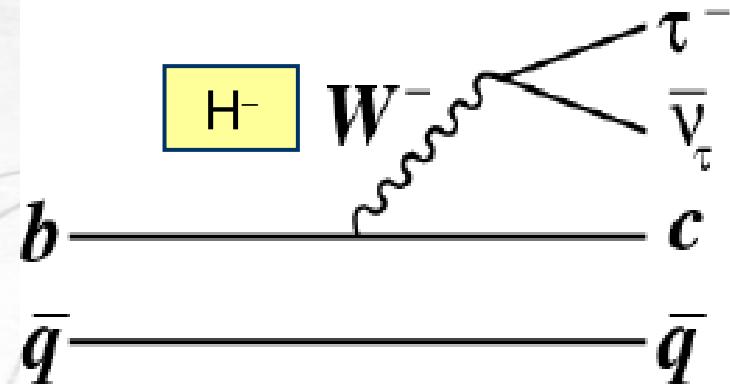
- Exclusive rates determined by  $|V_{c(u)b}|$  and **Form Factors (FF)**, which represent the probability that the heavy-quark combine to form the selected final state particle.

- Theoretically calculable at **kinematical limits**
  - Lattice QCD works if  $D^*$  or  $\pi$  is  $\sim$  at rest relative to  $B$
  - Empirical extrapolation** is necessary to extract  $|V_{c(u)b}|$  from measurements
- Measure differential rates to constrain the FF shape, then use FF normalization from the theory for  $|V_{c(u)b}|$



# New Physics, $B \rightarrow D^{(*)} \tau \bar{\nu}_\tau$

- Same Feynman diagram as the light leptons ( $e, \mu$ ), but the decays can also be mediated by a charged Higgs boson.
- Very clean probe of New Physics:
  - NP contributes at tree level
  - Measurements of FF's for light leptons allow for very precise prediction of the  $\tau$ -hadronic behaviour
  - Spin zero Higgs does not couple to all the helicity states, affect  $D$  and  $D^*$  differently,  $\tau$  polarization.



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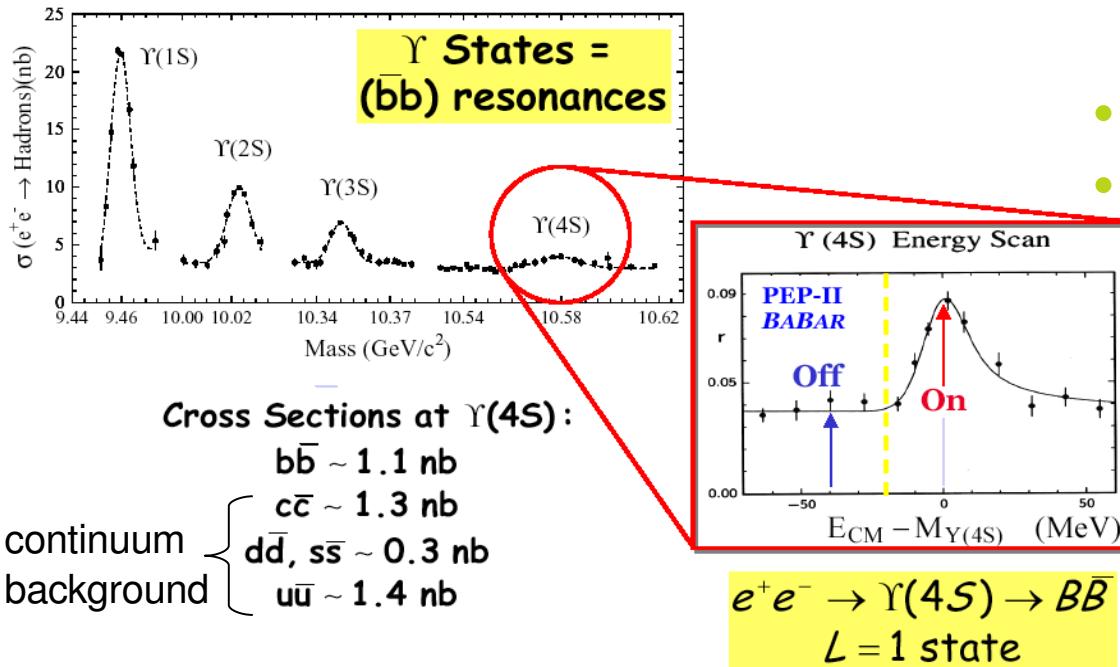
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# PEPII at SLAC and BaBar



- B-factories: run @  $\gamma(4S)$
- BaBar (BELLE) asymmetric factory: 9 GeV  $e^-$  on 3.1 GeV  $e^+$ ,  $\gamma(4S)$  boost:  $\beta\gamma \sim 0.56$

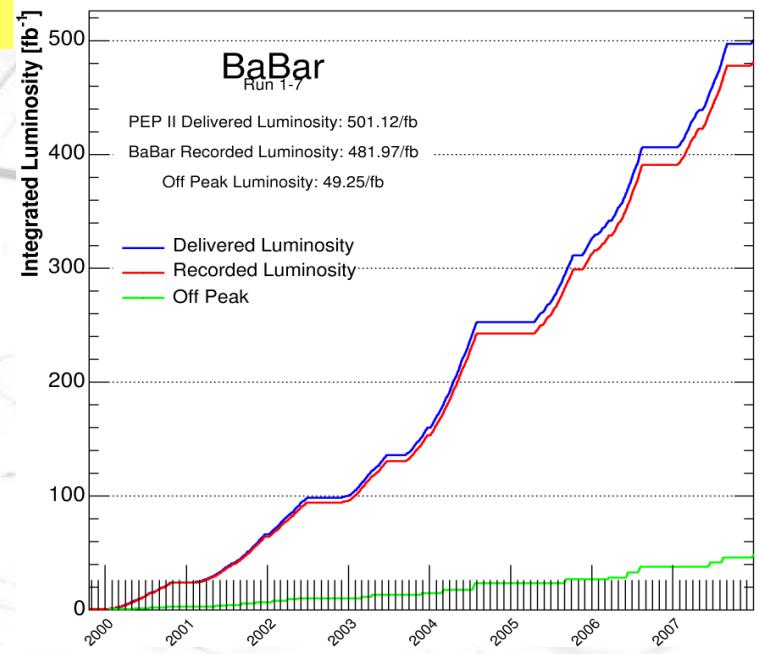
Peak luminosity:  
 $1.2 \times 10^{34} \text{ cm}^2 \text{s}^{-1}$

Integrated luminosity:  
 $482 \text{ fb}^{-1}$  (Jan 1, 2008)

Analyses presented here:  $79-382 \text{ fb}^{-1}$

10 January 2008

F. Di Lodovico, QMUL

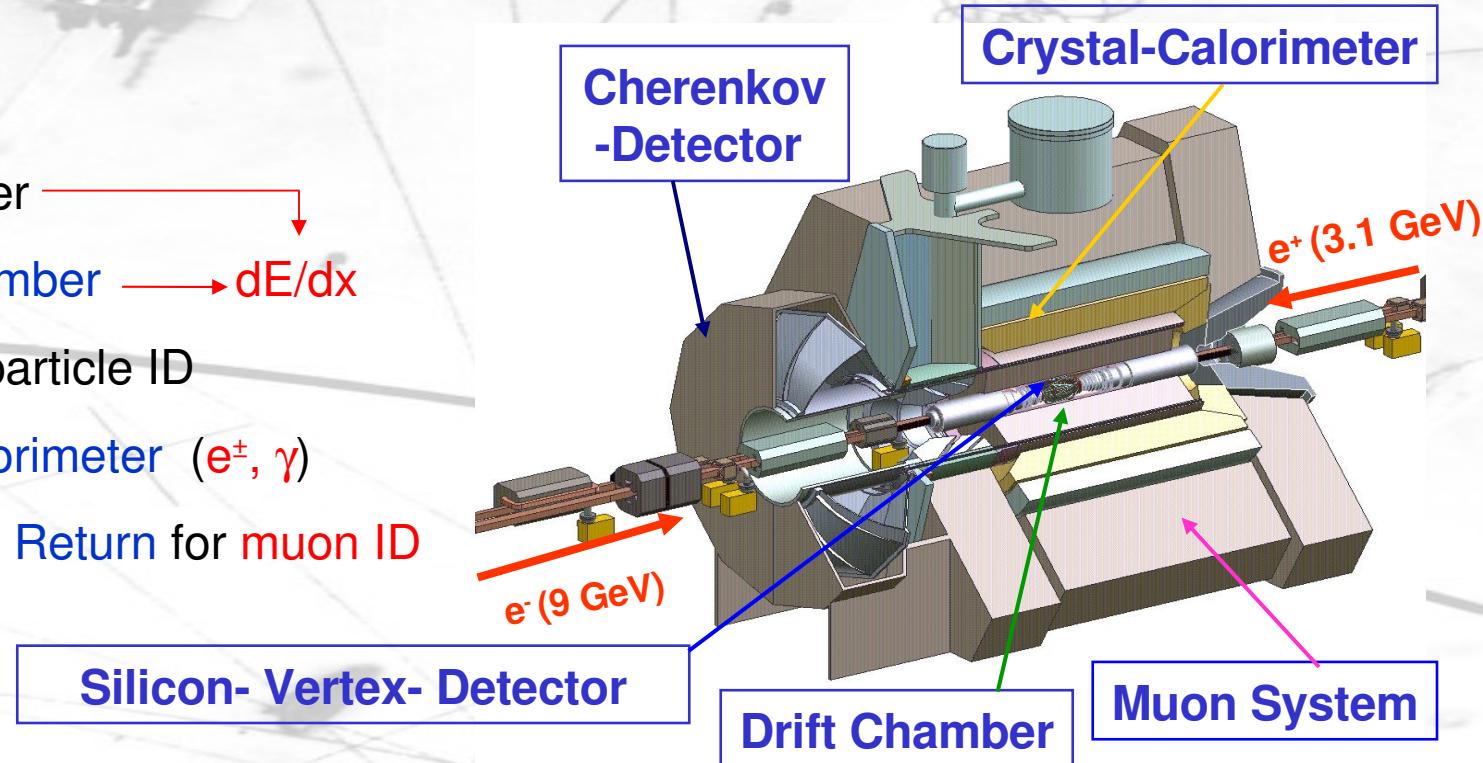


# The BaBar Detector

$B \rightarrow X_{c,u} l \bar{\nu}$   
 $\rightarrow \pi^\pm's, K^\pm's, \gamma's$   
 $l = e, \mu, \tau$

- Good  $e, \mu$  ID ( $p^*_\ell > 1\text{GeV}$ )
- Good hadron ID (e.g.  $\pi/K$  separation)
- Angular coverage  $\approx 91\%$  of  $4\pi$  in CMS  
(challenge for  $\nu$  reconstruction)

- 5-layer SVT tracker
- 40-layer Drift Chamber  $\rightarrow dE/dx$
- DIRC (RICH) for particle ID
- CsI(Tl) crystal calorimeter ( $e^\pm, \gamma$ )
- Instrumented Flux Return for muon ID

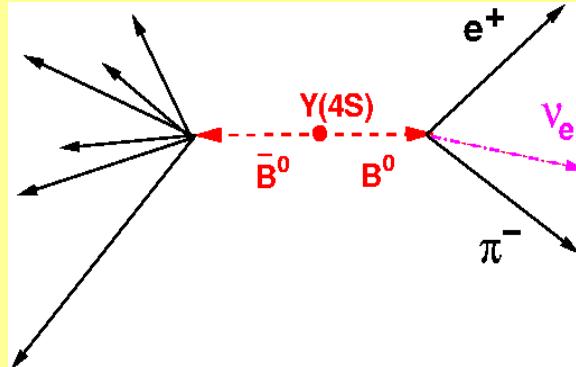
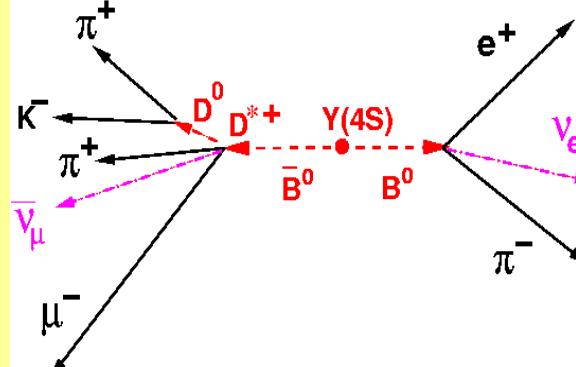
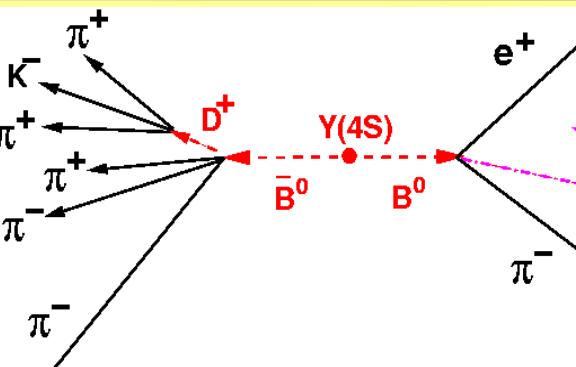


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# Approaches to Measuring $B \rightarrow X\ell\nu$

Signal example:  
 $B \rightarrow \pi \ell \nu$

		(Un)tagged B
<b>Untagged</b> <ul style="list-style-type: none"> <li>Initial 4-momentum known</li> <li>Missing 4-momentum = <math>\nu</math></li> <li>Reconstruct <math>B \rightarrow X\ell\nu</math> using <math>m_B</math> (beam-constrained) and <math>\Delta E = E_B - E_{\text{beam}}</math></li> </ul>	<b>Pros</b> <ul style="list-style-type: none"> <li>High efficiency</li> </ul> <b>Cons</b> <ul style="list-style-type: none"> <li><math>\nu</math> resolution problematic</li> <li>Rel. high backgrounds (relatively low purity)</li> </ul>	
<b>Semileptonic (SL) Tag</b> <ul style="list-style-type: none"> <li>One B reconstructed in a selection of <math>D^{(*)}\ell\nu</math> modes</li> <li>Two missing <math>\nu</math> in event</li> <li>Use kinematic constraints</li> </ul>	<b>Pros</b> <ul style="list-style-type: none"> <li>Lower backgrounds (higher purity)</li> </ul> <b>Cons</b> <ul style="list-style-type: none"> <li>Relatively low efficiency</li> </ul>	
<b>Full Recon Tag (Breco)</b> <ul style="list-style-type: none"> <li>One B reconstructed completely in known <math>b \rightarrow c</math> mode.</li> <li>Many modes used.</li> </ul>	<b>Pros</b> <ul style="list-style-type: none"> <li>Very good <math>\nu</math> resolution</li> <li>Very low backgrounds</li> </ul> <b>Cons</b> <ul style="list-style-type: none"> <li>Very low efficiency</li> </ul>	

