



Google AI
Quantum

Google's quantum computer and pursuit of quantum supremacy

Ping Yeh (pingyeh@google.com)

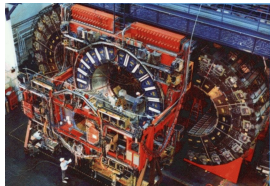
Google Santa Barbara

KEK, 2019-09-26



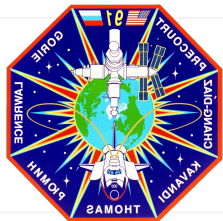
About me

Collider Detector at
Fermilab (CDF)



Thesis: "Measurement of Top Quark Mass from Dilepton Events using Invariant Mass of Lepton and b-jet in p-pbar collisions at $\sqrt{s} = 1.8 \text{ TeV}$ "

Data production design for CDF-2 upgrade



Alpha Magnetic
Spectrometer

Onboard data acquisition software in assembly for Sharc DSP

Particle back-tracing in geo-magnetic field, for identifying cosmic rays (signals) from geo-trapped particles (backgrounds)

Belle B factory



eta' meson



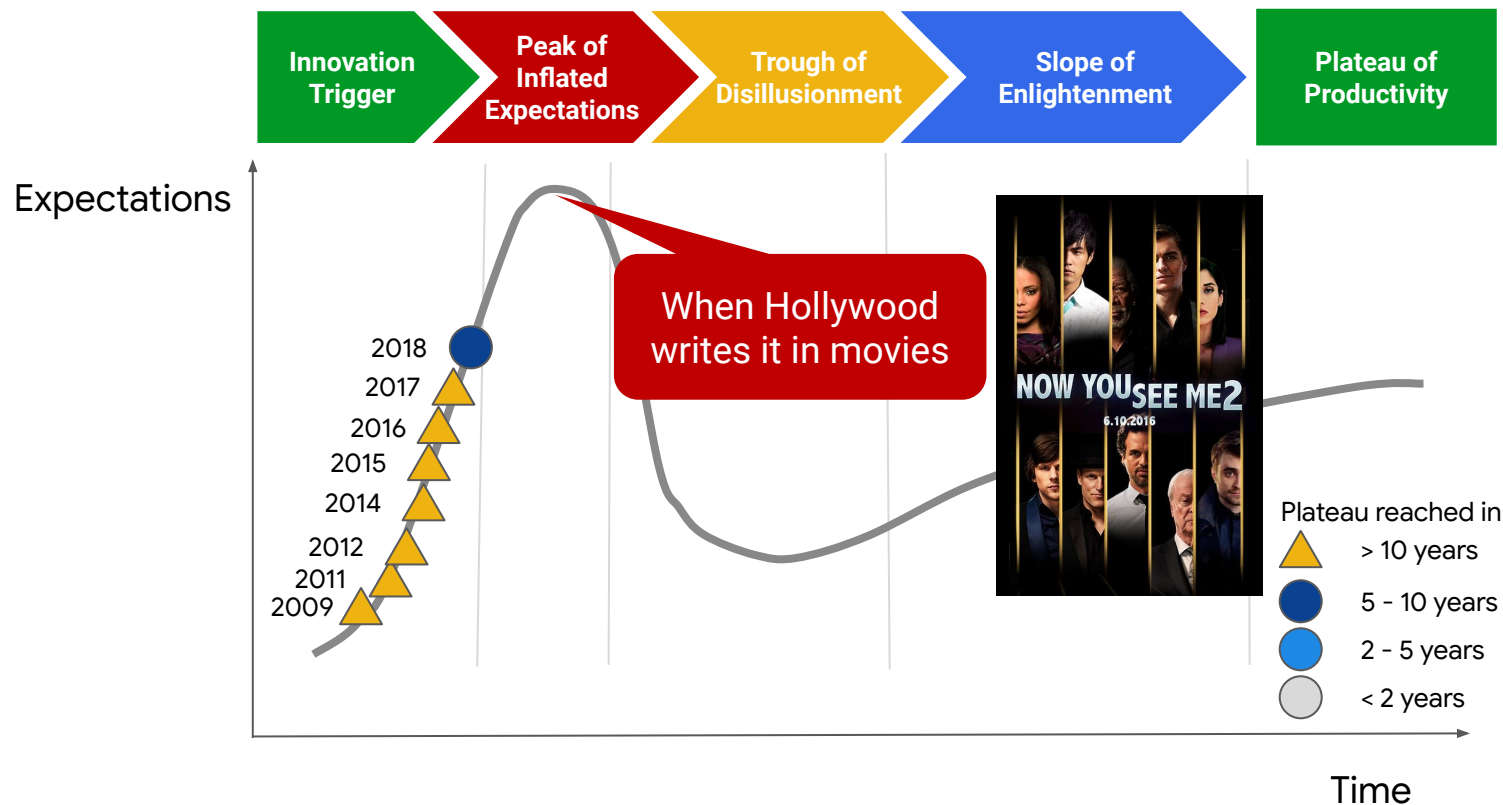
oogle

Search quality, iGoogle (personalized homepage), Google Analytics & Adwords, Cross-device ads attribution, 2 cancelled "start up" projects, and now quantum computing.



Google AI
Quantum

Quantum computing on Gartner's hype curve



Goal & timeline set by physicists

Quantum Computing Roadmap v1 (2002) and v2 (2004)

https://qist.lanl.gov/pdfs/qc_roadmap.pdf

“ The ten-year (2012) goal would extend QC into the “architectural / algorithmic” regime, involving a quantum system of such complexity that it is beyond the capability of classical computers to simulate. ”



Not yet achieved



Coined by John Preskill as "Quantum Supremacy" in 2012.

Quantum control

Also in the roadmap:

“ Quantum systems of ***unprecedented complexity*** will be created and ***controlled***, potentially leading to greater fundamental understanding of how classical physics emerges from a quantum world, which is as perplexing and as important a question today as it was when quantum mechanics was invented. ”

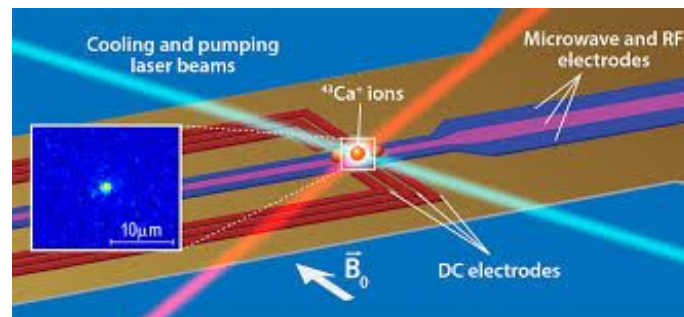
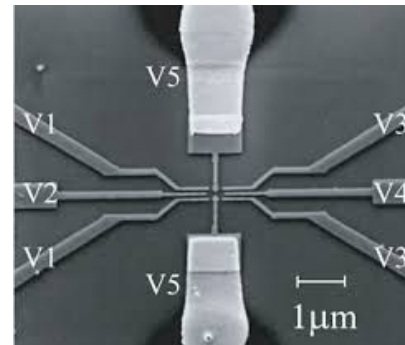
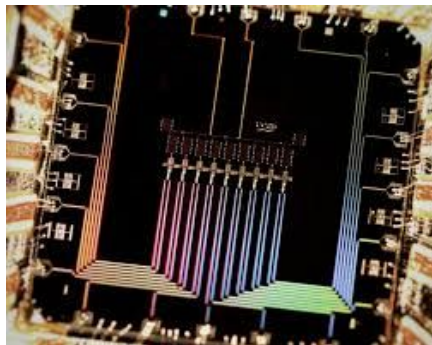


What is Quantum Computing?

Using **2-state quantum systems** to perform computational tasks.

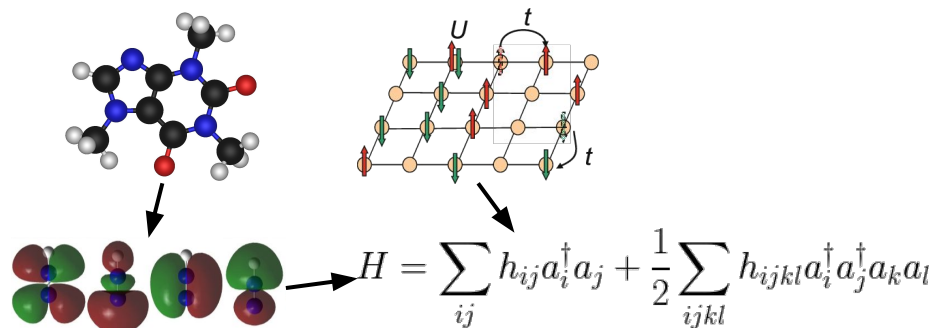
Some 2-state quantum systems:

- Photons
- Nuclear spins
- Trapped Ions
- Neutral Atoms
- Molecular spins
- Quantum dots
- Superconducting circuits

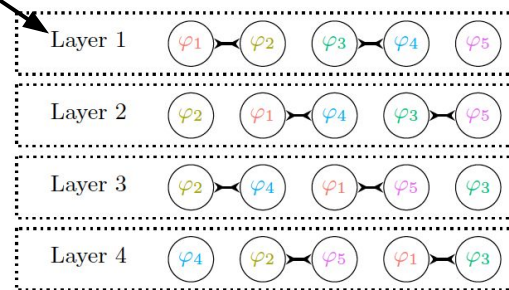
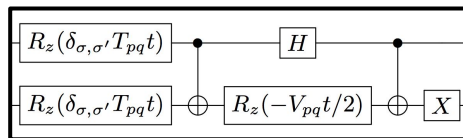


Why build a quantum computer?

Quantum simulation
Feynman's initial idea



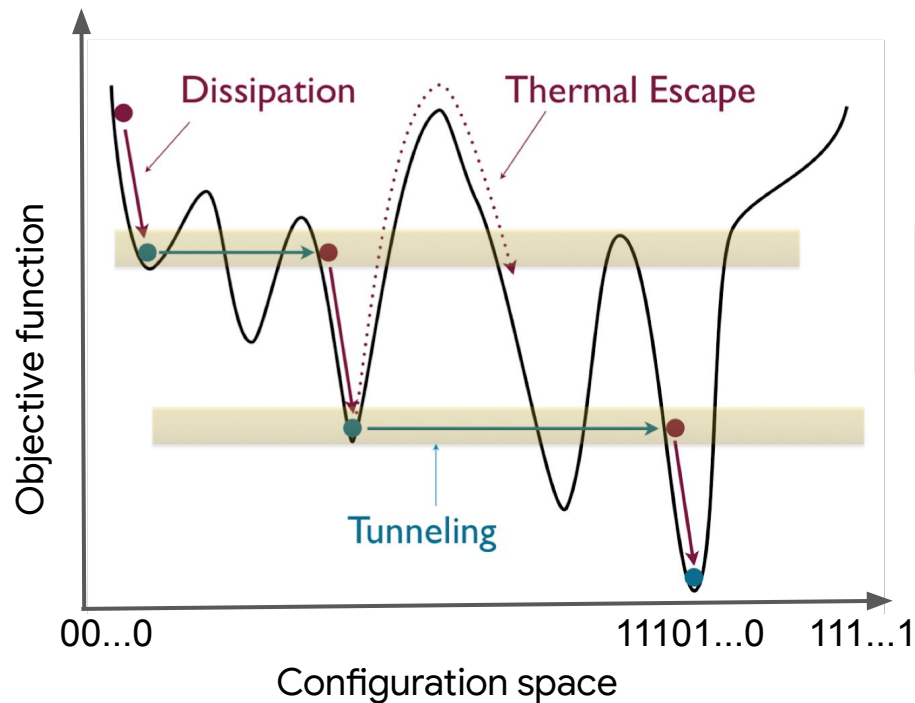
$$H = \sum_{p \neq q} \tilde{T}_{pq} (X_p Z_{p+1} \cdots Z_{q-1} X_q + Y_p Z_{p+1} \cdots Z_{q-1} Y_q) \\ + \sum_{p \neq q} \tilde{V}_{pq} Z_p Z_q + \sum_p \tilde{U}_p Z_p$$



Why build a quantum computer?

Quantum simulation

Optimization



Why build a quantum computer?

Quantum simulation

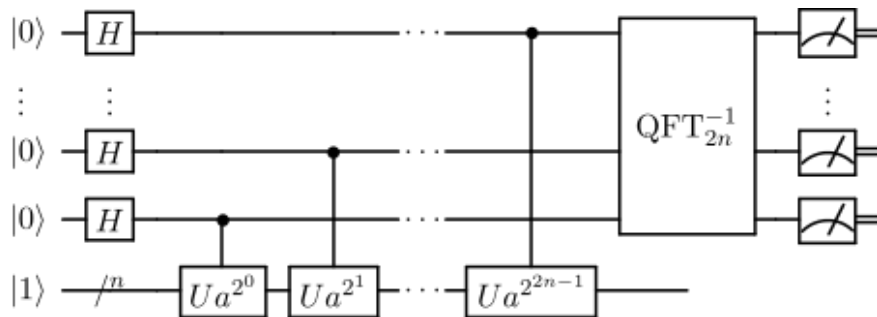
Optimization

Factoring

age of universe vs. < 1 day
for $n = 2048$.

Classical algorithm $O\left(e^{1.9n^{1/3}(\log n)^{2/3}}\right)$

Shor's algorithm $O\left(n^2(\log n)(\log \log n)\right)$



Factoring

$$15 = 5 \times 3$$



Why build a quantum computer?

Quantum simulation

Optimization

Factoring

???



OpenFermion

+



Cirq

<https://www.openfermion.org/>

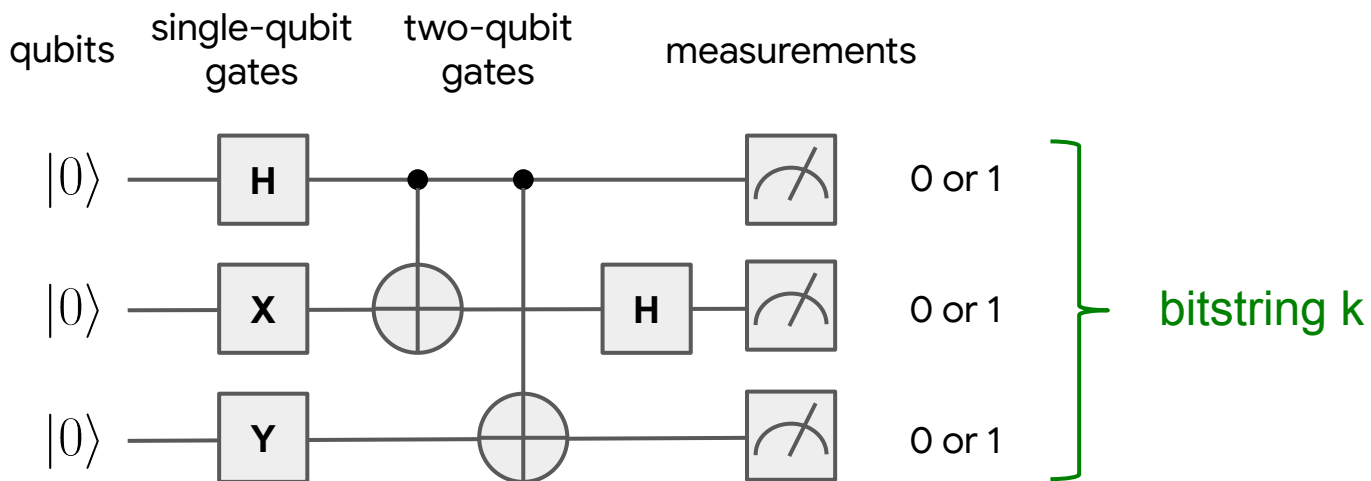
<https://github.com/quantumlib/cirq>



The computation model

Turing machine \rightarrow Quantum Turing machine

Alternatively: Quantum circuit



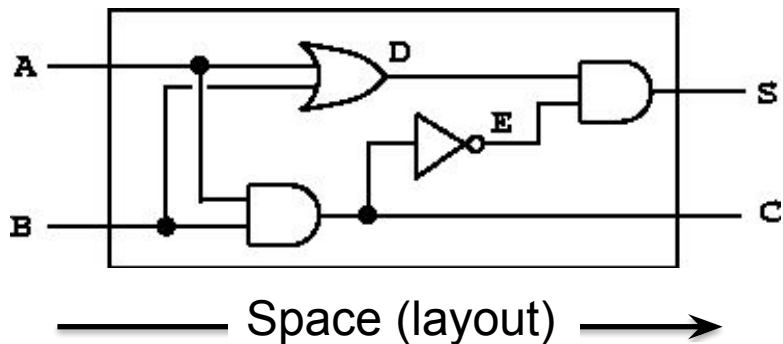
Other models: quantum annealing, adiabatic quantum computing.



Logic and quantum circuits

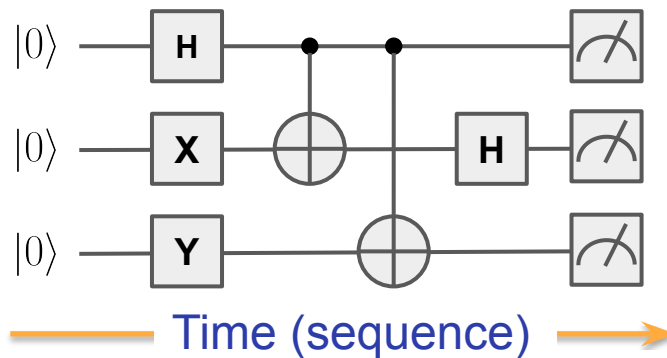
Classical logic circuit

- Deterministic
- Wiring fan-out
- Universal: 1 bit NOT + 2 bit AND



Quantum circuit

- Probabilistic
- No clone theorem
- Universal: 1 qubit rotation + 2 qubit CNOT



State of a qubit: Bloch sphere representation

Bloch sphere representation of a qubit:

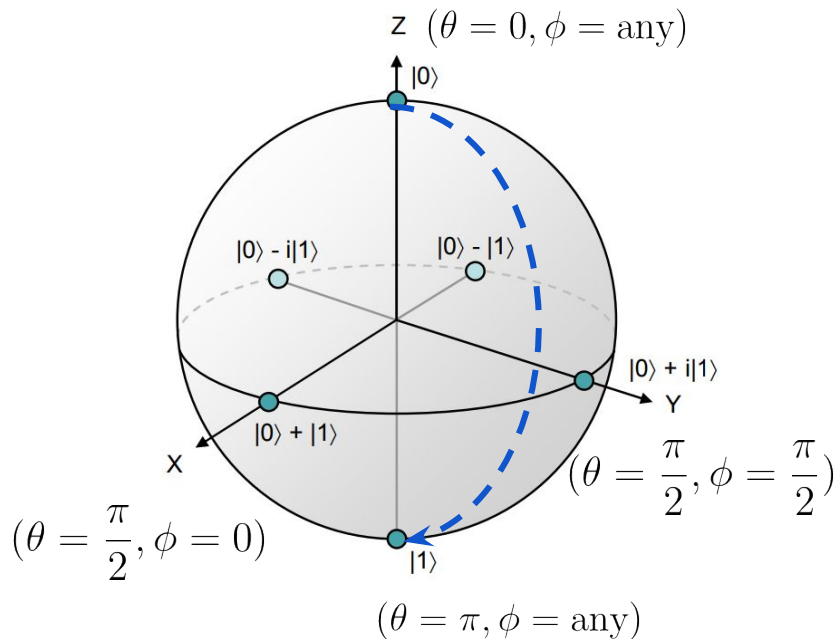
$$\begin{aligned} |\psi\rangle &= c_0|0\rangle + c_1|1\rangle \\ &= \cos \frac{\theta}{2} |0\rangle + \sin \frac{\theta}{2} e^{i\phi} |1\rangle \end{aligned}$$

(Global phase discarded)

A gate operation: $(\theta, \phi) \longrightarrow (\theta', \phi')$

- can be modeled as a rotation on Bloch sphere
- NOT gate = rotate around x-axis by π
- What about $\frac{\pi}{2}$ rotation?