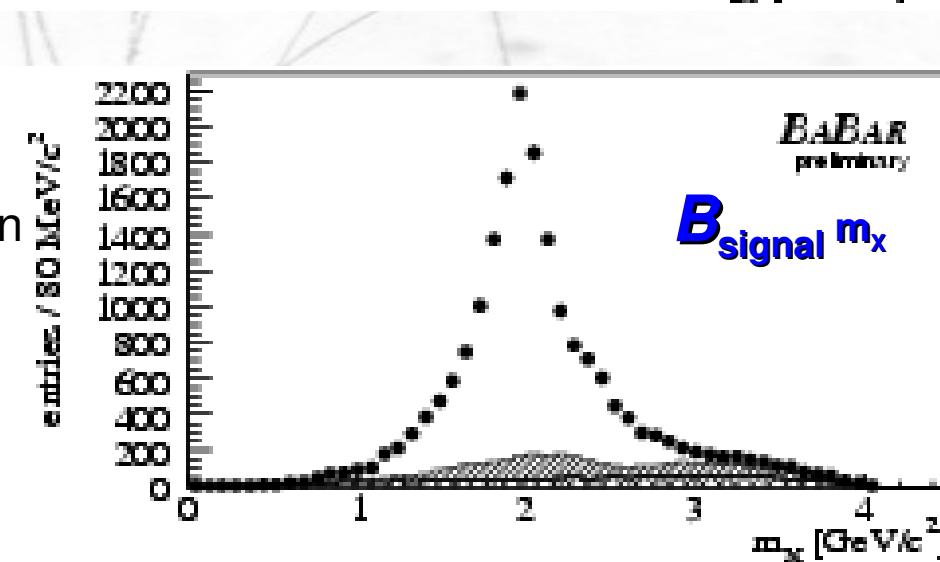
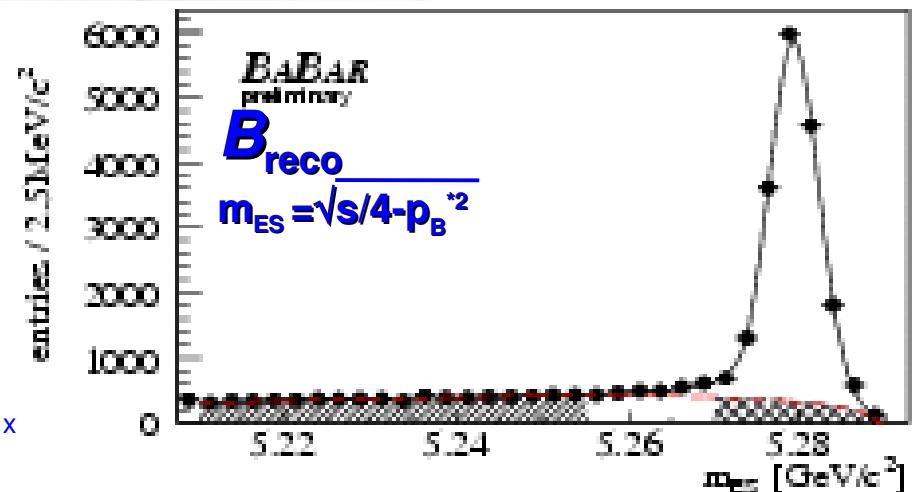
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# Moments in $B \rightarrow X_c \ell \nu$ decays

232M BB

- B-reco. Subtract background with  $m_{ES}$
- 1 lepton ( $e, \mu$ ) in recoil with energy  $P_\ell > 0.8$  GeV in B-rest frame
- Remaining charged and neutral particles form inclusive  $X_c$  system
- Measure moments of hadronic mass  $m_x$  and mixed mass-and-energy moments for several lower cuts on  $P_\ell$
- Improve resolution with kinematic fit
  - energy-momentum conservation
  - $E_{miss}, p_{miss}$  consistent with  $\nu$
- Correct  $X_c$  system for bias due to unmeasured particles
- Dominant systematic uncertainty: efficiency on inclusive event reconstruction

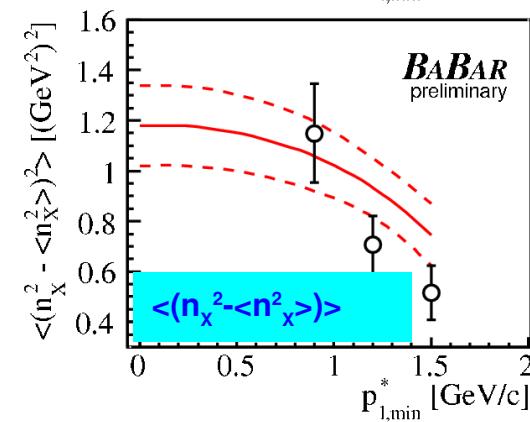
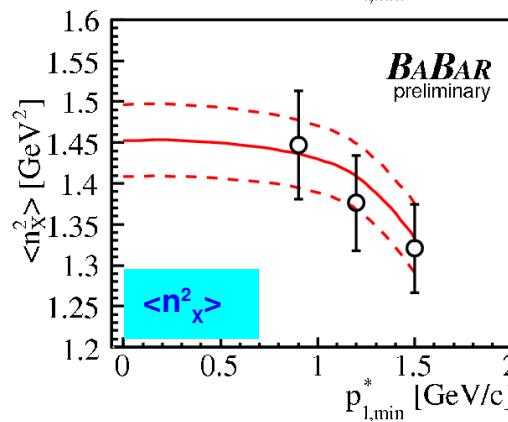
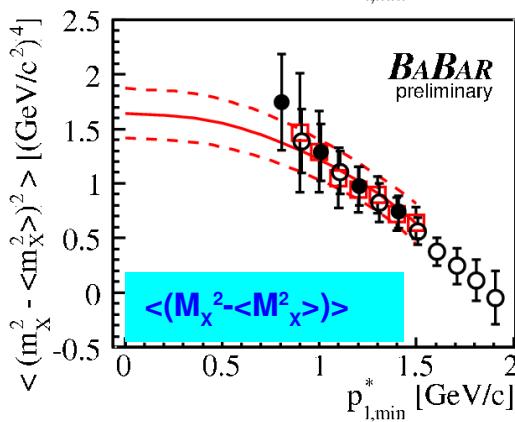
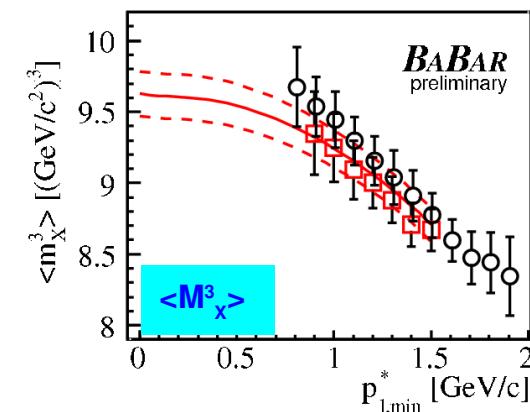
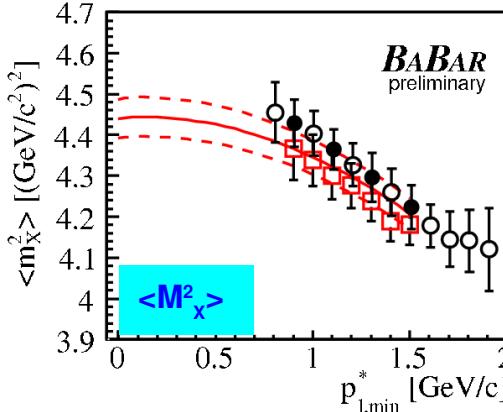
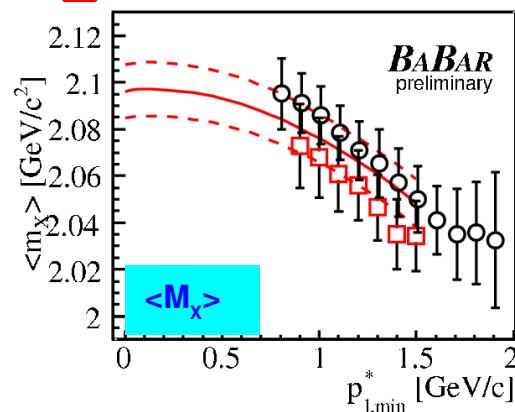


# Measured Moments



This measurement (open symbols not fitted)

BaBar 2004



$$n_x = m_x^2 c^4 - 2\Lambda E_x + \Lambda \quad (\Lambda = 0.65 \text{ GeV})$$

- Moments integrated over data for various lepton cuts over the same mass or lepton energy distribution (**all points highly correlated**)
- Each observable has a different dependence on  $|V_{cb}|$ ,  $m_b$ ,  $m_c$ , and several **non-perturbative params**
- Parameters determined by a **global fit** over ● points
- The ○ points, not used in the fit, agree well with the fit results

# Global OPE Fit – Kinetic Scheme

- 27 input moments:
  - 8 mass moments  
(this analysis)
  - 13  $E_\ell$  moments  
(Phys. Rev. D69 111104 (2004))
  - 6  $E_\gamma$  moments  
(Phys. Rev. D 72, 052004 (2005),  
Phys. Rev. Lett. 97 171803 (2006))

- Further input:  $\tau_B$

- 8 fit parameters:

- $|V_{cb}|, m_b, m_c, \beta_{sl}$
- 4 HQE parameters

- Fit results:  $|V_{cb}| = (41.88 \pm 0.44_{\text{exp}} \pm 0.35_{\text{theo}} \pm 0.59_{\text{TSL}}) 10^{-3}$  (1.9% total error)

$$m_b = (4.55 \pm 0.038_{\text{exp}} \pm 0.040_{\text{theo}}) \text{ GeV} \quad (1.2\% \text{ total error})$$

$$m_c = (1.070 \pm 0.038_{\text{exp}} \pm 0.040_{\text{theo}}) \text{ GeV}$$

$$\beta_{sl} = (10.597 \pm 0.171_{\text{exp}} \pm 0.053_{\text{theo}}) \%$$

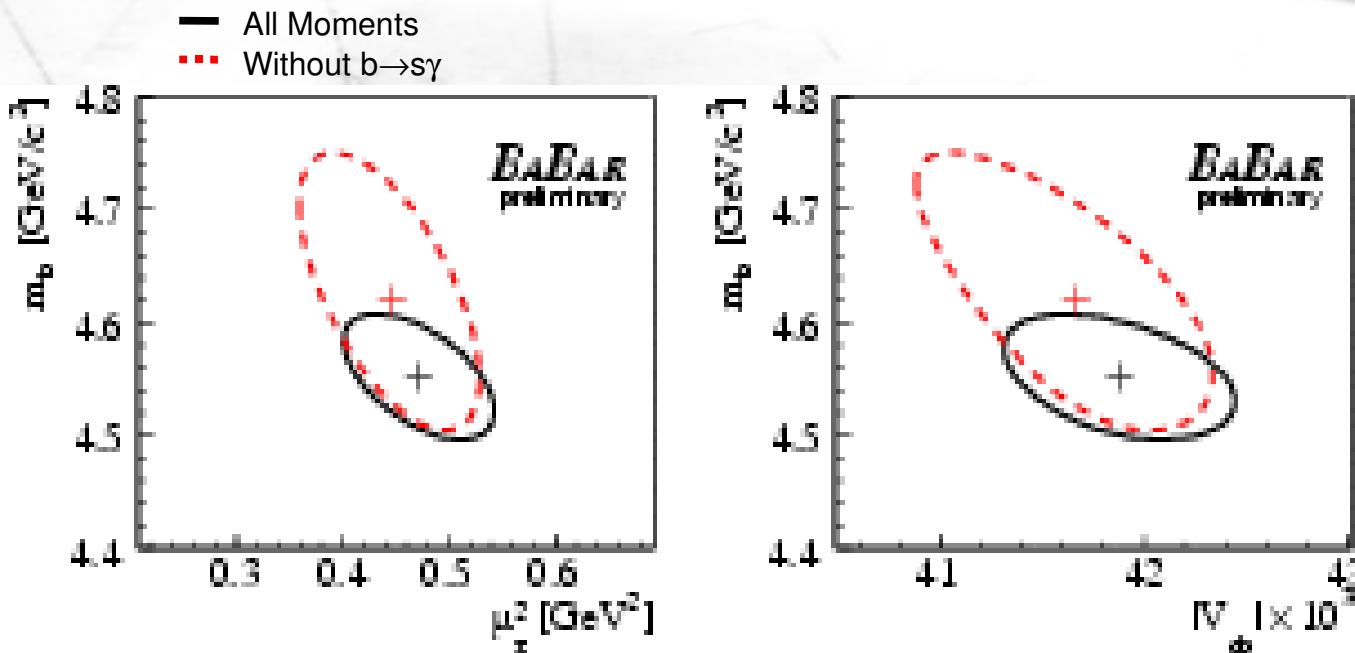
$$m_\pi^2 = (0.471 \pm 0.034_{\text{exp}} \pm 0.062_{\text{theo}}) \text{ GeV}^2$$

$$m_G^2 = (0.330 \pm 0.042_{\text{exp}} \pm 0.043_{\text{theo}}) \text{ GeV}^2$$

$$\rho_D^3 = (0.220 \pm 0.021_{\text{exp}} \pm 0.042_{\text{theo}}) \text{ GeV}^3$$

$$\rho_{LS}^3 = -(0.159 \pm 0.081_{\text{exp}} \pm 0.050_{\text{theo}}) \text{ GeV}^3$$

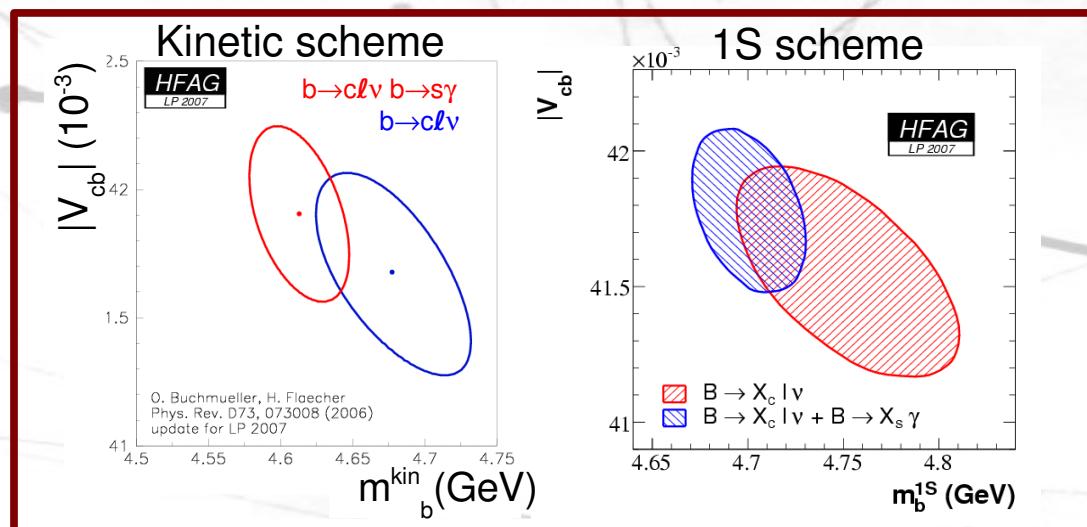
non-perturbative  
params



# OPE Global Fits

- More results from global fits in the kinetic and 1S schemes are available. Recent averages performed by the HFAG
- A pattern is present: results with  $b \rightarrow c\ell\nu$  and  $b \rightarrow s\gamma$  moments differ from results with  $b \rightarrow c\ell\nu$  moments only (except in hep-ex/0611047, but larger errors).
- HFAG results for Lepton Photon:

	$m_b$ (GeV)	$m_b$ (GeV)
	$b \rightarrow c\ell\nu$	$b \rightarrow c\ell\nu$
Kinetic scheme	$4.613 \pm 0.035$	$4.677 \pm 0.053$
1S scheme	$4.701 \pm 0.030$	$4.751 \pm 0.058$