Spherical angular coordinates (θ, ϕ)



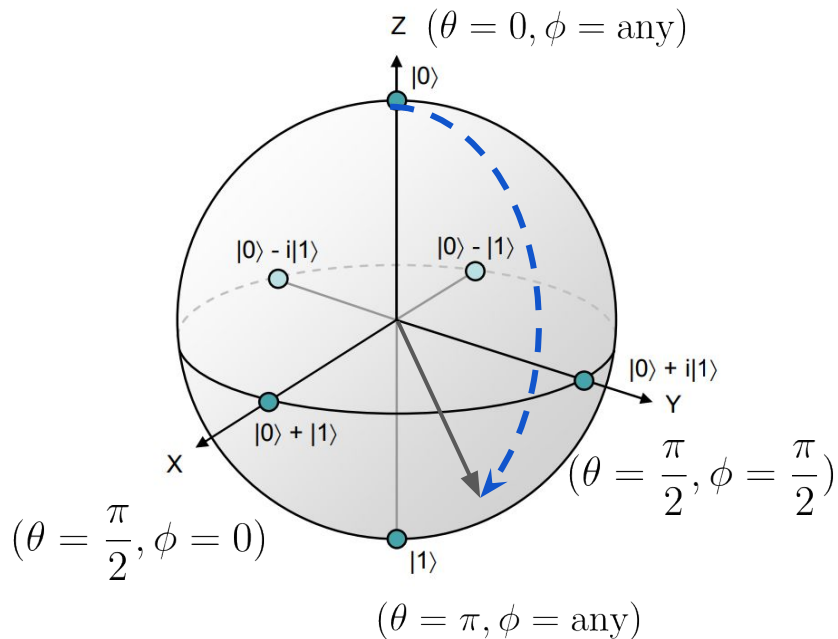
Challenge: Controlling a qubit

Analog control errors: over/under rotation, deviation of the rotation axis

Decoherence (environmental) errors: random bit flips / phase changes

Qubit error mechanisms inform nearly all design decisions

Spherical angular coordinates (θ, ϕ)



End Goal: Universal Fault-Tolerant QC

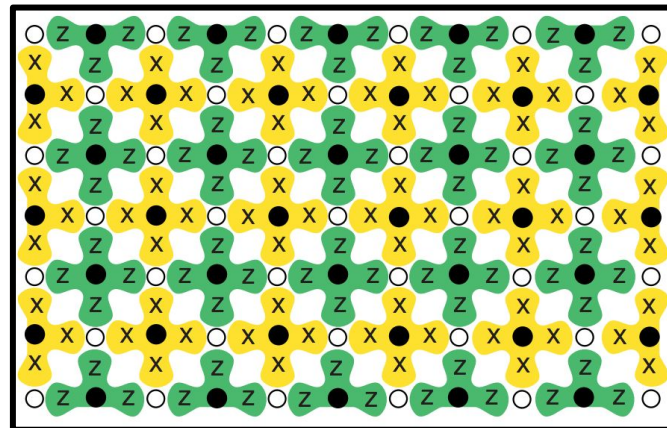
Fault tolerance via error correction

1 **logical qubit** from many **physical qubits**

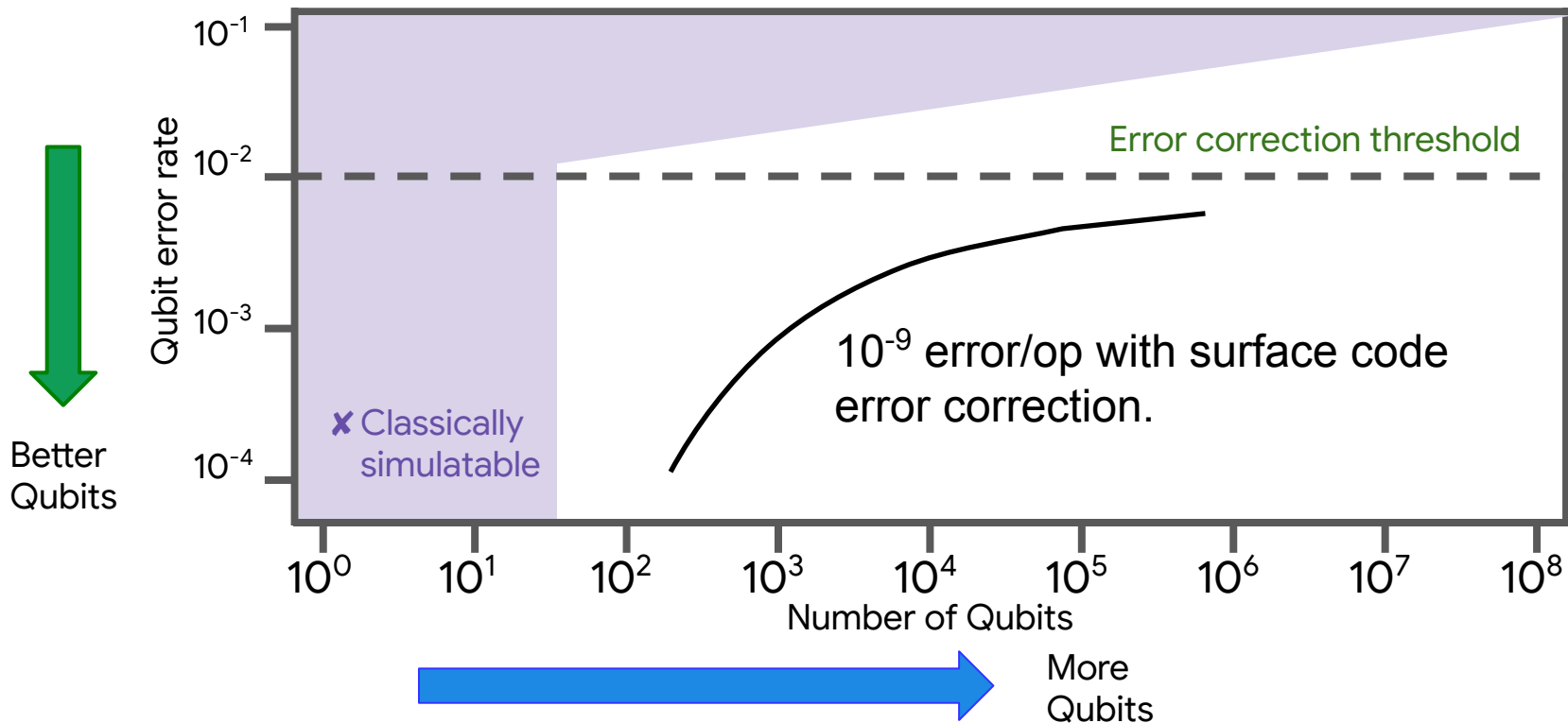
Universal QC requires error/op $\sim 10^{-10}$

Surface code error correction:

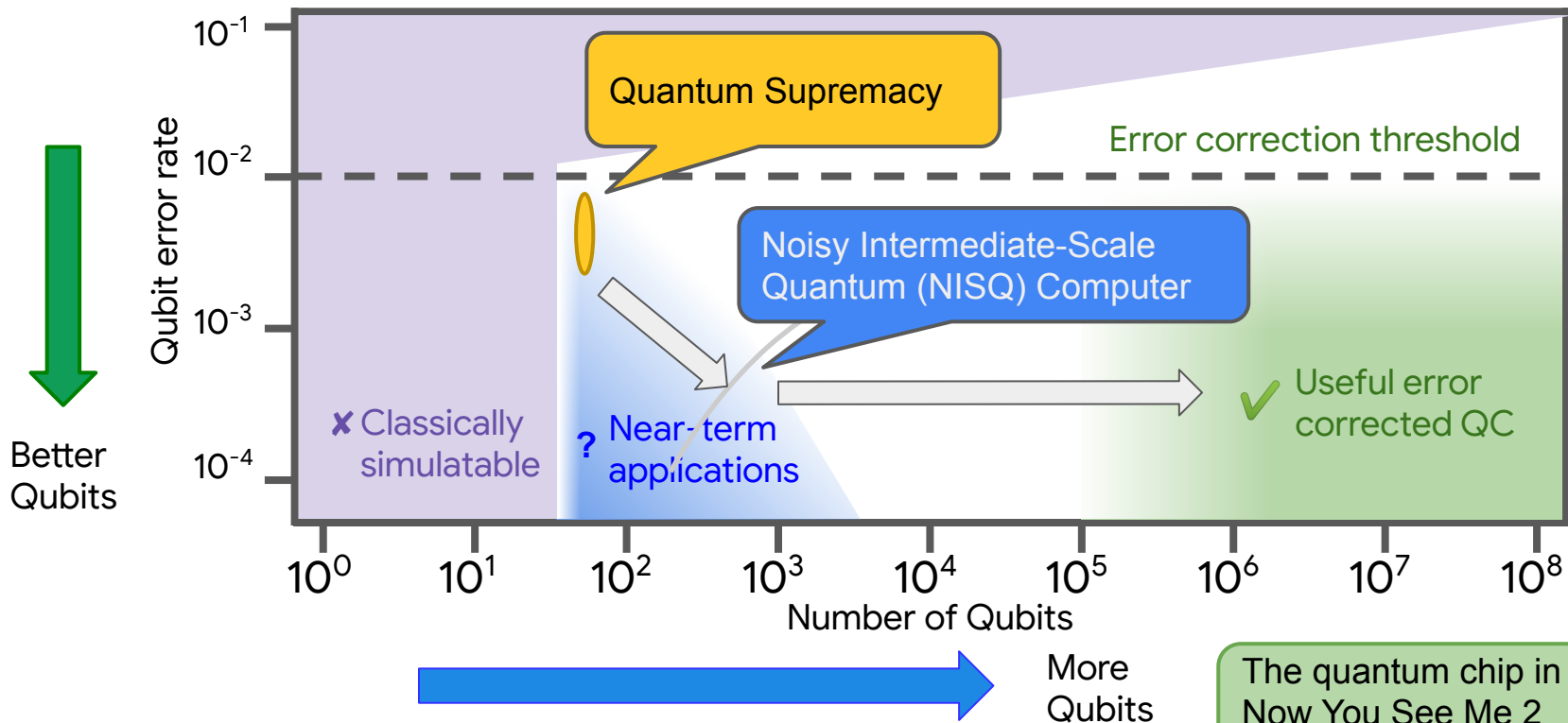
- 2D qubit array, nearest-neighbor coupling
- Error/op (physical): 10^{-2} threshold, 10^{-3} target
- Useful at 10^5 - 10^6 physical qubits



When is a Quantum Computer Useful?



When is a Quantum Computer Useful?



The quantum chip in Now You See Me 2 is off the chart.



DiVincenzo Criteria for Quantum Computers

1. Scalable system of well-characterized qubits
2. Ability to initialize to a fiducial state
3. Long coherence time
4. Universal set of quantum gates
5. Capable of measuring any specific qubit

[D. P. DiVincenzo, NATO ASI Series E, Kluwer Ac. Publ., Dordrecht, 1996]; arXiv:cond-mat/9612126v2.

Two more criteria were added later for quantum communications.



Physical systems for quantum computers (2004)

DiVincenzo Criteria	NMR	Neutral Atom	Cavity QED	Super-conductors	Trapped Ion	Photonic	Solid State
Scalable / well characterized	●	●	●	●	●	●	●
State preparation	●	●	●	●	●	●	●
Long coherence	●	●	●	●	●	●	●
Universal gates	●	●	●	●	●	●	●
Random-access measurement	●	●	●	●	●	●	●

- No viable approach is known
- Viable approach proposed, no sufficient proof of principle yet
- Viable approach has been sufficiently demonstrated

D. P. DiVincenzo, NATO ASI Series E, Kluwer Ac. Publ., Dordrecht, 1996; arXiv:cond-mat/9612126v2.

QC Roadmap 2.0 (2004)
https://qist.lanl.gov/pdfs/qc_roadmap.pdf



Physical systems for quantum computers (2018)

DiVincenzo Criteria	NMR	Neutral Atom	Cavity QED	Super- conductors	Trapped Ion	Photonic	Solid State
Scalable / well characterized	●	●	●	●●	●	●	●
State preparation	●	●	●	●	●	●●	●●
Long coherence	●	●●	●●	●●	●●	●	●●
Universal gates	●	●●	●	●●	●	●●	●●
Random-access measurement	●	●●	●	●●	●	●●	●●

- No viable approach is known
- Viable approach proposed, no sufficient proof of principle yet
- Viable approach has been sufficiently demonstrated

QC Roadmap 2.0 (2004)

Peter McMahon, Q2B 2018

<https://q2b2018.qcware.com/videos-presentations>



Major commercial players

Company	Qubit technology	#qubits	announcement time
IonQ	trapped ion	79/160	2018-12
Rigetti	superconducting	128	2018-08
Google	superconducting	72	2018-03
Alibaba	superconducting	11	2018-03
Intel	superconducting, silicon spin qubits	49 N/A	2018-01
IBM	superconducting	50	2017-11
D-Wave	superconducting	2000	2017-01
Microsoft	topological	N/A	N/A
Others

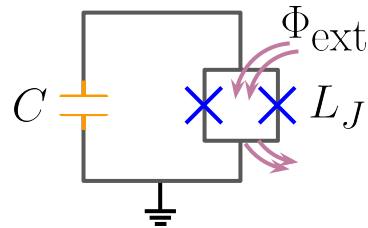
quantum
annealing
machine



Building a Superconducting Quantum Computer



Tunable qubits: LC circuit with SQUID



Josephson junction \sim nonlinear inductor

Hamiltonian

$$H = 4E_C n^2 - 2E_J \left| \cos \frac{\pi \Phi_{\text{ext}}}{\Phi_0} \right| \cos \varphi$$

$N(\text{Cooper pairs})$

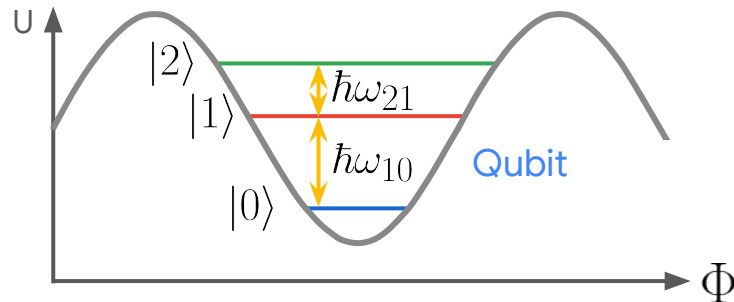
effective phase diff across SQUID

$[\varphi, n] = 1$

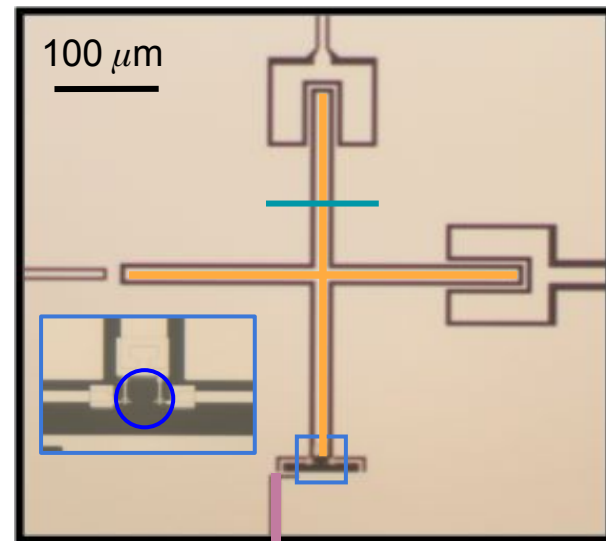
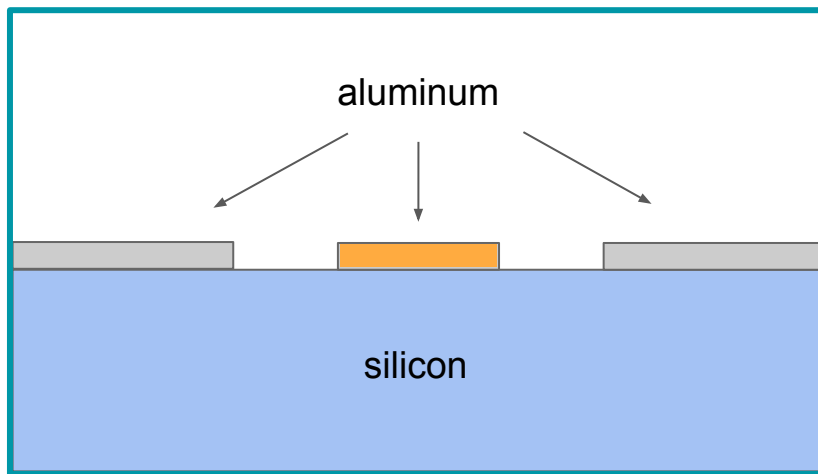
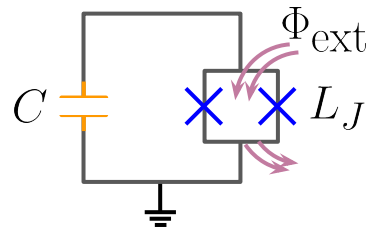
flux quantum

E_C, E_J : fixed by qubit material and geometry

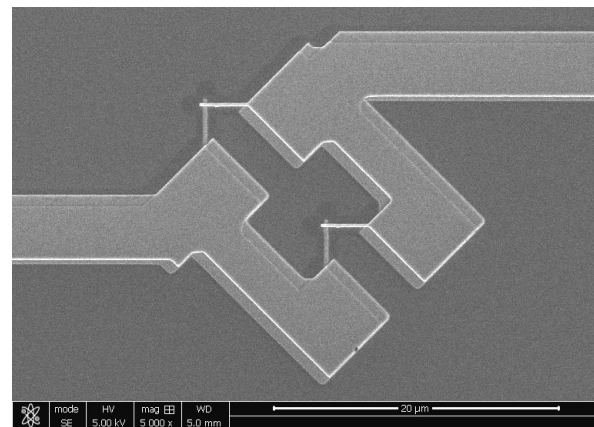
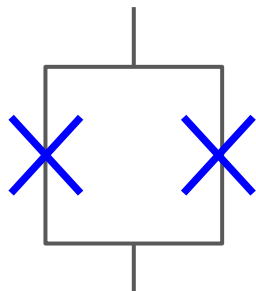
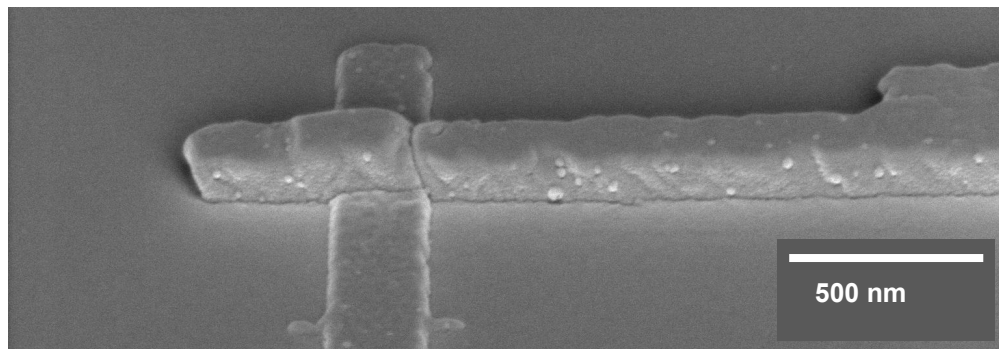
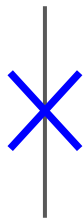
Qubit frequency tunable by Φ_{ext}



Physical layout of a transmon qubit



The fabricated Josephson junction



Region of Operation

Energy gap of superconducting aluminum

$$\Delta_{\text{Al}} = 3.4 \times 10^{-4} \text{ eV} \approx 82 \text{ GHz}$$

Consumer wireless applications (WiFi, LTE, etc.)