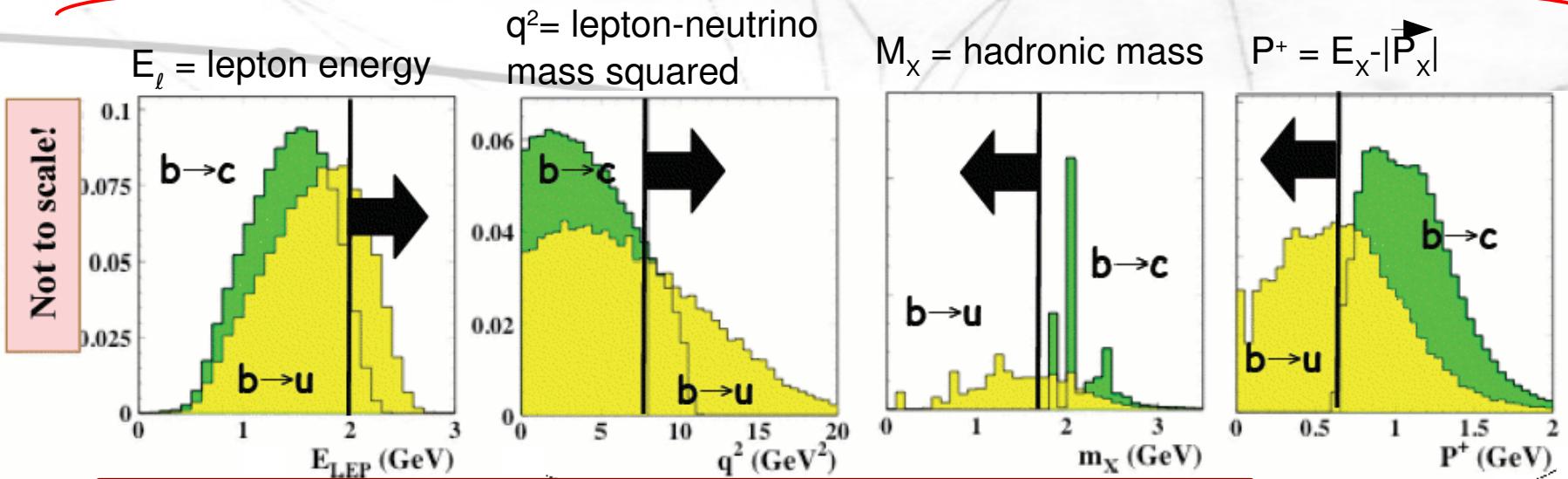
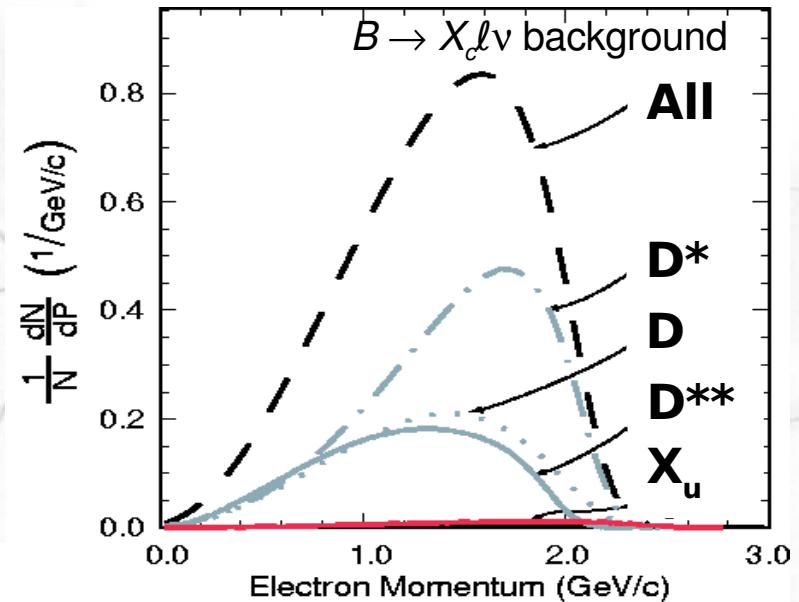
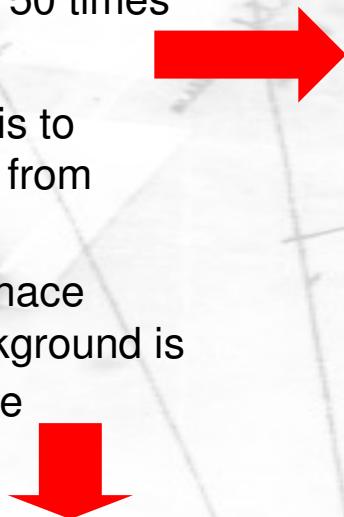
- Large uncertainties due to the ansatz and missing terms
- Different values of  $m_b$  impact the determination of  $|V_{ub}|$  from inclusive decays

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# $B \rightarrow X_u \ell \nu$ rate

- $B \rightarrow X_c \ell \nu$  background is about 50 times larger than  $B \rightarrow X_u \ell \nu$
- Major experimental challenge is to separate  $B \rightarrow X_c \ell \nu$  background from signal
- This is achieved in region of phase space where the  $B \rightarrow X_c \ell \nu$  background is suppressed → partial decay rate

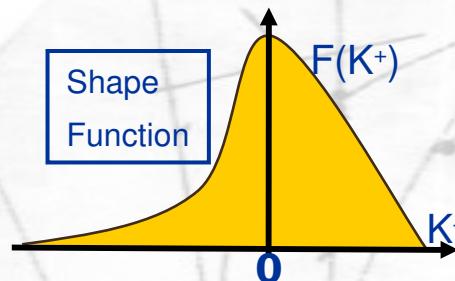


Restriction of the phase-space is a challenge to theory!

# $B \rightarrow X_u \ell \nu$ theory: OPE approach

Restrict kinematics to suppress background from  $B \rightarrow X_c \ell \nu$ : **OPE convergence is compromised!** Need light-cone distribution (shape) function of b quark:

Detailed shape not constrained,  
in particular the low tail.  
Needs to be determined by data



Mean and r.m.s. are known  
from the moments!

Four approaches:

- 3-scale OPE based on HQET, SCET: Bosch, Lange, Neubert, Paz (**BLNP**) [**PRD 72:073006 (2005)**]
- Relate  $b \rightarrow u \ell \nu$  directly to  $b \rightarrow s \gamma$ : Lange, Neubert, Paz (**LNP**) [**JHEP 0510:084, 2005**], Leibovich, Low, Rothstein (**LLR**) [**PLB 486:86**]
- Select phase space in  $m_x$ - $q^2$  with reduced SF dependence: Bauer, Ligeti, Luke (**BLL**) [**PRD 64:113004 (2001)**]
- Kinetic scheme: P.Gambino, P.Giordano, G.Ossola, N.Uraltsev (**GGOU**) [**JHEP10(2007)058**] (very recent!)

# $B \rightarrow X_u \ell \nu$ theory: parton-level approach

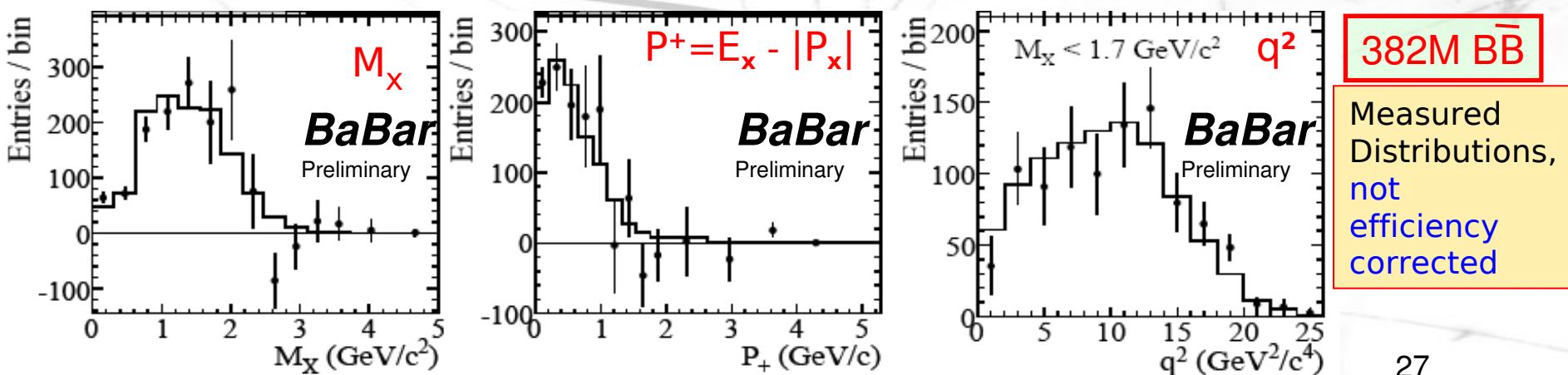
- On-shell calculation framework
- Use perturbation QCD, with inclusive hadron final states coming from gluon radiation, as  $m_b \gg \Lambda$  (hadronic scale)
- The perturbative expansion of spectra in the threshold region is affected by large logarithms, to be resummed
- No Shape Function is introduced, but a modelling of non-perturbative QCD effects is adopted.
- Two approaches:
  - Dressed Gluon Exponentiation: J.R. Andersen and E. Gardi (DGE) [JHEP 0601:097 (2006)]
  - Analytic Coupling: U. Aglietti, G. Ferrera, G. Ricciardi (AC) [Phys.Rev. D74 (2006) 034006, Phys.Rev. D74 (2006) 034005, Phys.Rev. D74 (2006) 034004]

# $B \rightarrow X_u \ell \nu$ : fully tagged B

arXiv:0708.3702 [hep-ex]  
submitted to PRL

- Fully reconstructed B
- Events identified fitting the  $m_{ES}$  distribution
- Normalize to semileptonic events to be independent of tagging efficiency
- Use 3 kinematic variables to distinguish  $b \rightarrow c \ell \nu$  from  $b \rightarrow u \ell \nu$ :  $M_x$ ,  $P^+$ ,  $M_x - q^2$
- Major systematic errors from: detector,  $m_{ES}$  fits, MC stat.

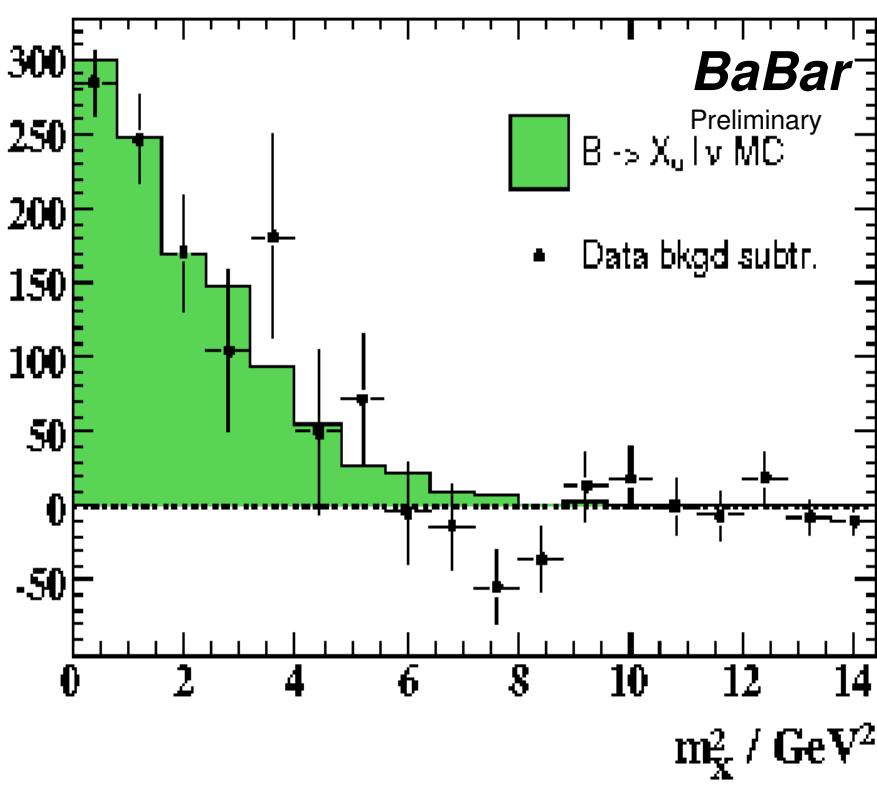
Variables	$X_u \ell \nu$ events	$\Delta\mathcal{B}(10^{-3})$
$M_x$	$803 \pm 60$	$1.18 \pm 0.09_{\text{stat}} \pm 0.07_{\text{syst}} \pm 0.01_{\text{theo}}$
$P^+$	$633 \pm 63$	$0.95 \pm 0.10_{\text{stat}} \pm 0.08_{\text{syst}} \pm 0.01_{\text{theo}}$
$M_x, q^2$	$562 \pm 55$	$0.76 \pm 0.08_{\text{stat}} \pm 0.07_{\text{syst}} \pm 0.02_{\text{theo}}$



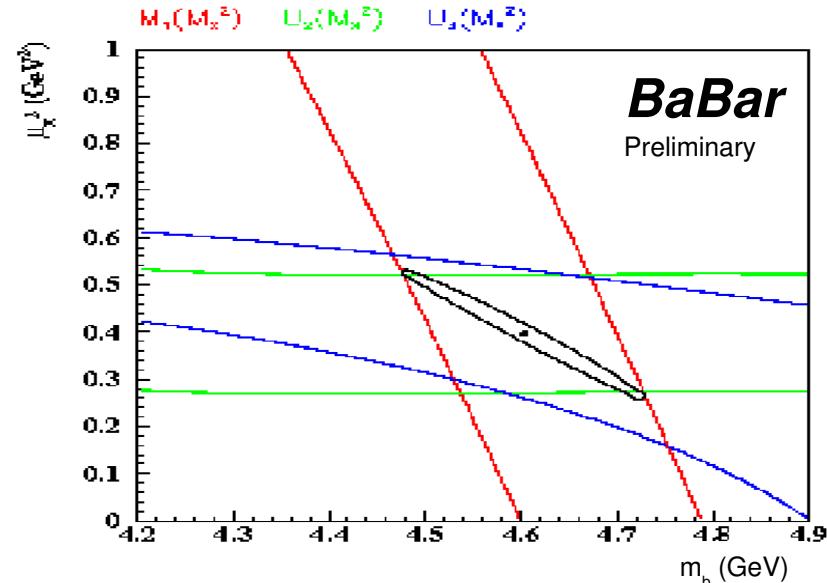
347M  $B\bar{B}$ 

# $B \rightarrow X_u \ell \nu$ $m_X$ moments

- Analysis approach similar to arXiv:0708.3702 [hep-ex]
- Unfold the  $m_X$  spectrum for detector acceptance, efficiency and resolution.
- Extract mass moments with upper cut  $m_X^2 < 6.2 \text{ GeV}^2$



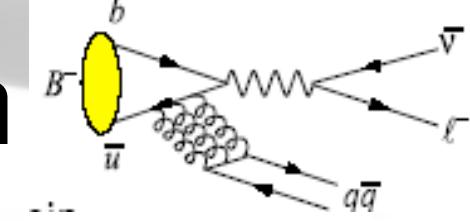
- $M_1 = (1.96 \pm 0.34_{\text{stat}} \pm 0.53_{\text{syst}}) \text{ GeV}^2$
- $U_2 = (1.92 \pm 0.59_{\text{stat}} \pm 0.87_{\text{syst}}) \text{ GeV}^4$
- $U_3 = (1.79 \pm 0.62_{\text{stat}} \pm 0.78_{\text{syst}}) \text{ GeV}^6$



Theory calculations used:  
 Gambino, Ossola, Uraltsev hep-ph/0505091

First measurement of  $m_b$  in  $X_u \ell \nu$  (but large errors):  
 $m_b = 4.604 \pm 0.025_{\text{stat}} \pm 0.193_{\text{mom. syst}} \pm 0.097_{\text{syst}} \text{ GeV}$

# Weak Annihilation

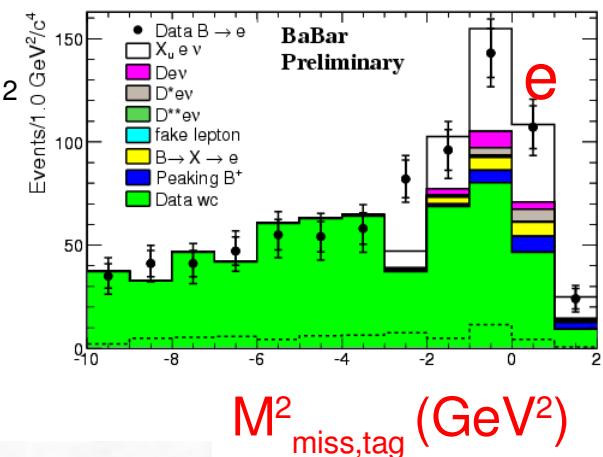


Small contribution to  $B \rightarrow X_u \ell \nu$  decay (<3% of total rate)

- Compare  $B^0 \rightarrow X_u \ell \nu$  partial rate to charge-averaged  $B \rightarrow X_u \ell \nu$  rate in WA-enhanced region (large  $p_\ell$  and large  $q^2$ )

- Tagging:  $B^0 \rightarrow D^{*+} \ell^- \nu X$  with partial  $D^*$  reconstruction
- Neutrino mass derived from kinematics  $m_\nu^2 = (P_B - P_{D^*} - P_\ell)^2$
- Measure  $\mathcal{B}$  for  $P_\ell > 2.2\text{-}2.4 \text{ GeV}$