> 10 GHz hard/expensive to engineer

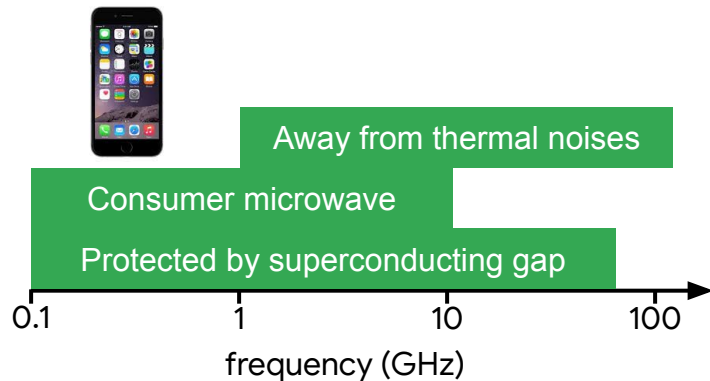
Dilution refrigerator cools to < 50 mK

Minimize thermal noises at $T \sim 10 \text{ mK}$ ($\sim 0.2 \text{ GHz}$)

Typical values (transmon):

$L \approx 8 \text{ nH}$, $C \approx 80 \text{ fF}$

$$\frac{\omega_{10}}{2\pi} = f_{10} \approx 6 \text{ GHz}$$



Qubit control example: Rabi Oscillation

Driving a qubit on-resonance with a wave:

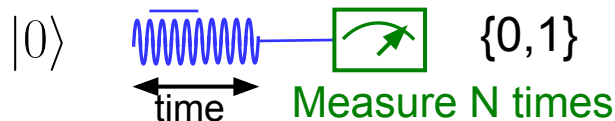
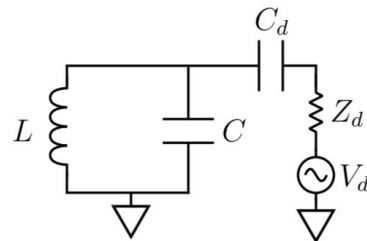
$$V(t) = V_0 \sin(\omega t + \phi)$$

Qubit oscillates

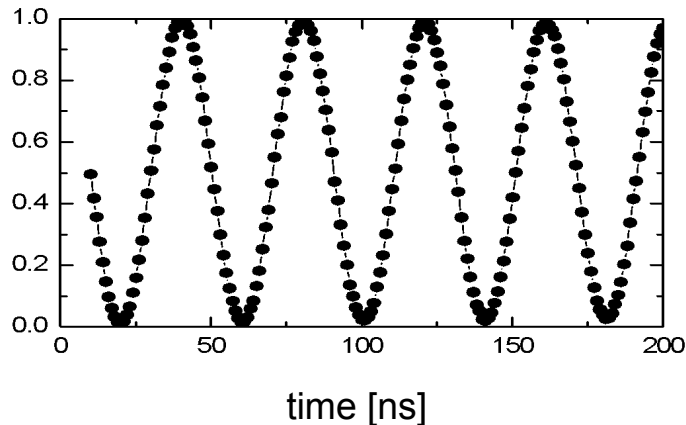
$$|\psi(t)\rangle = \cos\left(\frac{\Omega}{2}t\right)|0\rangle + ie^{i\phi} \sin\left(\frac{\Omega}{2}t\right)|1\rangle$$

with Rabi frequency

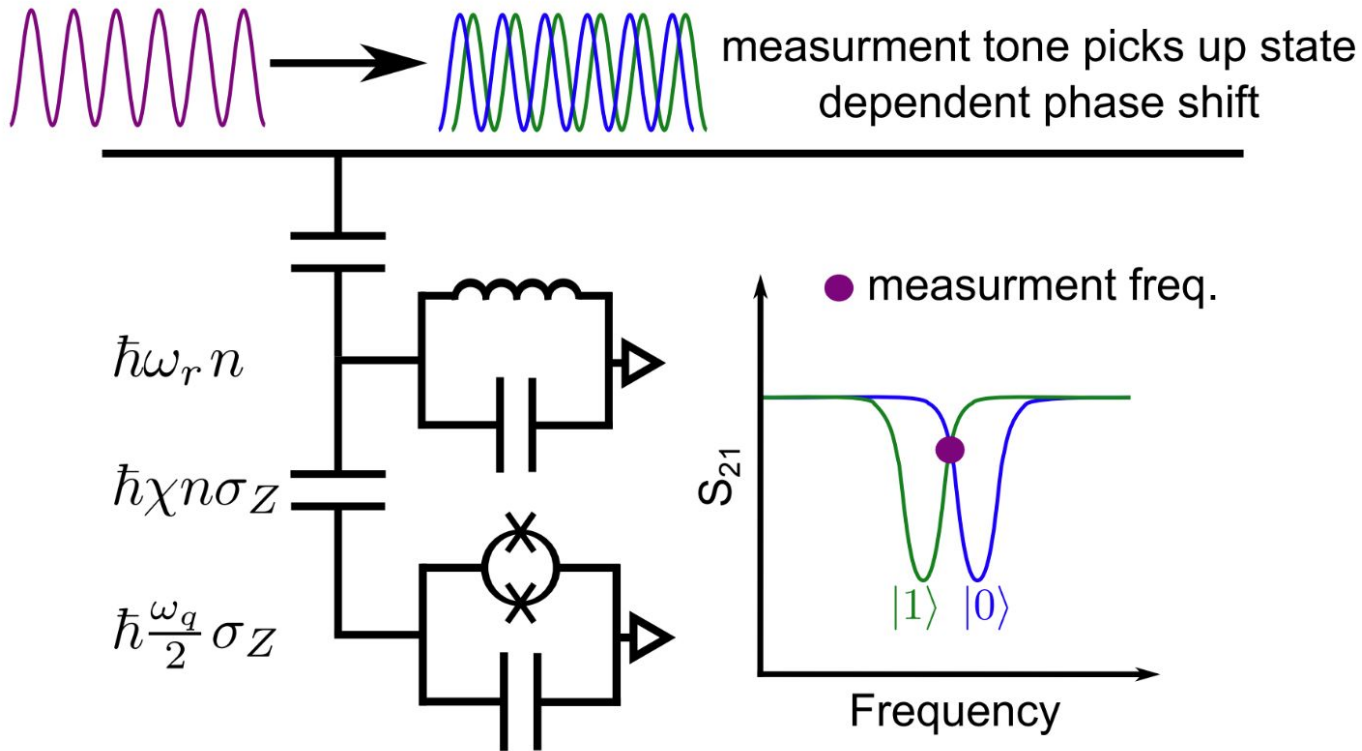
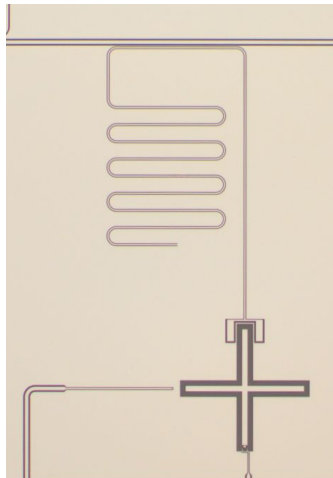
$$\Omega = \frac{C_d}{C + C_d} \frac{V_0}{\hbar} \langle 0|Q^2|0\rangle^{\frac{1}{2}}$$



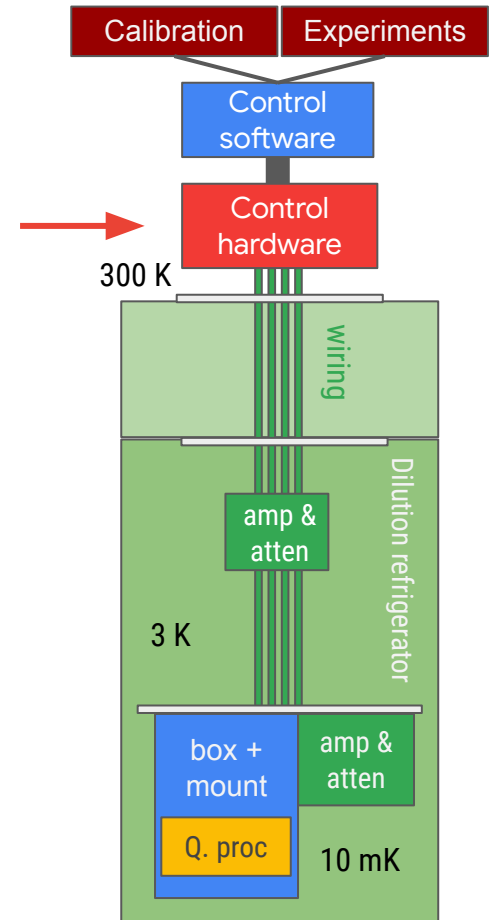
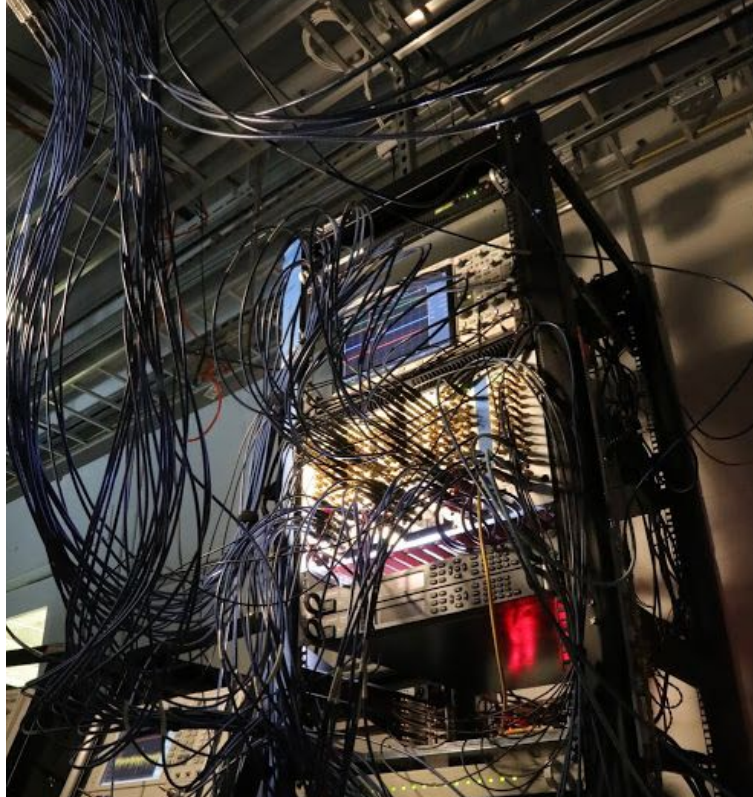
Prob($|0\rangle$)