$\Delta P_\ell$	$\hat{\Delta}\mathcal{B}(B^0) \cdot 10^4$
2.2 – 2.6 GeV/c	$2.62 \pm 0.33 \pm 0.16$
2.3 – 2.6 GeV/c	$1.30 \pm 0.21 \pm 0.07$
2.4 – 2.6 GeV/c	$0.76 \pm 0.15 \pm 0.05$



- Extract charge asymmetry, using info from untagged  $B \rightarrow u \ell \nu$  from endpoint analysis (Phys.Rev.D73:012006,2006)

$$A^{+/0} = \frac{\Delta\Gamma^+ - \Delta\Gamma^0}{\Delta\Gamma^+ + \Delta\Gamma^0}$$

- Limit on contribution from WA for interval  $2.3 < E_l < 2.6 \text{ GeV}$ :

$$\frac{|\Gamma_{WA}|}{\Gamma_u} = \frac{2 \cdot f_u(\Delta P_\ell)}{f_{WA}(\Delta P_\ell)} \cdot A^{+/0} < \frac{3.8 \%}{f_{WA}(2.3 - 2.6)}, \quad \text{at 90\% C.L.}$$

$$\begin{aligned} \Gamma_{WA} &= \Gamma^+ - \Gamma^0 \\ f_{WA}(\Delta P_\ell) &= \text{fraction of WA in interval } \Delta P_\ell \end{aligned}$$

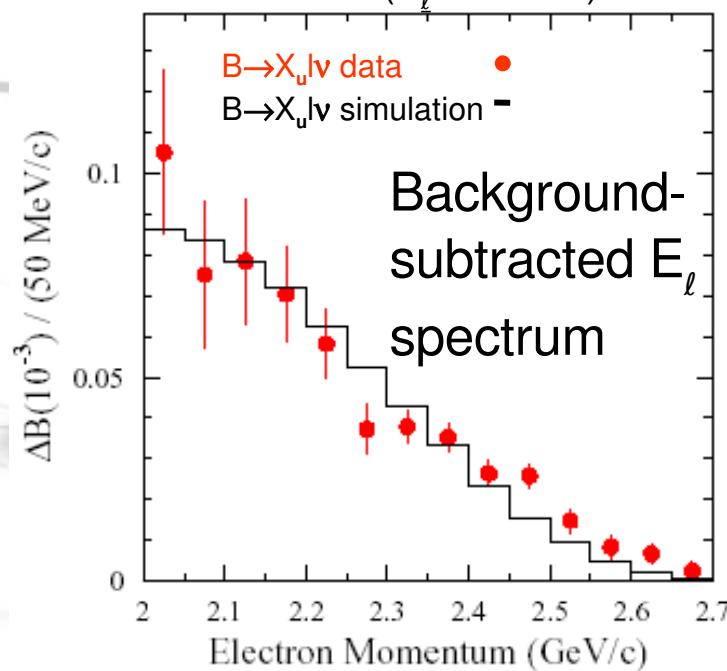
# $B \rightarrow X_u \ell \nu$ $E_\ell$ analyses

- The  $E_\ell$  (endpoint) analysis is the original method to study  $B \rightarrow X_u \ell \nu$
- Two untagged analyses so far
- Identify high energy lepton (electron, plenty of statistics)
- Very high background from  $B \rightarrow X_c \ell \nu$ !
- Accurate subtraction of the background is crucial
- Missing momentum used for determining  $q^2$

Phys.Rev.D73:012006,2006

88M  $B\bar{B}$

■  $S/B \sim 1/15$  ( $E_\ell > 2$  GeV)

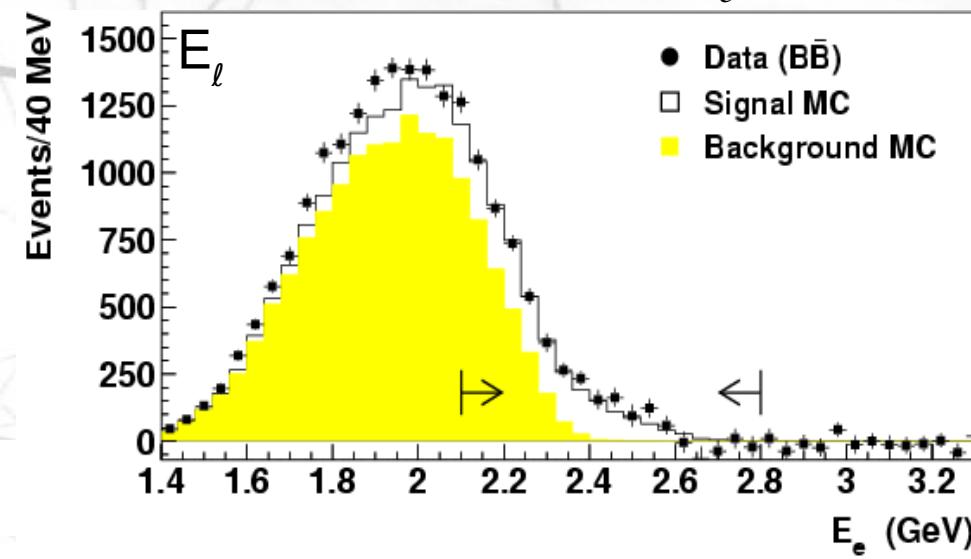


Phys.Rev.Lett.95:111801,2005

88M  $B\bar{B}$

■ Suppress background using:

$$s_h^{\max} = m_B^2 + q^2 - 2m_B(E_e + \frac{q^2}{4E_e})$$

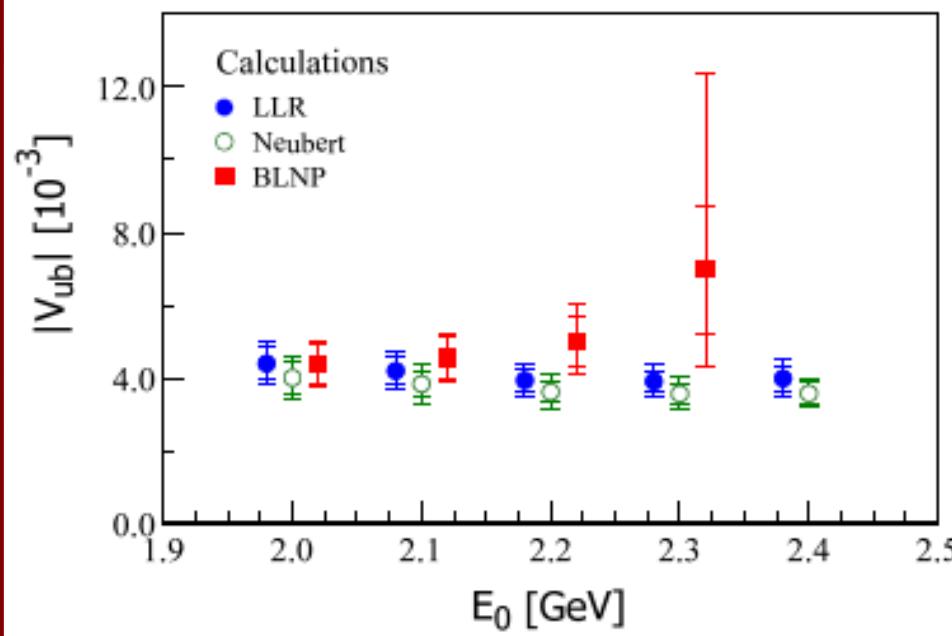


# SF independent analyses

- Assumption that QCD interactions affecting  $b \rightarrow s\gamma$  and  $b \rightarrow u\ell\nu$  are the same
- Take ratio of weighted  $b \rightarrow s\gamma$  and  $b \rightarrow u\ell\nu$  decay rates
- $b \rightarrow s\gamma$  spectrum from Phys. Rev. D72 (2005) 052004
- Two BaBar analyses:

arXiv:hep-ph/0702072v1  
accepted by PRD

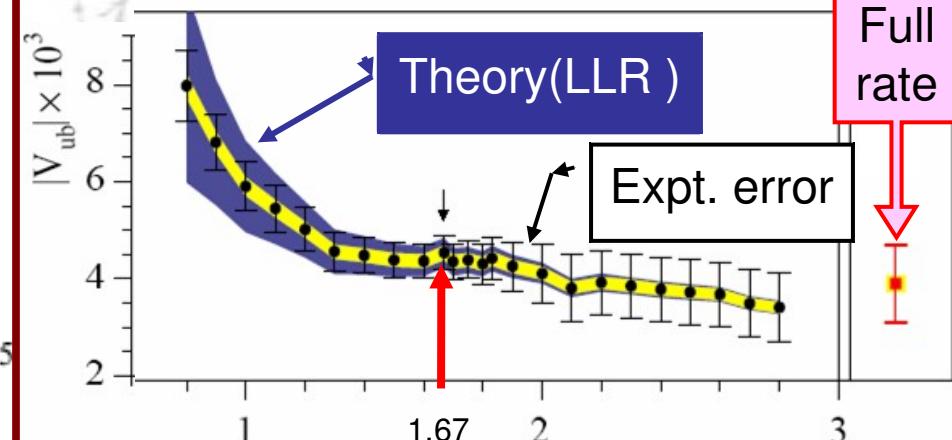
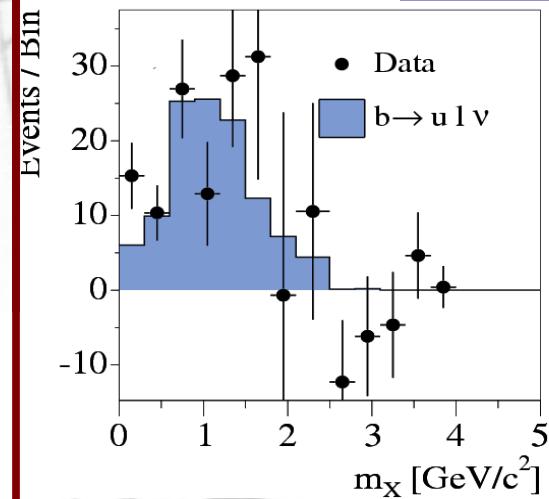
- Using the endpoint spectrum,  $|V_{ub}|$  is calculated as a function of  $E_\ell$
- Consistent results except at high  $E_\ell$



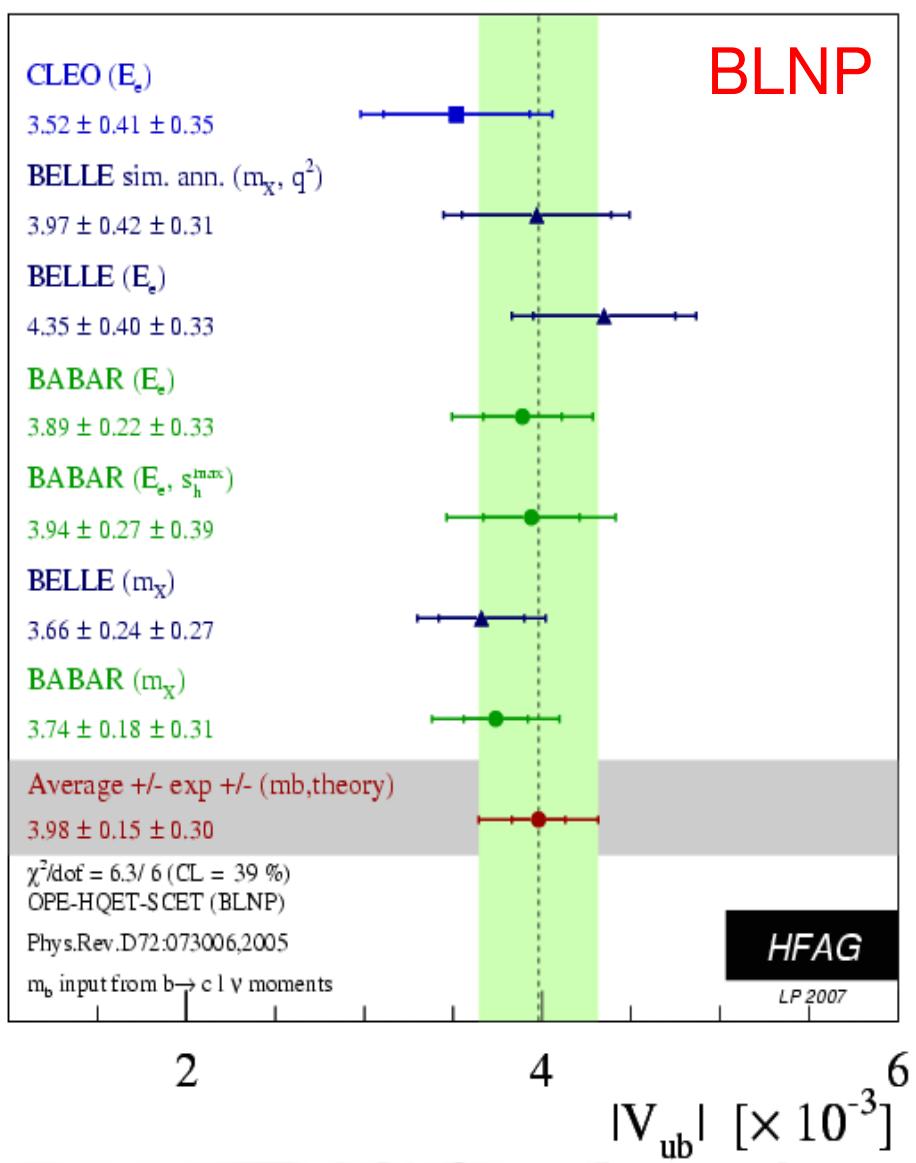
Phys.Rev.Lett. 96 (2006) 221801

88.9M BB

- Select Breco events and measure  $m_x$
- Statistic limited analysis



# $|V_{ub}|$ results



Plethora of theoretical approaches  
→ plethora of  $|V_{ub}|$  values for each analysis

Current approach is either to quote all the values or just BLNP (OPE)

BLNP:  $m_b$  from  $b \rightarrow clv$  moments:

$$|V_{ub}| = (3.98 \pm 0.15 \pm 0.30) 10^{-4}$$

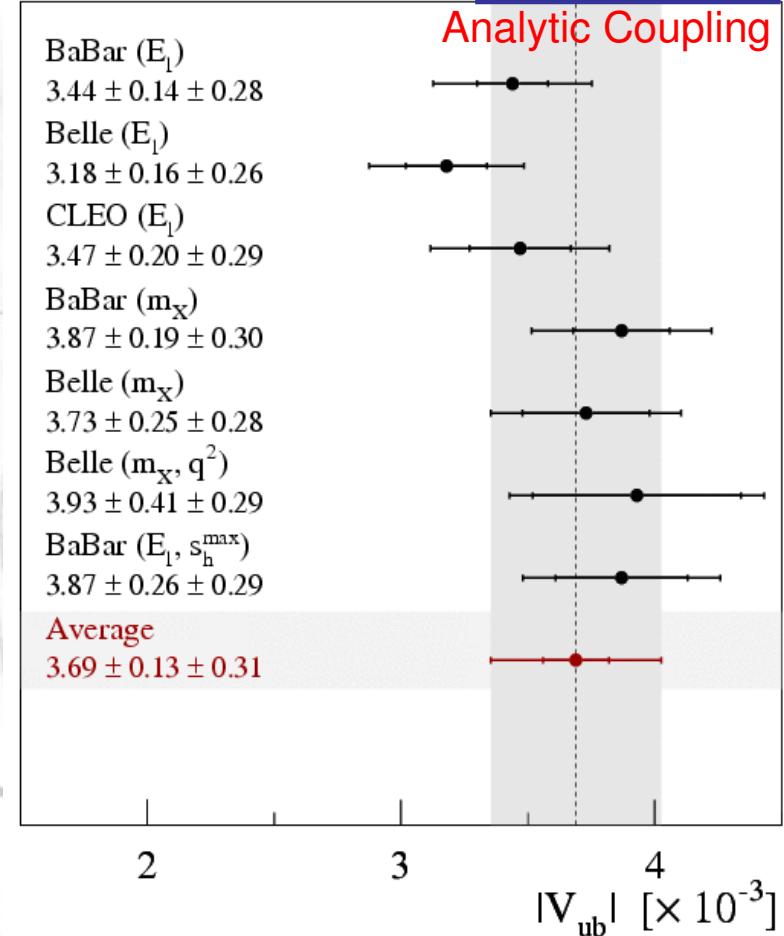
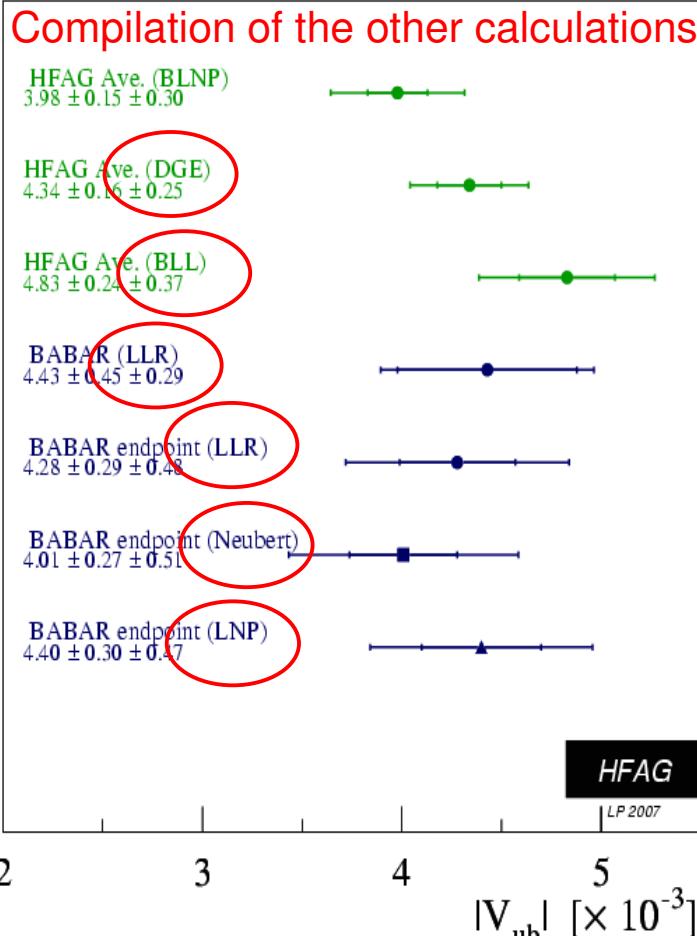
BLNP:  $m_b$  from  $b \rightarrow clv$  and  $b \rightarrow s\gamma$  moments can't be used because of uncontrolled theoretical errors for the  $b \rightarrow s\gamma$  moments.  $|V_{ub}|$  value using  $b \rightarrow clv$  and  $b \rightarrow s\gamma$  was:

$$|V_{ub}| = (4.31 \pm 0.17 \pm 0.35) 10^{-3}$$

Use only the partial  $B$  from  $m_x$  for the Breco analyses as experimental correlation among the variables are not published

# More $|V_{ub}|$ results

arXiv:0711:0860



- Results vary from  $4.83 \times 10^{-3}$  (BLL) to  $3.69 \times 10^{-3}$  (AC)
- b-quark masses approaches and dependences different.
- Aim for the near future: to quote one value of  $|V_{ub}|$
- $|V_{ub}|$  average using the Kinetic scheme (P.Gambino, P.Giordano, G.Ossola, N.Uraltsev, [JHEP10(2007)058]) is being computed.

# Outline

- Introduction
  - ▶ Motivations
  - ▶ BaBar
  - ▶ Experimental approach
- Inclusive decays
  - ▶ Determination of  $|V_{cb}|$
  - ▶ Determination of  $|V_{ub}|$
- Exclusive Decays
  - ▶  $D^{(*)}(\ell\nu)$
  - ▶  $\pi(\eta)(\ell\nu)$
- Conclusions

# $|V_{cb}|$ and Form Factors from $B \rightarrow D^* \ell \nu$

- Differential decay rate :

$$\frac{d\Gamma(B^0 \rightarrow D^* - \ell^+ \nu_\ell)}{dw d\cos\theta_\ell d\cos\theta_V d\chi} = \frac{G_F^2 |V_{cb}|^2}{48\pi^3} \boxed{F(w, \theta_\ell, \theta_V, \chi) G(w)}$$

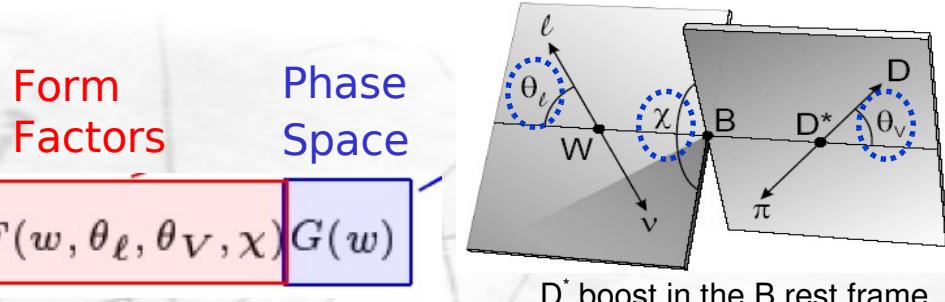
- HQ symmetry (b and c mass infinite) predicts a unique universal FF, normalized to 1.0 at zero recoil.
- QCD (and QED) correction to F(1) needed!
- $F(w, \theta_\ell, \theta_V, \chi)$  incorporates 3 non-trivial form factors,  $A_1(w), A_2(w), V(w)$
- HQET relates the 3 FF's to each other through HQS, but leaves 3 free parameters to be determined experimentally. They are:

Amplitude ratios:  $R_1(w) = V/A_1$

$$R_2(w) = A_2/A_1$$

Curvature  $\rho^2 = -dF/dw|_{w=1}$

- Using a parametrization by CLN (Caprini, Lellouch, Neubert, NPB530, (1998) 153): three parameters need to be extracted from data  $R_1(1), R_2(1)$  and  $\rho^2$ .
- Goal is to determine  $R_1(w), R_2(w), \rho^2$
- There are 4 observables:  $w$  and 3 angles ( $\theta_\ell, \chi, \theta_V$ )



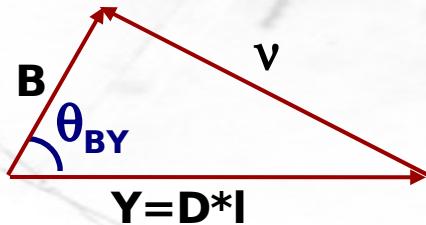
$D^*$  boost in the B rest frame

$$w \equiv \frac{M_B^2 + M_{D^*}^2 - q^2}{2M_B M_{D^*}}$$

# $B^0 \rightarrow D^{*+} \ell \nu$ Selection

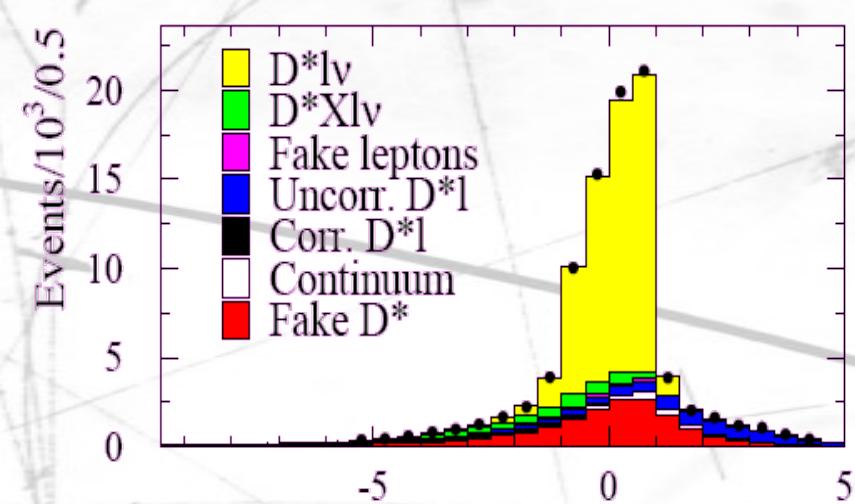
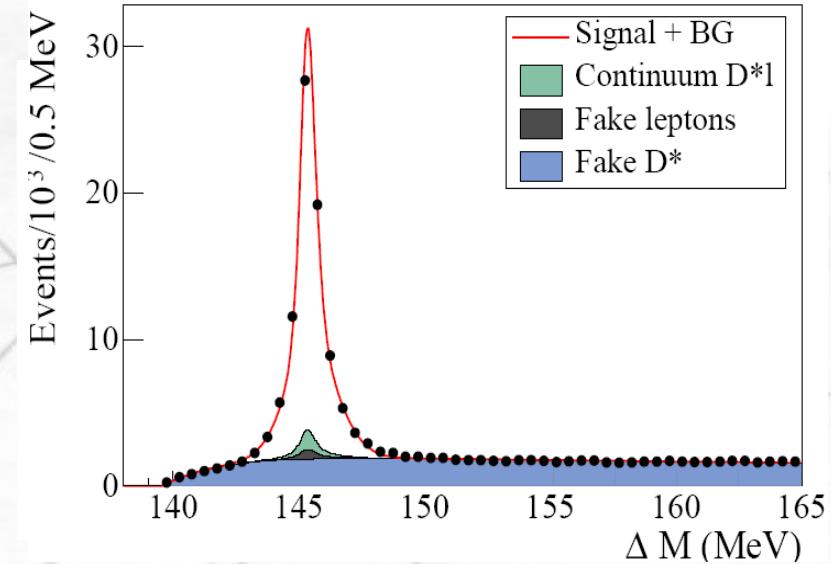
Select  $B^0 \rightarrow D^{*+} \ell \nu$  ( $D^{*+} \rightarrow D^0 \pi^+$ ) events with  $p_{\ell}^* > 1.2$  GeV

Estimate backgrounds (comb.,  $D^{**}$ ) from  $\Delta M = M(D^*) - M(D)$  and  $\cos \theta_{BY}$



Two BABAR analyses:

- (1) **Three D modes:**  $D^0 \rightarrow K\pi$ ,  $K\pi\pi^0$ ,  $K\pi\pi\pi^0$   
 $\chi^2$  fit to 1D projections
- (2) **One D mode:**  $D^0 \rightarrow K\pi$ ,  
 4D maximum Likelihood fit

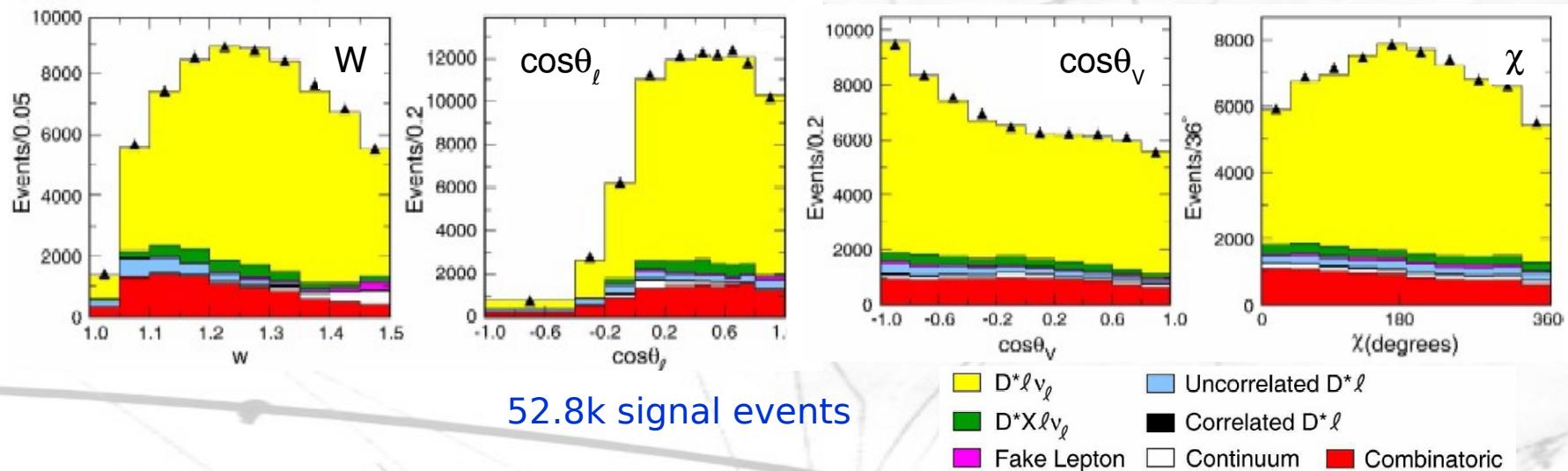


$$\cos \theta_{BY} = -\frac{M_B^2 + M_Y^2 - 2E_B E_Y}{2p_B p_Y}$$

# $B \rightarrow D^*$ Form Factors: 1D Projections

- Simultaneous  $\chi^2$  fit of 1D projections in three variables  $w$ ,  $\cos\theta_l$ ,  $\cos\theta_V$  (integrated over angle  $\chi$ )
- First simultaneous measurement of form factors and  $|V_{cb}|$ , fully accounting for all correlations

79M BB



- Final results combined with Phys.Rev. D74 (2006) 092004 (which uses a full 4D fit) to give a combined value of the form factors:

$$\rho^2 = 1.179 \pm 0.048 \pm 0.028$$

$$R_1(1) = 1.417 \pm 0.061 \pm 0.044$$

$$R_2(1) = 0.836 \pm 0.037 \pm 0.022$$

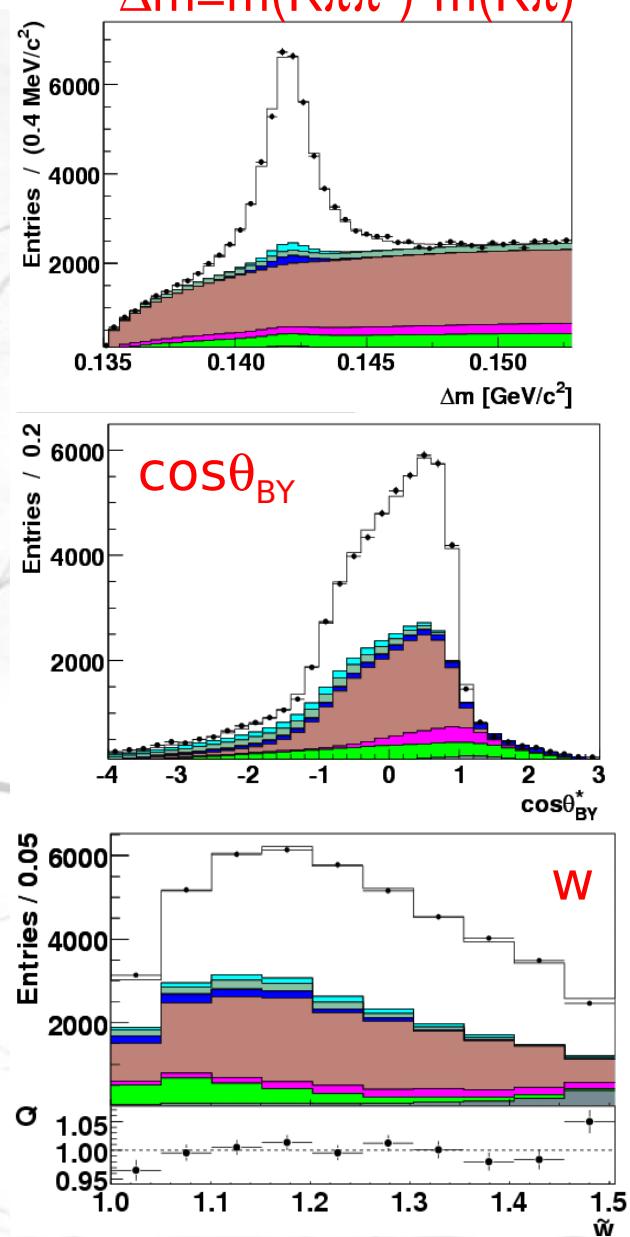
$$F(1)|V_{cb}| = (34.7 \pm 0.3 \pm 1.1) 10^{-3}$$

New BaBar FF are  $\sim 5$  times better than the old ones from CLEO (with  $\sim 3 \text{ fb}^{-1}$ )

*Syst. Uncertainties dominated by detector efficiencies,  $Bg$ ,  $R_1$ ,  $R_2$*