Qubit state measurement with readout resonator



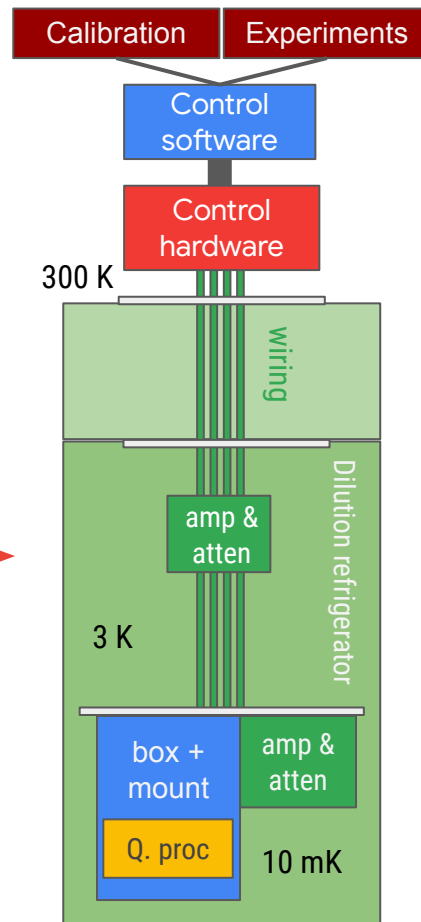
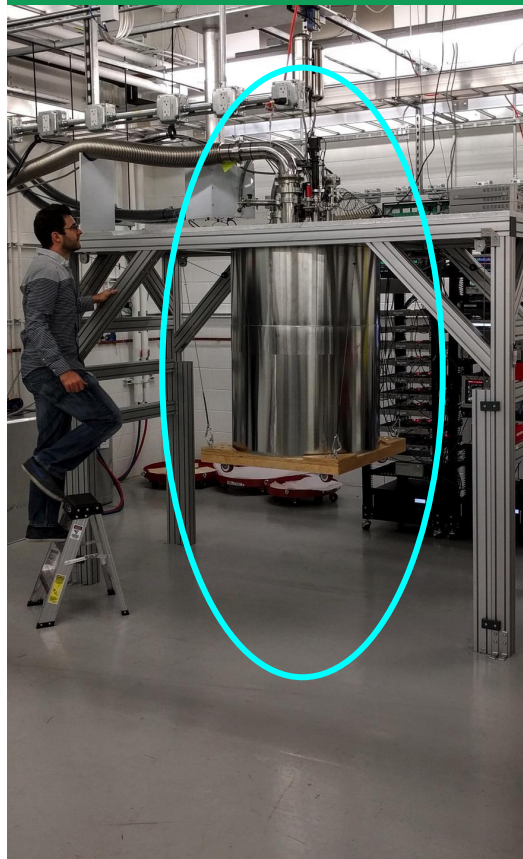
Custom Microwave Control Electronics

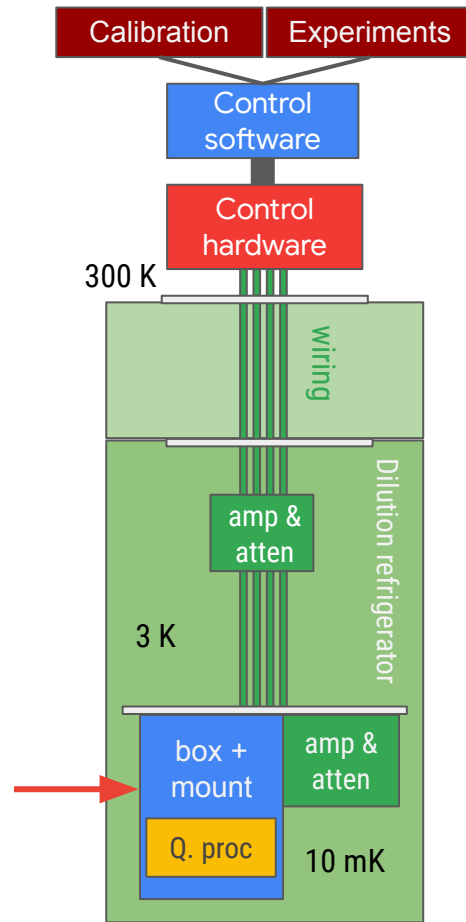
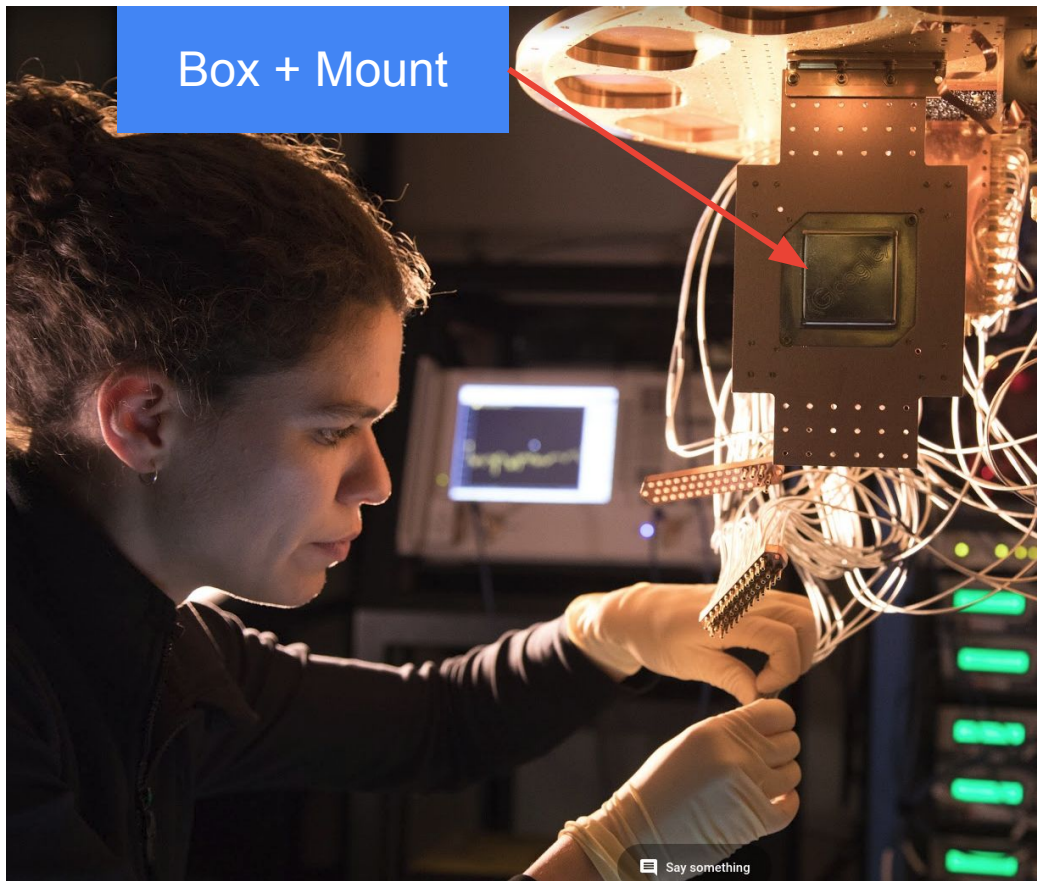


Wiring + amplifiers & filters



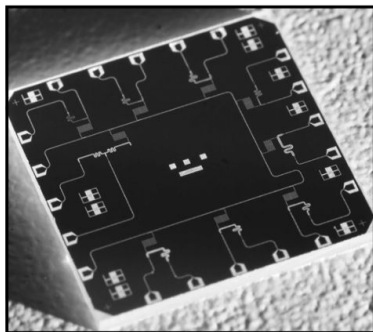
Dilution Refrigerator





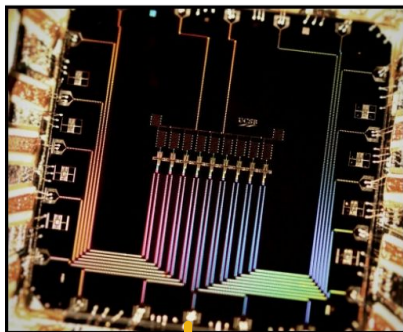
Fluxmon

- Flux qubit, tunable coupling
- optimization problems



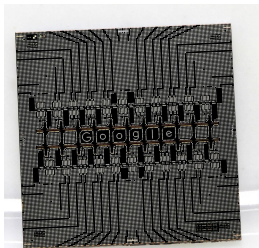
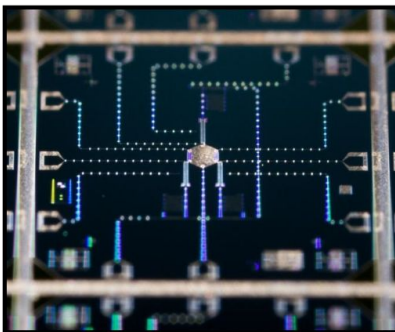
Xmon

- X-shaped transmon qubit
- gate-based QC

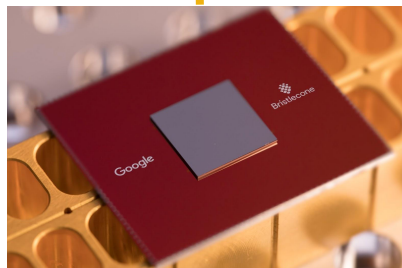


Gmon

- Transmon qubit, tunable nearest-neighbor coupling



Foxtail: 22 qubits



Bristlecone: 72 qubits

Calibration Experiments

Control software

Control hardware

300 K

wiring

amp & atten

3 K

Dilution refrigerator

box + mount

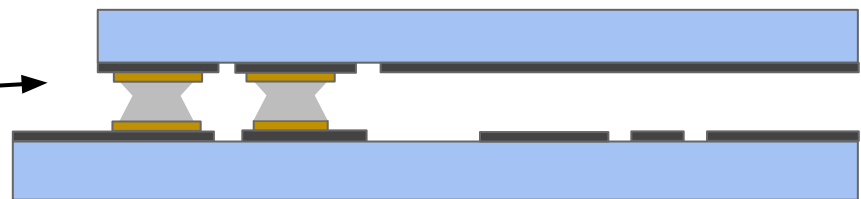
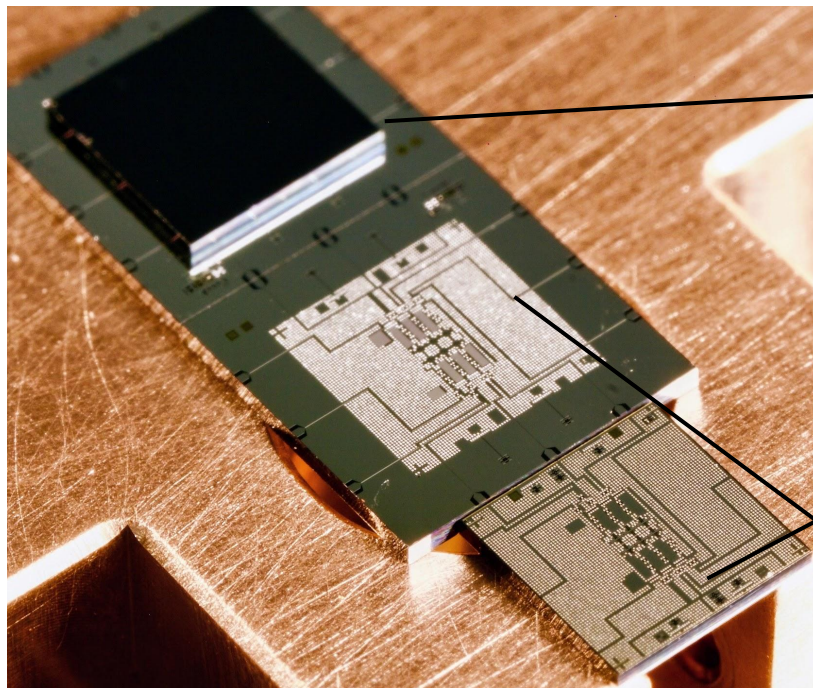
amp & atten

Q. proc

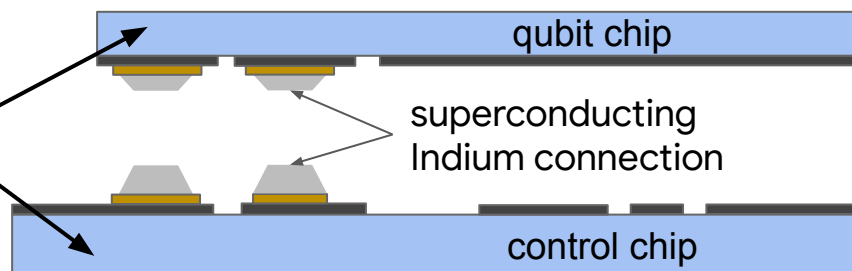
10 mK



Flip chip geometry with bump bonds



bonded chip

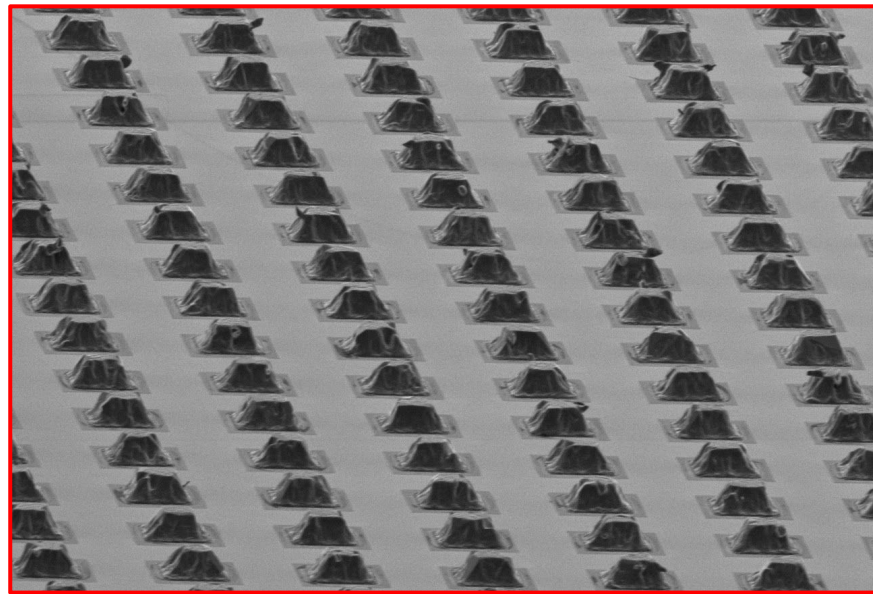
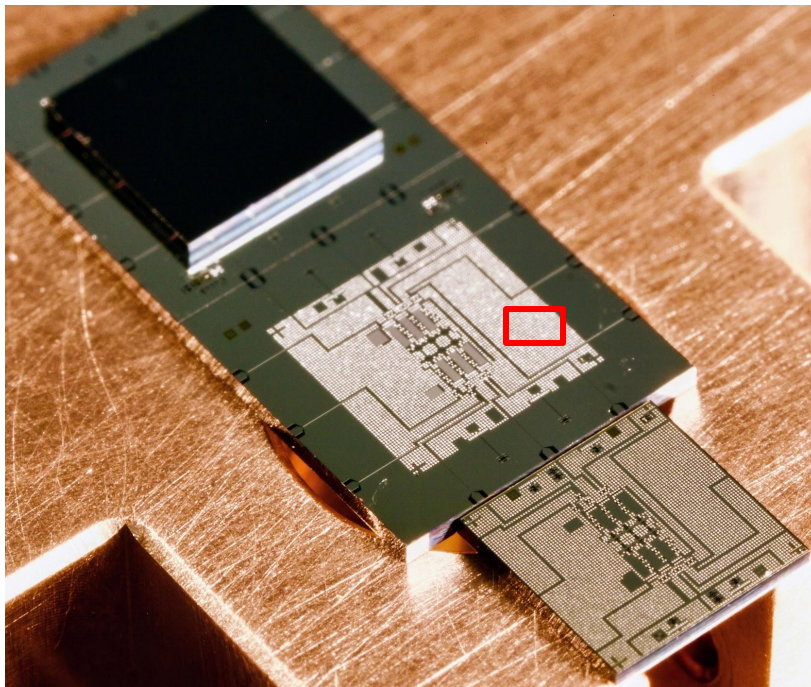


qubit chip

superconducting
Indium connection

control chip

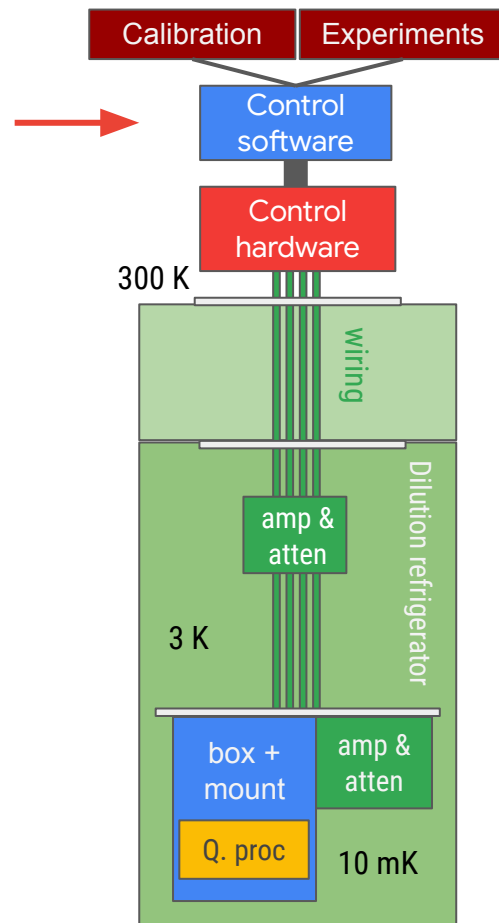
Flip chip geometry with bump bonds



B. Foxen et al. Quantum Science and Technology, Volume 3, Number 1 (2017)

Quantum OS

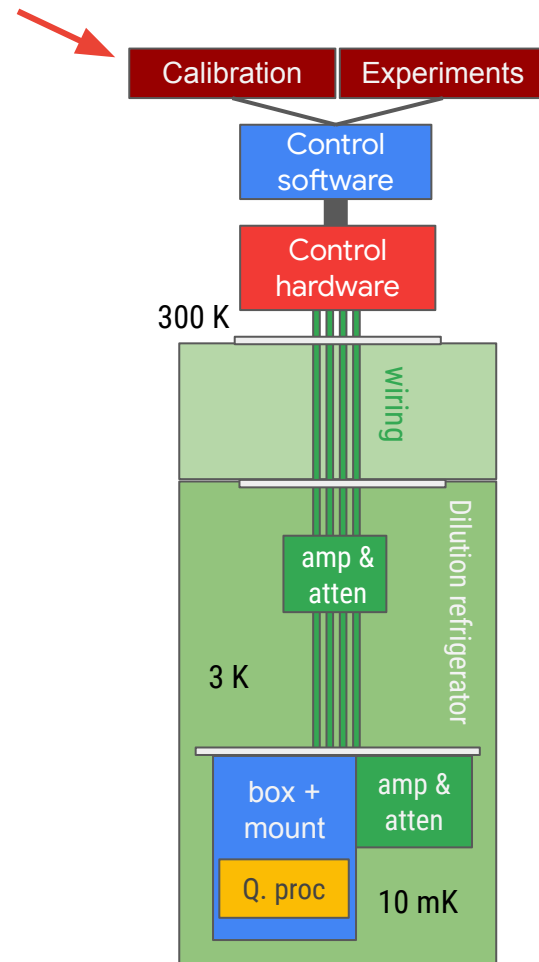
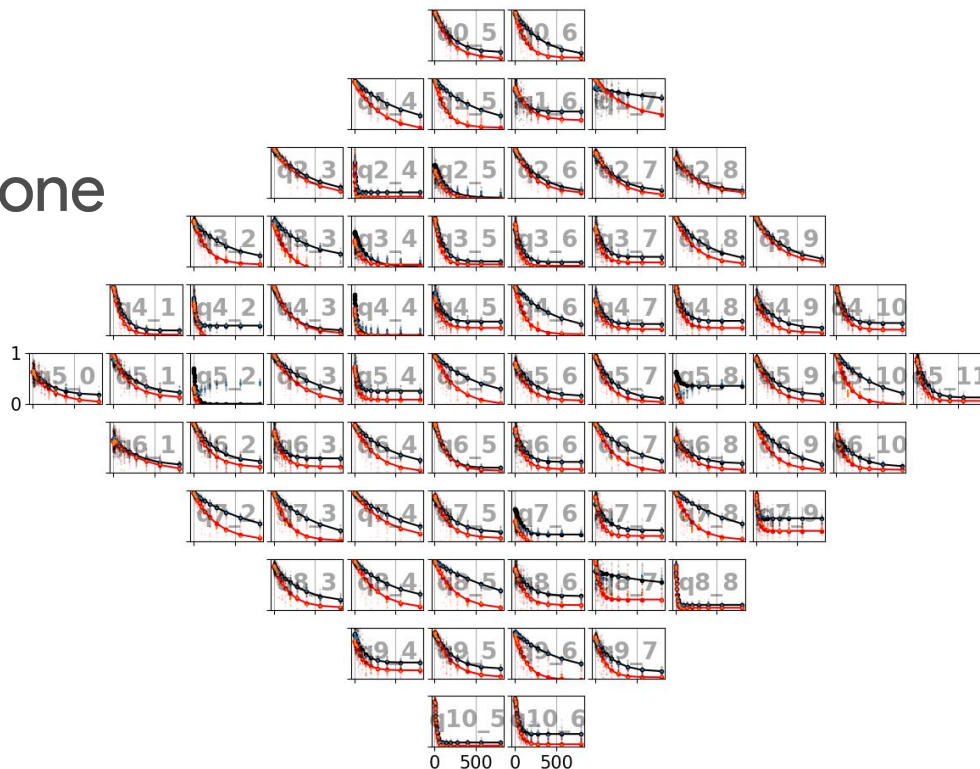
- Micro-services
 - LabRAD: service architecture / RPC
 - scheduling, gate compiler, FPGA, GPIB, etc. are servers
 - Experiments are initiated from clients
- Private github repo
 - Python + scala + rust
 - Coding styles / formatter / linter / type check
 - Code reviews / continuous integration
- Automate calibrations, experiments
 - Make hard things easy to move forward