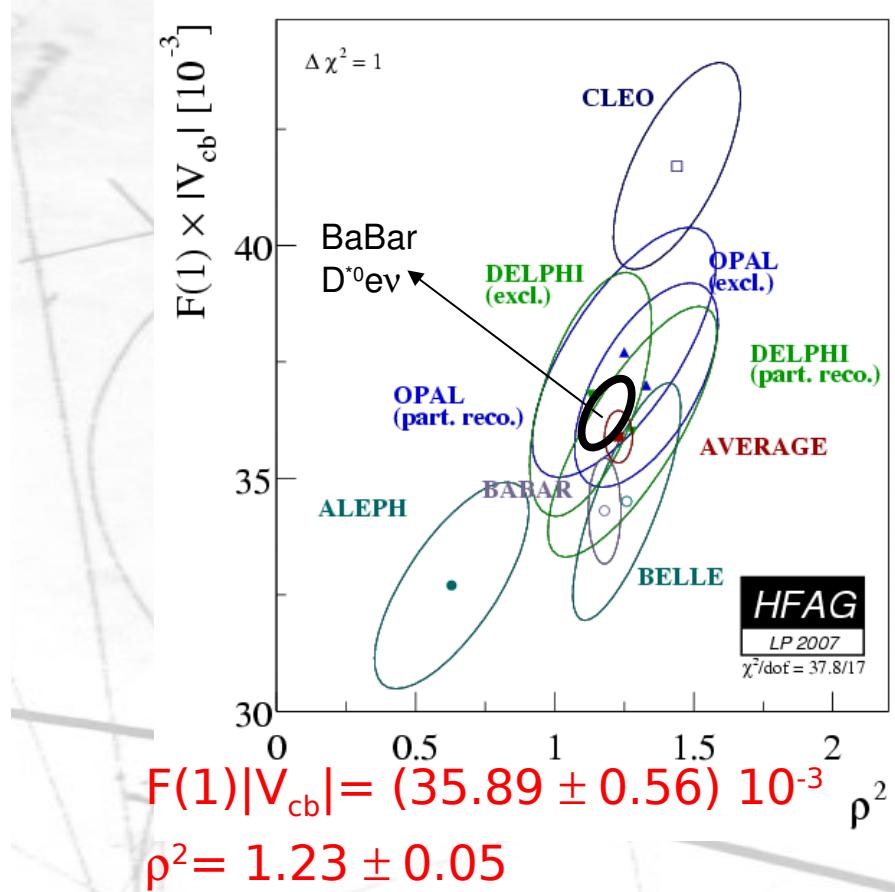
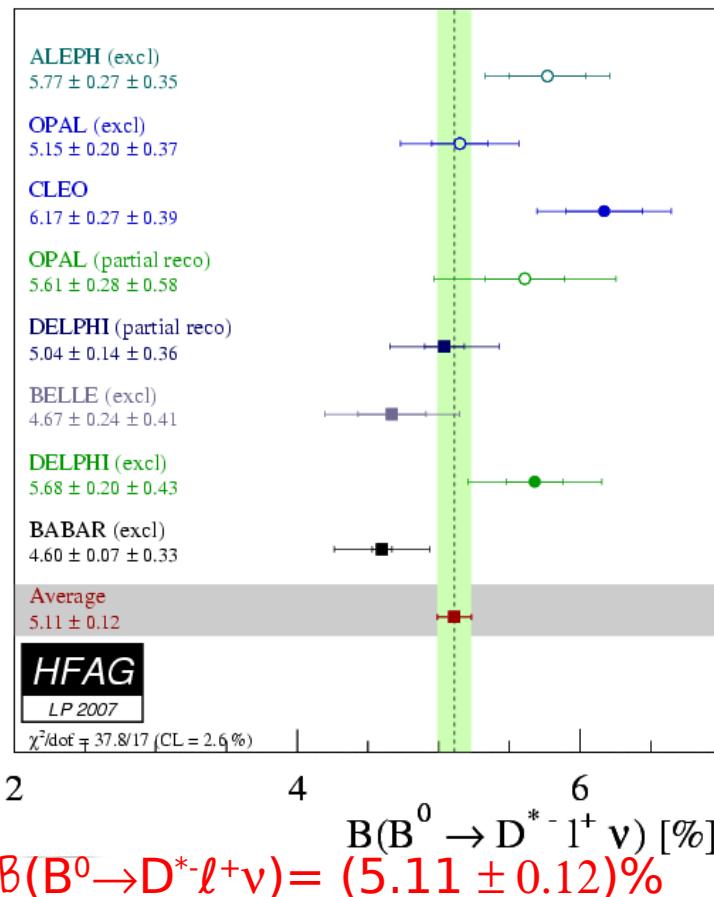
# $|V_{CB}|$ and Form Factors from $B^- \rightarrow D^{*0} e^- \bar{\nu}$

- Look at decay chain:  $D^{*0} \rightarrow \pi^0 D^0$  and  $D^0 \rightarrow K^- \pi^+$
  - Discriminating variables:  $\Delta m$ ,  $\cos\theta_{BY}$
  - Binned maximum likelihood fit in  $\Delta m$ ,  $\cos\theta_{BY}$  and  $\omega$
  - $23500 \pm 330$  signal events from the fit
  - Main background: mis-reconstructed  $B^{0\pm} \rightarrow D^{*0\pm} e^- \bar{\nu}$
  - Main systematic uncertainties:
    - $\pi^0$  reconstruction efficiency
    - $\mathcal{B}(D^{*0} \rightarrow \pi^0 D^0)$
    - $R_1(1)$  and  $R_2(1)$  for  $p^2$
  - Results:
    - $F(1)|V_{cb}| = (35.9 \pm 0.6 \pm 1.4) \cdot 10^{-3}$
    - $p^2 = 1.16 \pm 0.06 \pm 0.08$
    - $\mathcal{B}(B^- \rightarrow D^{*0} e^- \bar{\nu}) = (5.56 \pm 0.08 \pm 0.41)\%$
- in agreement with PDG values of  $\mathcal{B}(B^0 \rightarrow D^{*+} e^+ \bar{\nu})$



# BABAR Results vs. World Average

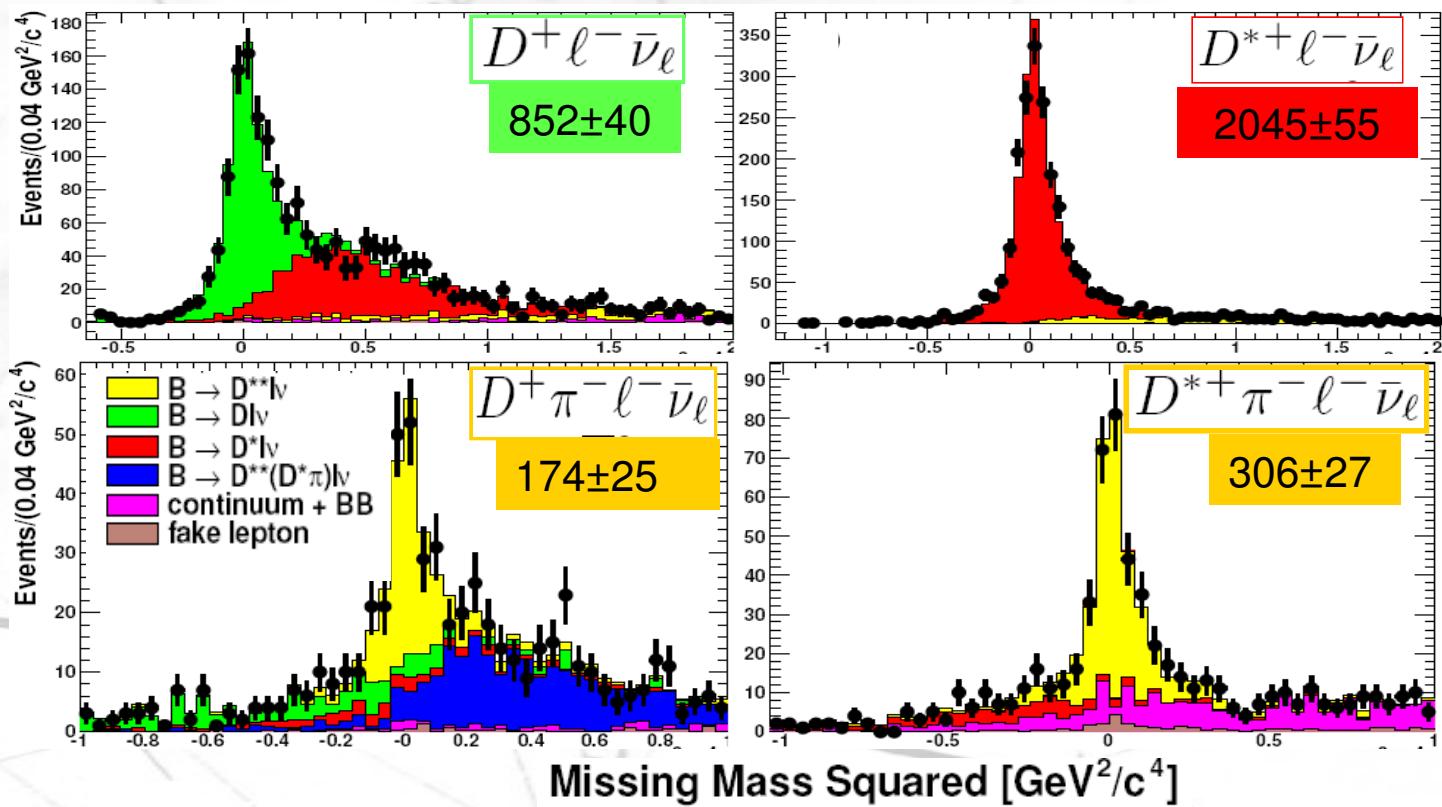
- Global multidimensional fit (arXiv:0712.3493,  $B \rightarrow D^{*0} \ell v$  not yet included)



- Improved precision: 2.1% (Winter 2006)  $\rightarrow$  1.6% (now) on  $F(1)|V_{cb}|$
- Using  $F(1)=0.919+0.033$  (Hashimoto et al PRD66 104503):  $|V_{cb}| = (39.1+0.6+1)10^{-3}$
- While from inclusive decays (kin. scheme)  $|V_{cb}| = (41.68+0.39+0.58)10^{-3}$
- Discrepancy between inclusive and exclusive  $|V_{cb}|$

# Branching Fractions for $B \rightarrow D/D^*/D\pi/D^*\pi\ell\nu_\ell$

- Breco sample
- reconstruct  $e, \mu$  in the recoil
- reconstruct  $D^{(*)}(0)(\pm)$  in the recoil
- extract signal by fitting missing mass squared
- dominant syst due to Breco,  $\mathcal{B}(D^{(*)}(0)(\pm))$  and track reconstr.



$$\begin{aligned}\mathcal{B}(B^- \rightarrow D^{(*)}\pi\ell^-\bar{\nu}_\ell) &= (1.52 \pm 0.12_{\text{stat.}} \pm 0.10_{\text{syst.}})\% \\ \mathcal{B}(\bar{B}^0 \rightarrow D^{(*)}\pi\ell^-\bar{\nu}_\ell) &= (1.37 \pm 0.17_{\text{stat.}} \pm 0.10_{\text{syst.}})\%,\end{aligned}$$

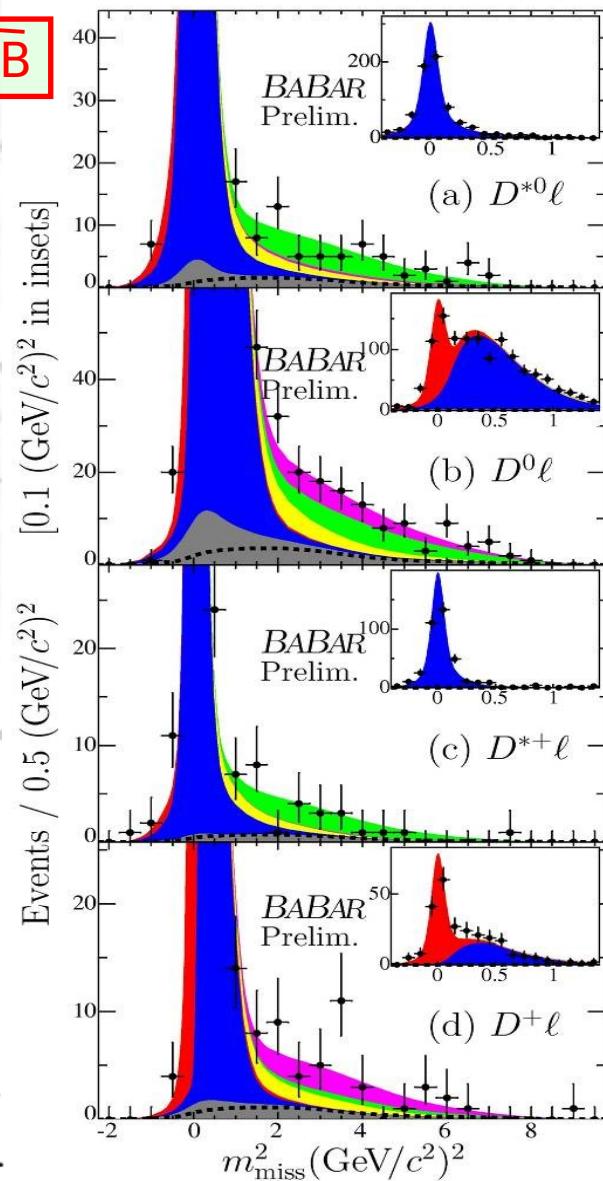
Results consistent with isospin symmetry, but  
 $\Delta_{\text{excl-incl.}} = (1.2 \pm 0.4)\%$ !

# Observation of $B \rightarrow D^{(*)}\tau \bar{\nu}$

232M  $B\bar{B}$

- Large  $\tau$  mass gives sensitivity to new physics at tree level.  
Eg charged Higgs boson
- Very challenging:  $\tau \rightarrow e\nu_e \tau$ ,  $\tau \rightarrow \mu\nu_\mu \tau$  produce two additional neutrinos
- Select Breco events. Identify  $D^{(*)}$  plus lepton in the recoil.
- Maximum likelihood fit with:
  - two discriminating variables **missing mass squared squared** and lepton energy
  - 8 channels: 4 signal ( $D^0\tau \bar{\nu}$ ,  $D^{*0}\tau \bar{\nu}$ ,  $D^+\tau \bar{\nu}$ ,  $D^{*+}\tau \bar{\nu}$ ), 4 background  $B \rightarrow D^{**}\ell \bar{\nu}$ .

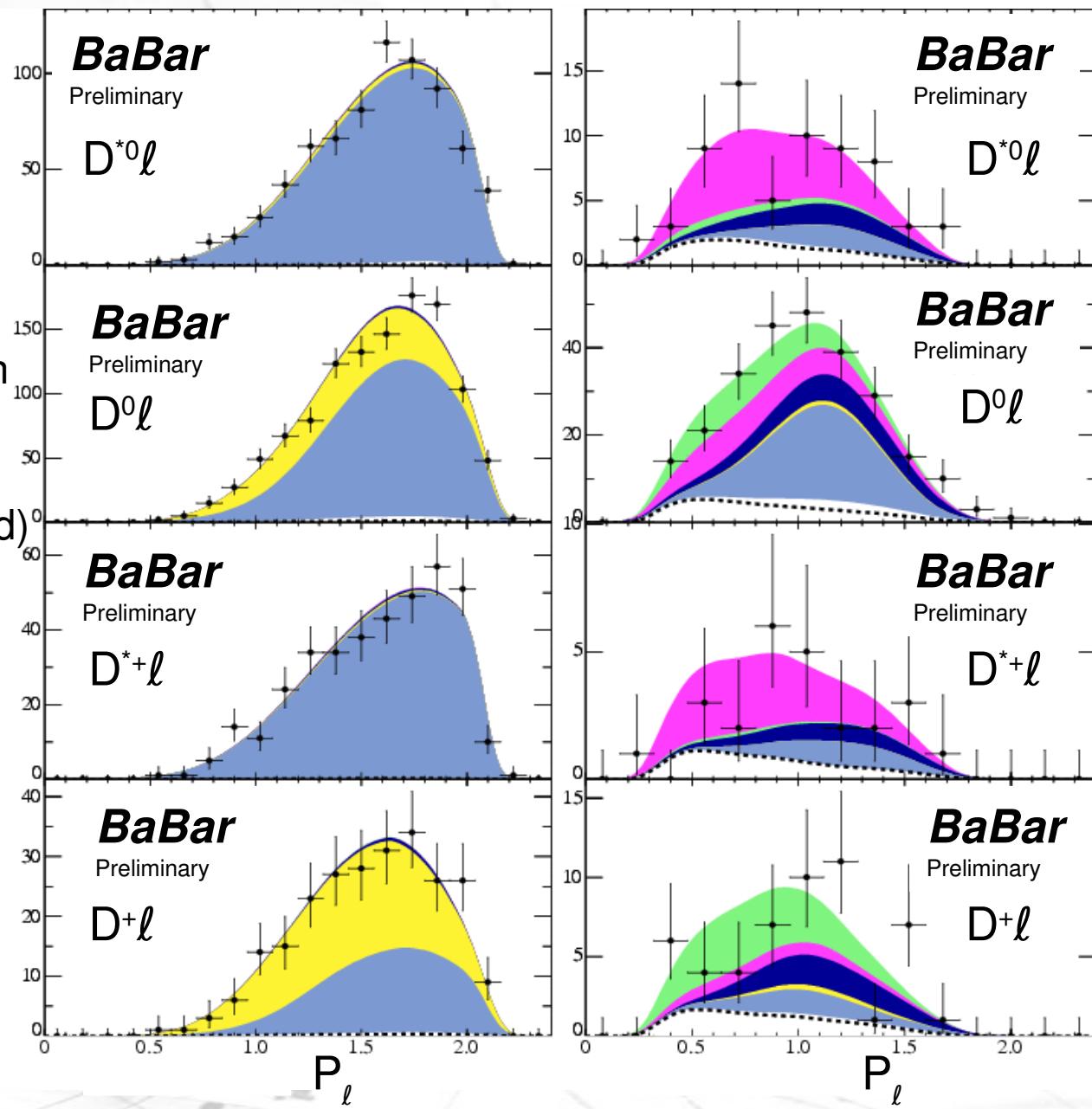
■	$D^*\tau \bar{\nu}$
■	$D\tau \bar{\nu}$
■	$D^{*\ell} \bar{\nu}$
■	$D\ell \bar{\nu}$
■	$D^{**}\ell \bar{\nu}$
□	Comb.



# $D^{(*)}\tau\nu$ – fit results

Normalization  
region  
(low invariant  
mass squared)

- █  $D^*\tau\nu$
- █  $D\tau\nu$
- █  $D^*\ell\nu$
- █  $D\ell\nu$
- █  $D^{**}\ell\nu$
- Comb.

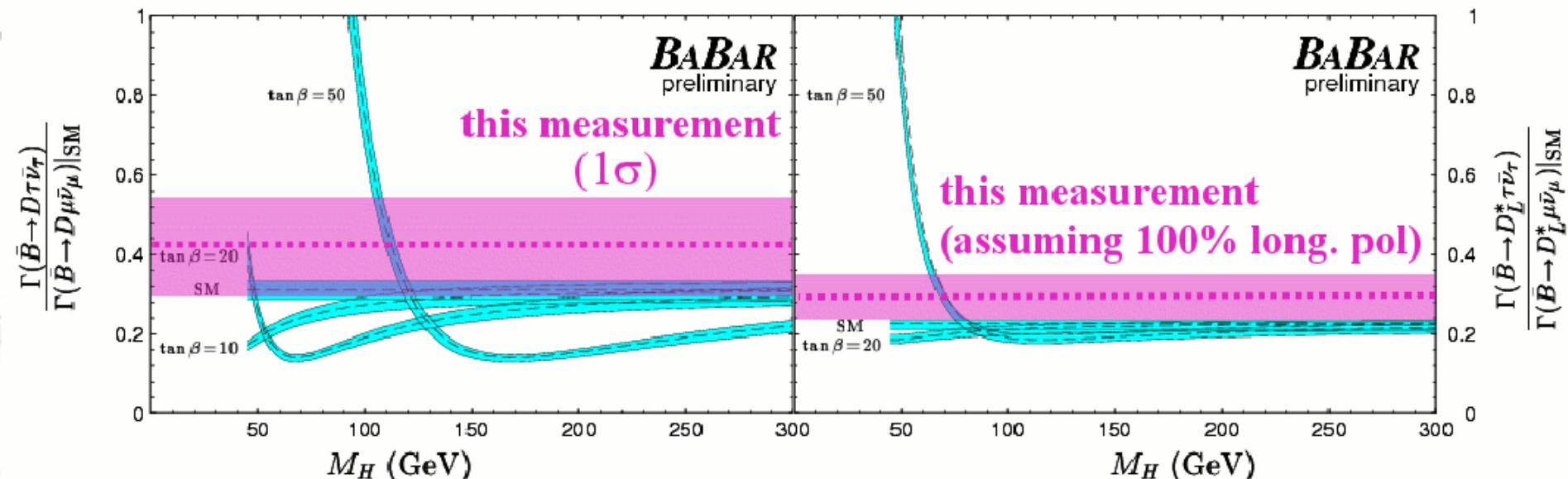


Signal region  
(high invariant  
mass squared)

# Observation of $B \rightarrow D^{(*)}\tau\nu$

*Confirmation of Belle observation in  $D^{*+}$ , first observation of  $D^{*0}$  and first evidence for the  $D$  modes.*

Mode	$R$ [%]	$\mathcal{B}$ [%]	Main systematic errors from PDF parametrization, combinatoric background parametrization
$B \rightarrow D\tau^-\bar{\nu}_\tau$	$41.6 \pm 11.7 \pm 5.2$	$0.86 \pm 0.24 \pm 0.11 \pm 0.06$	$3.6 \sigma$
$B \rightarrow D^*\tau^-\bar{\nu}_\tau$	$29.7 \pm 5.6 \pm 1.8$	$1.62 \pm 0.31 \pm 0.10 \pm 0.05$	$6.2 \sigma$



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- Exclusive Decays
  - ▶  $D^{(*)}(\ell\nu)$
  - ▶  $\pi(\eta^{'})\ell\nu$
- Conclusions

# Exclusive $B \rightarrow \pi \ell \nu$

- $B \rightarrow \pi \ell \nu$  rate is given by

$$\frac{d\Gamma(B \rightarrow \pi \ell \nu)}{dq^2} = \frac{G_F^2}{24\pi^3} |V_{ub}|^2 p_\pi^3 |f_+(q^2)|^2$$

- Form factor  $f_+(q^2)$  has been calculated using

- Lattice QCD

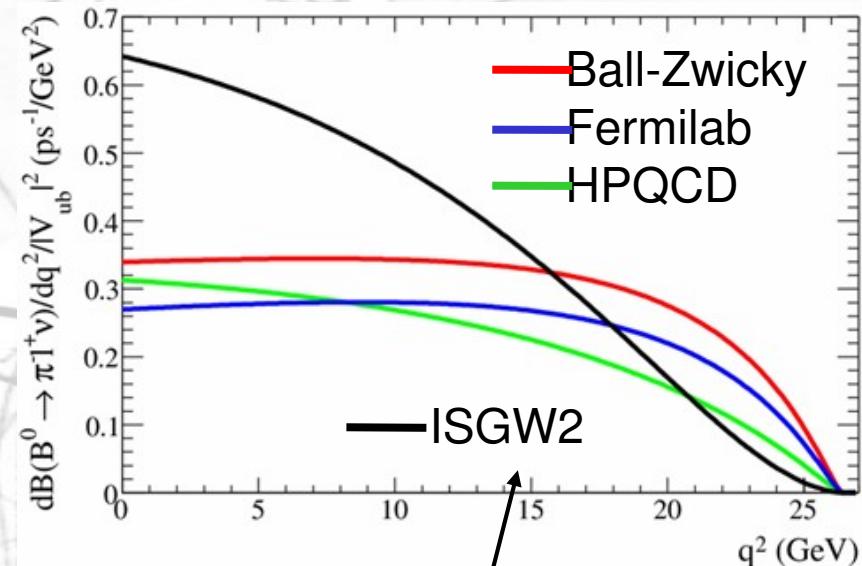
- Unquenched calculations by Fermilab ([hep-lat/0409116](#)) and HPQCD ([PRD73:074502](#))

- $\pm 12\%$  for  $q^2 > 16 \text{ GeV}^2$

- Light Cone Sum Rules

- Ball & Zwicky ([PRD71:014015](#))
  - $\pm 13\%$  for  $q^2 < 16 \text{ GeV}^2$

One FF for  $B \rightarrow \pi \ell \nu$  with massless lepton



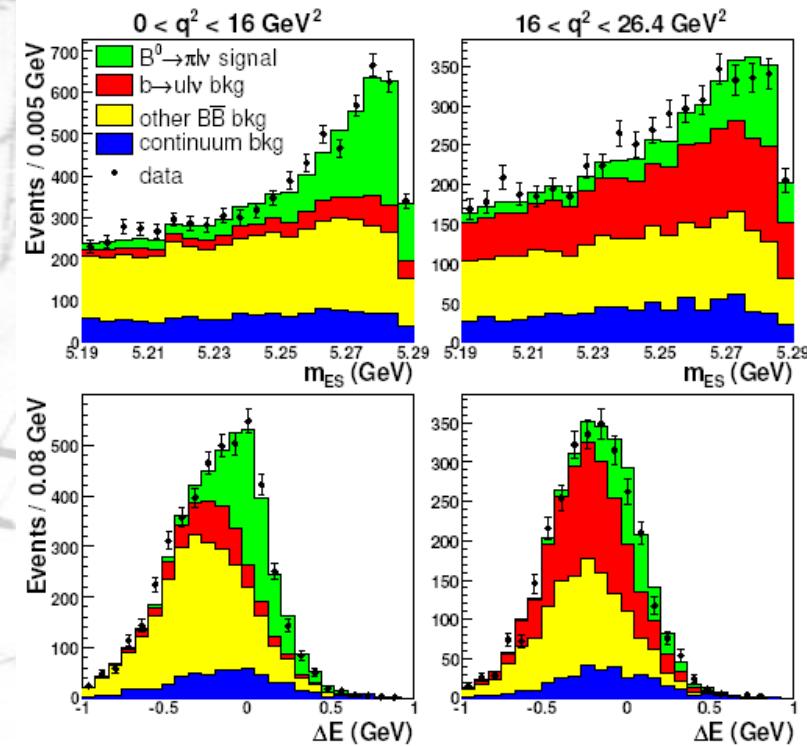
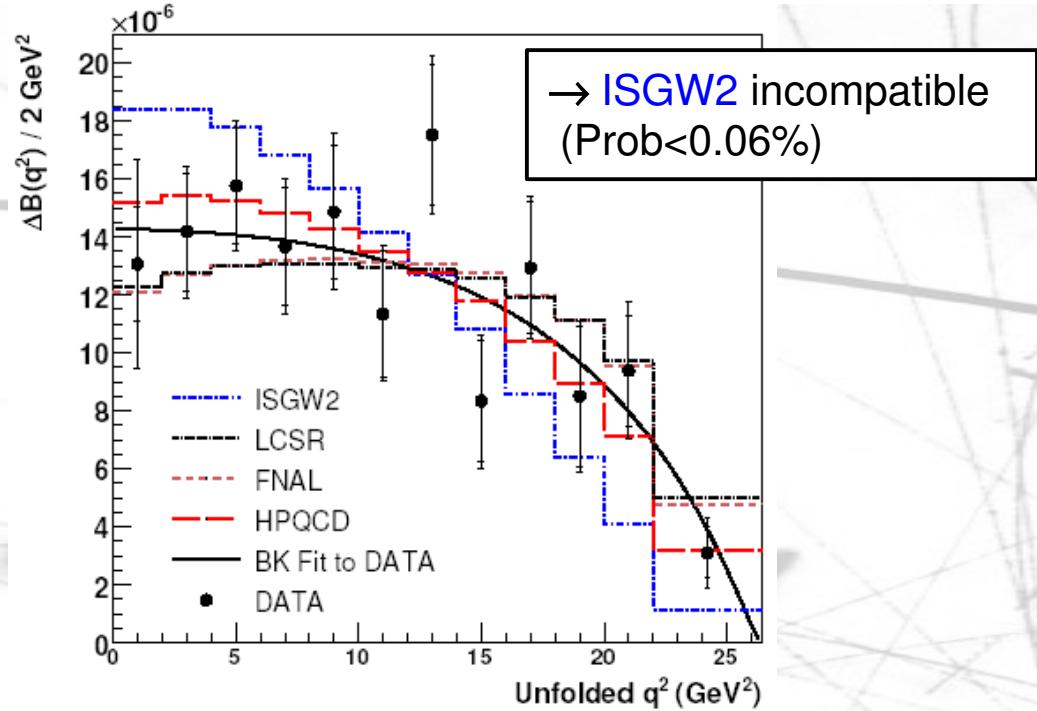
Quark model, PRD52 (1995) 2783

# Loose untagged $B \rightarrow \pi^+ \ell \nu$

206M BB

- No Tag
- No *neutrino tight quality* cuts (increase signal efficiency)
- 12  $q^2$  bins
- Smallest statistical and systematic uncertainties of all individual published  $B \rightarrow \pi \ell \nu$  measurements
- Larger systematic error due to fit

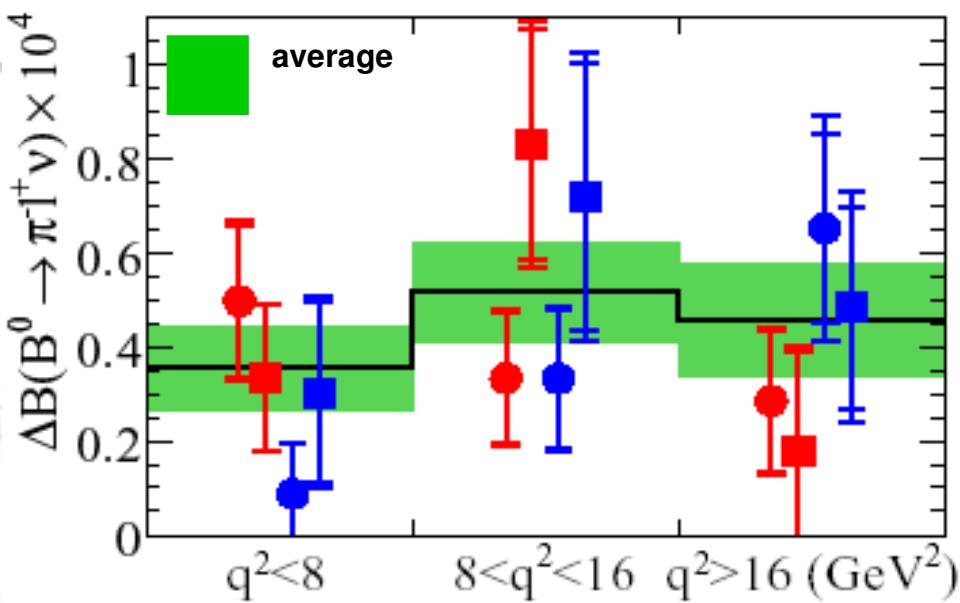
$$\mathcal{B}(B \rightarrow \pi^+ \ell \nu) = (1.46 \pm 0.07_{\text{stat}} \pm 0.08_{\text{syst}}) 10^{-4}$$



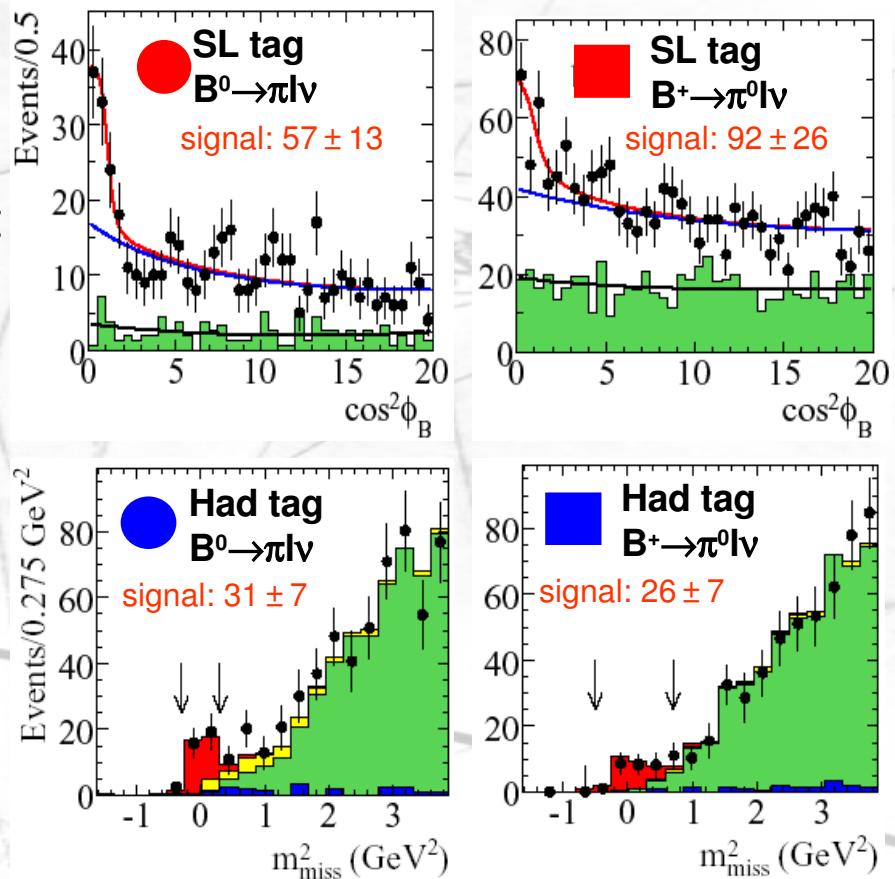
# Tagged $B \rightarrow \pi^0/\ell\nu$

211M BB

- Fully (hadronic) and semileptonic tags
- Neutral and charged pion
- 3  $q^2$  bins
- Dominated by statistical error for the moment
- Main syst errors: signal MC stat., signal PDF, photon and  $\pi^0$  reconstruction.

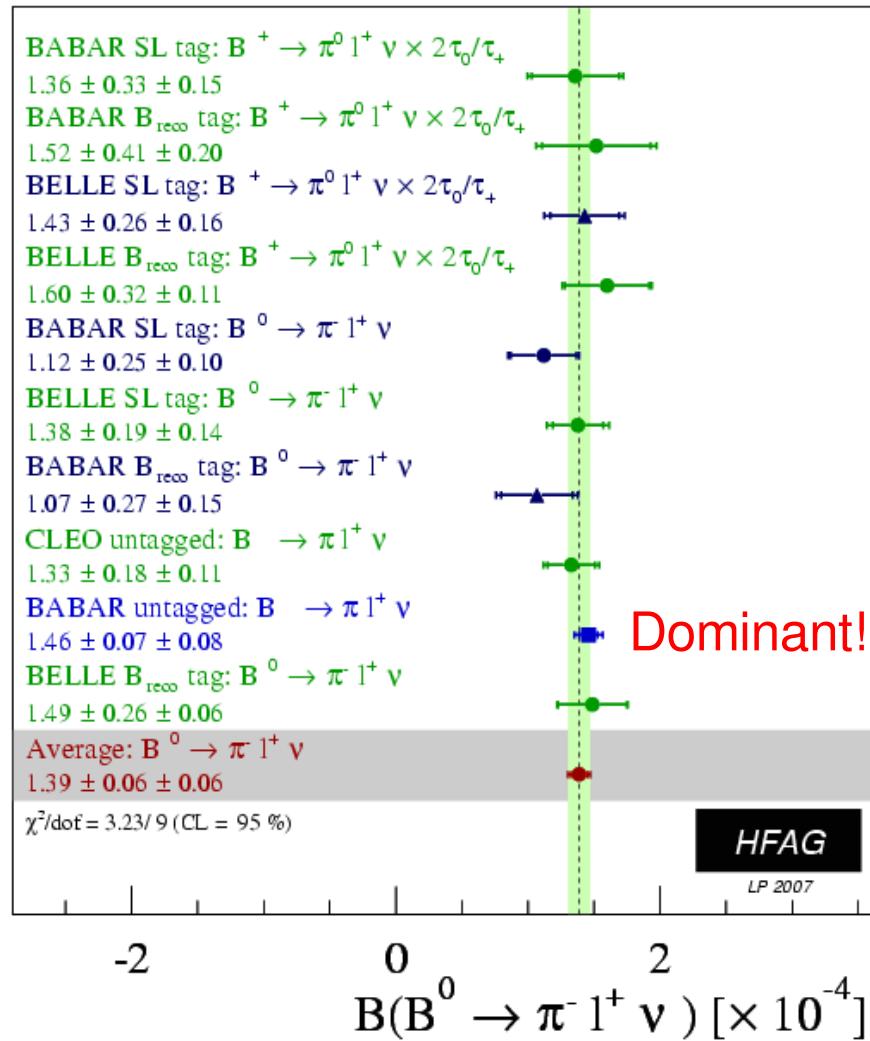


$\phi_B$  is the angle between the directions of the two B mesons.



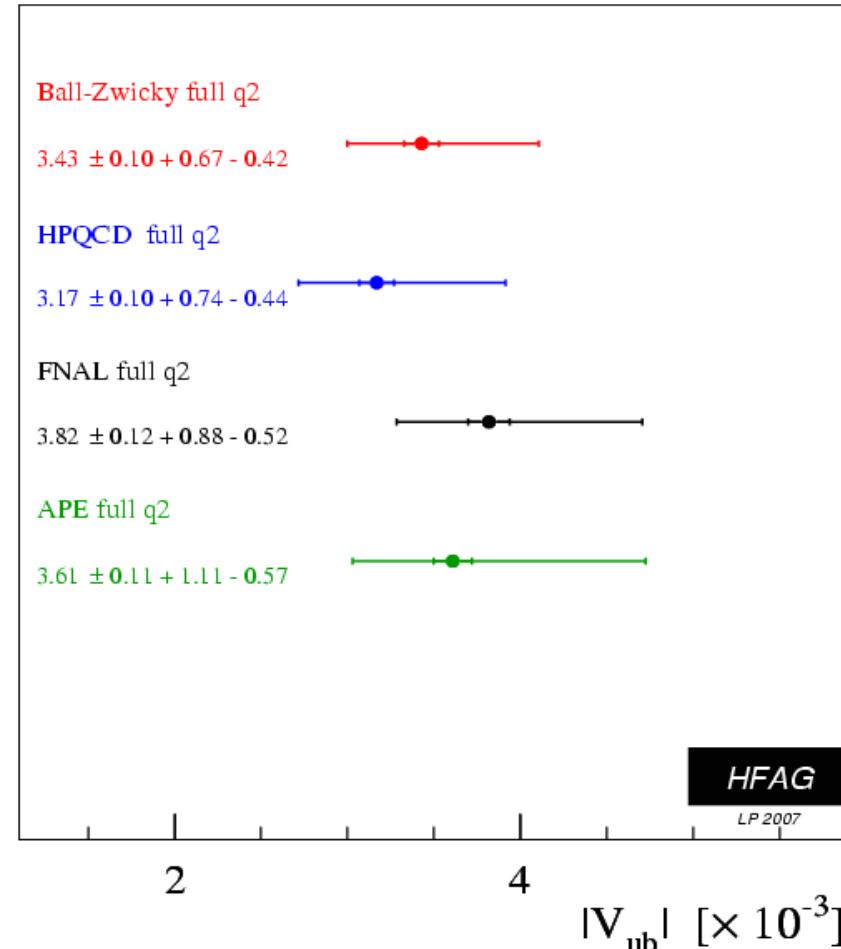
Total B comparable with untagged analysis  
 $B(B \rightarrow \pi^+ \ell \bar{\nu}) = (1.33 \pm 0.17_{\text{stat}} \pm 0.11_{\text{syst}}) 10^{-4}$

# Exclusive $|V_{ub}|$ : Summary



HFAG branching fraction average:

$$\mathcal{B}(B \rightarrow \pi^+ l \nu) = (1.39 \pm 0.06_{\text{stat}} \pm 0.06_{\text{syst}}) 10^{-4}$$

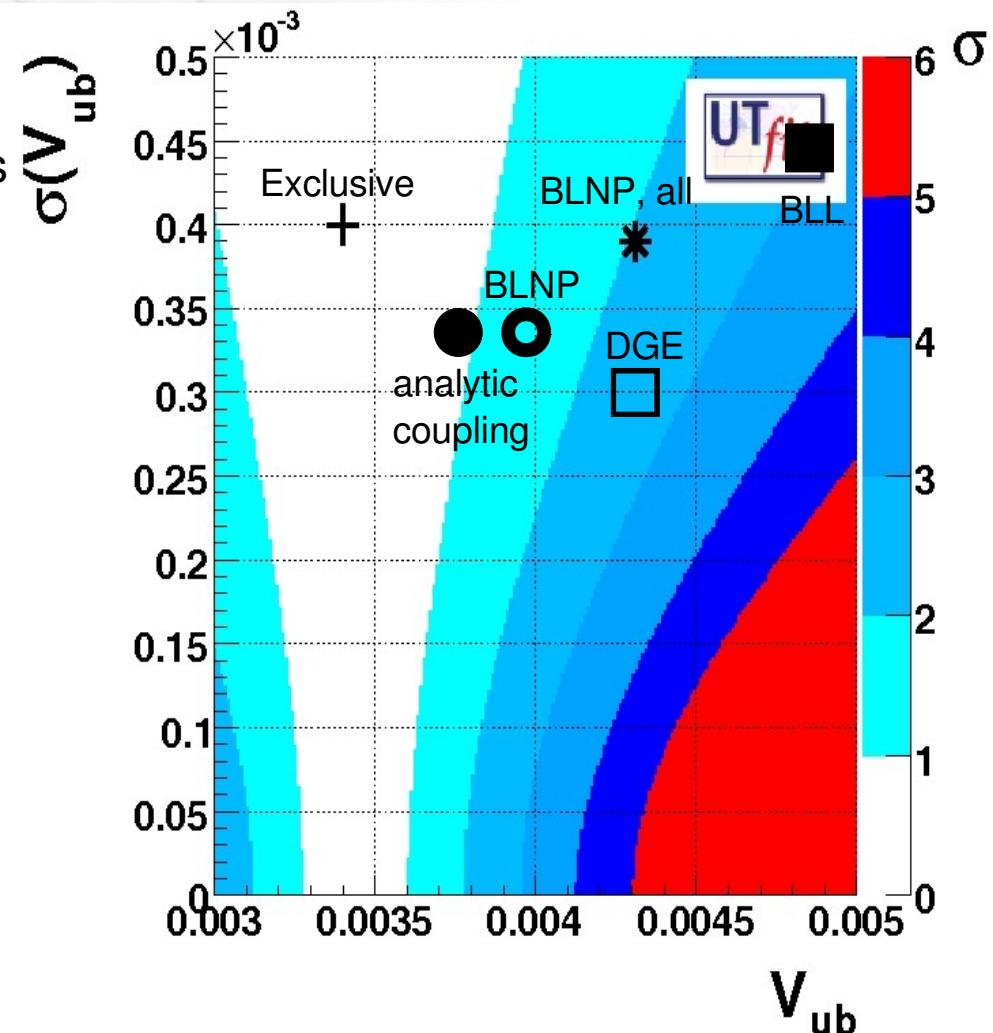


$|V_{ub}|$ :

- Small experimental errors
- Large theoretical error on FF
- Theory error needs to improve!

# $|V_{ub}|$ : CKM consistency

- Most probable value of  $|V_{ub}|$  from measurements of other CKM parameters Standard Model and from the exclusive final states favours a value  $\sim 3.5 \cdot 10^{-3}$
- Steady work in the inclusive decays to improve current calculations of  $|V_{ub}|$
- “Tension” with exclusive decays not there anymore for some calculations
- Still work on the experimental and theoretical side needed to understand current results

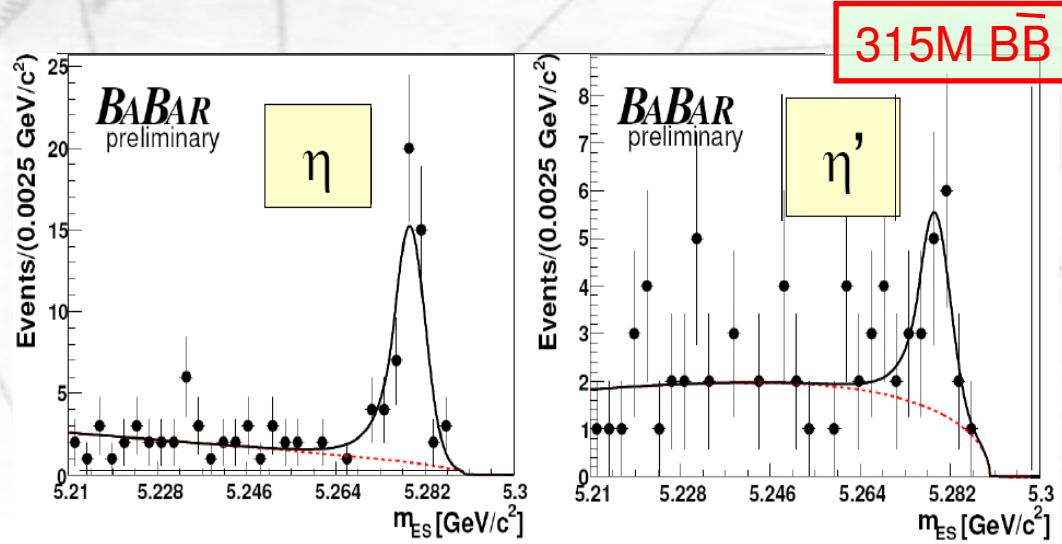


$|V_{ub}|$  values obtained with other methods have larger errors than  $0.5 \cdot 10^{-3}$ .

# Other Modes: $B \rightarrow \eta \ell \nu$ and $B \rightarrow \eta' \ell \nu$

Independent measurements of various  $B \rightarrow X_u \ell \nu$  decay modes important to further constraint theoretical models

- ❖ Hadronic tag
- ❖ Reconstruction of signal  $B$ :
  - Lepton momentum  $p^* > 0.5 \text{ GeV}$  for electrons  $p^* > 0.8 \text{ GeV}$  for muons
  - Meson reconstructed in
    - $\eta \rightarrow \gamma\gamma$
    - $\eta \rightarrow \pi^+\pi^-\pi^0$
    - $\eta \rightarrow \pi^0\pi^0\pi^0$
    - $\eta' \rightarrow \rho\gamma$
    - $\eta' \rightarrow \eta\pi^+\pi^-$
- ❖ fit to  $m_B$  distributions to extract signal yields



$$\mathcal{B}(B^+ \rightarrow \eta \ell^+ \nu) < 1.4 \times 10^{-4} \text{ (90\% CL)}$$

$$\mathcal{B}(B^+ \rightarrow \eta' \ell^+ \nu) = (0.84 \pm 0.27_{\text{stat}} \pm 0.21_{\text{syst}}) 10^{-4}$$

$$\mathcal{B}(B^+ \rightarrow \eta' \ell^+ \nu) < 1.3 \times 10^{-4} \text{ (90\% CL)}$$

# Outline

- Introduction
  - ▶ Motivations
  - ▶ BaBar
  - ▶ Experimental approach
- Inclusive decays
  - ▶ Determination of  $|V_{cb}|$
  - ▶ Determination of  $|V_{ub}|$
- Exclusive Decays
  - ▶  $D^{(*)}(\ell\nu)$
  - ▶  $\pi(\eta^*)\ell\nu$
- Conclusions

# Summary

- Very significant improvements of understanding semileptonic B decays in the past 5 years!
- Challenge of QCD corrections is being addressed.
- High order terms in OPE calculations are needed. Special treatment for  $B \rightarrow X_s \gamma$  required.
- Experimentally,  $B \rightarrow X_u l \bar{\nu}$  measurements can be improved with higher statistics and reduced systematics.
- Exclusive measurements: needed improved normalization of FF by theory
- Current differences between exclusive and inclusive measurements may be of both theory and experimental nature.
- Tight scrutiny needed to arrive at a more stringent test of the CKM matrix in the future!
- First evidence of  $B \rightarrow D \tau \bar{\nu}$ !