Calibration: Key to Quality



Bristlecone



Bootstrapping

Experiment

Rabi

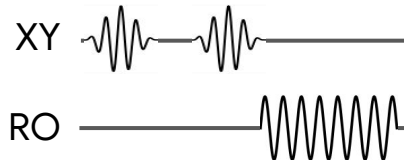
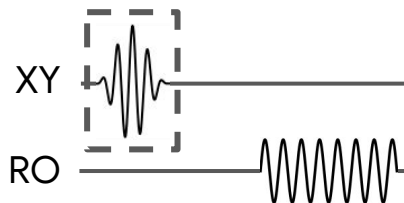


Readout

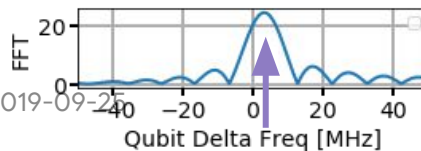
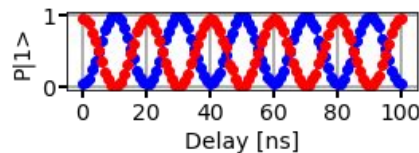
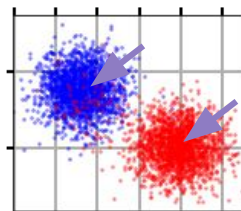
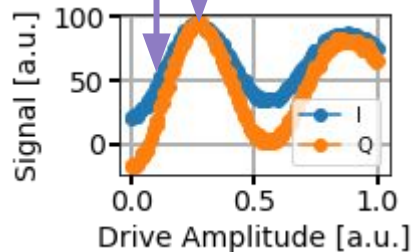


Ramsey

Control Sequence



Data



Cal Value

π amp. = 0.3
 $\pi/2$ amp. = 0.15

0-state = (25, -20)
1-state = (100, 100)

$f_{10} = 6.0 \text{ GHz} + 3 \text{ MHz}$



Bootstrapping

Experiment

Rabi

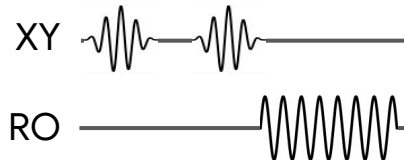
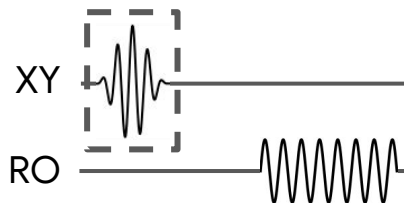


Readout

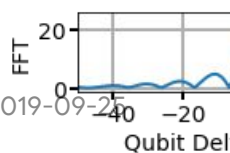
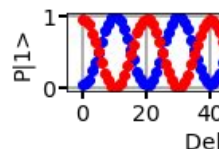
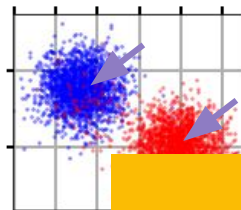
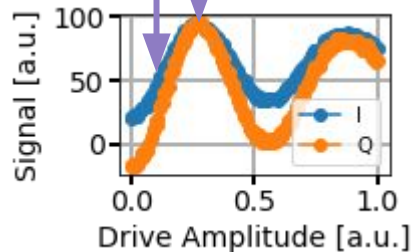


Ramsey

Control Sequence



Data



Cal Value

π amp. = 0.3
 $\pi/2$ amp. = 0.15

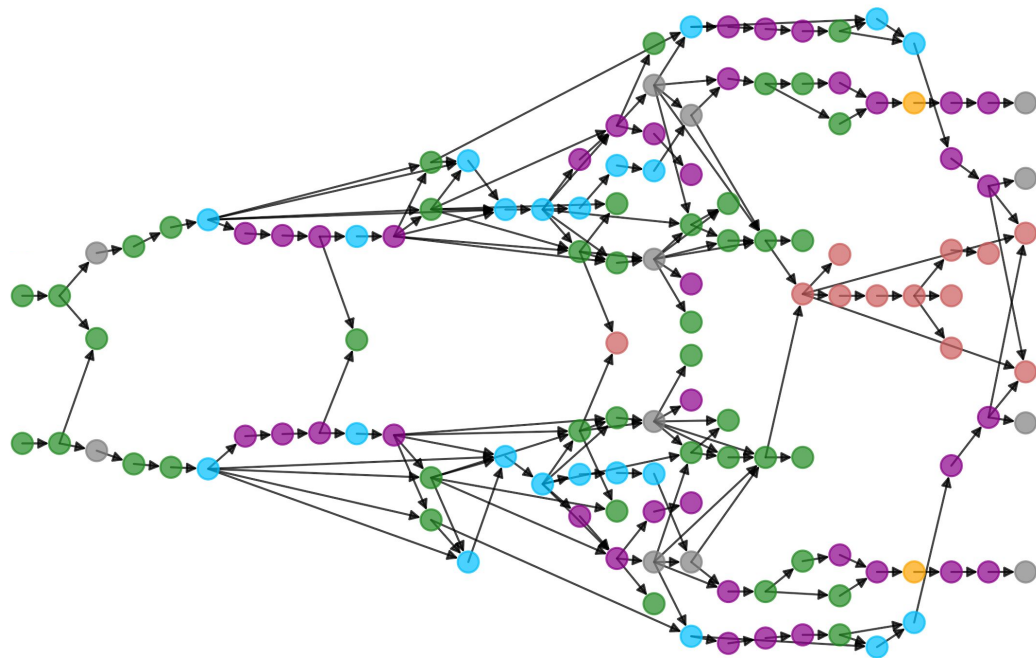
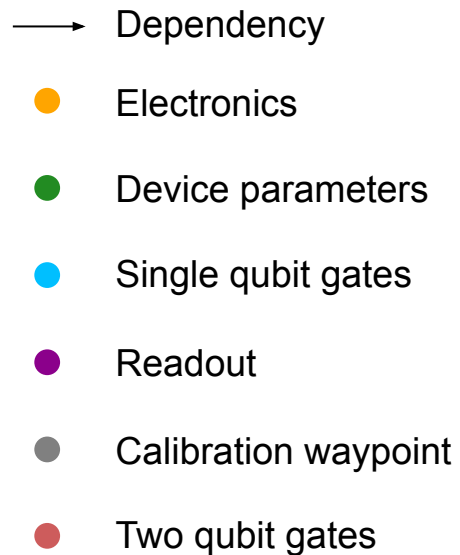
0-state = (25, -20)
1-state = (100, 100)

Why does this sequence work?

Careful order to **bootstrap**
system knowledge



Calibration Dependency Graph

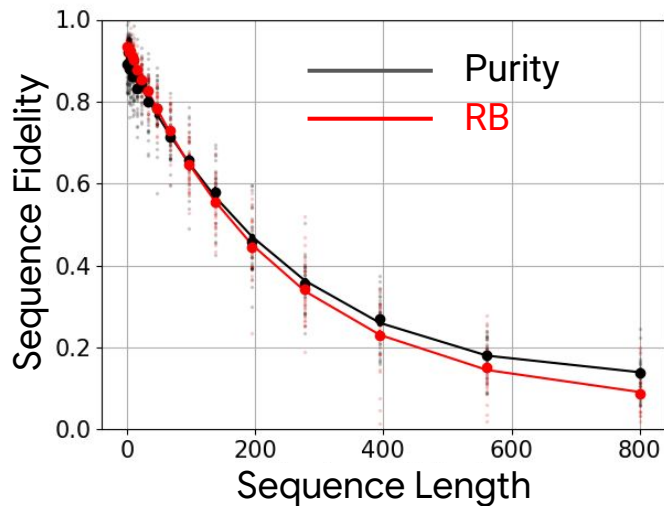


White paper on automation: [arxiv: 1803.03226](https://arxiv.org/abs/1803.03226)



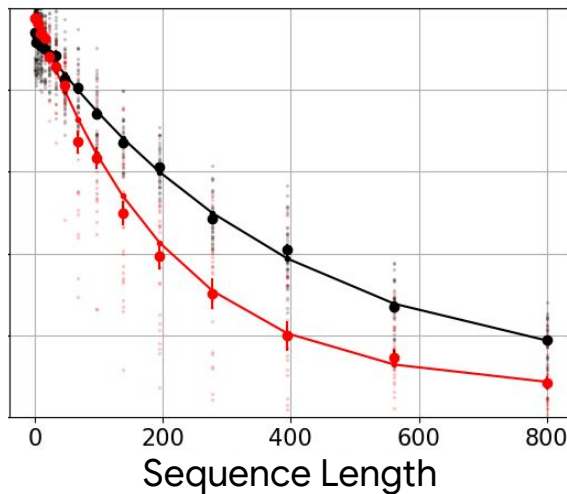
Data: Randomized Benchmarking vs. Purity

Error = 1 - fidelity. Purity \rightarrow decoherence error, RB \rightarrow total error.



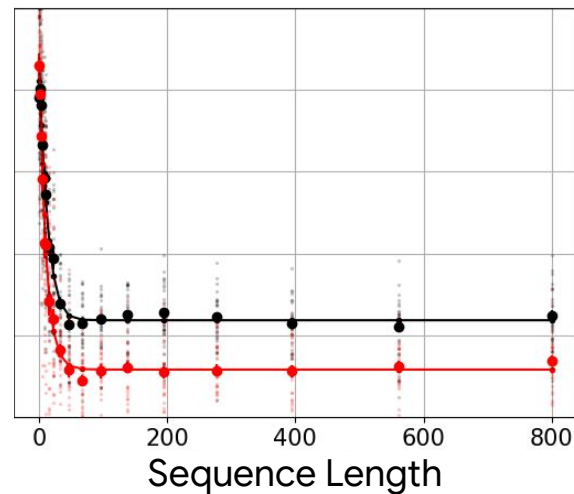
Low decoherence error
Low total error

qubit #1



Low decoherence error
Medium total error

qubit #2



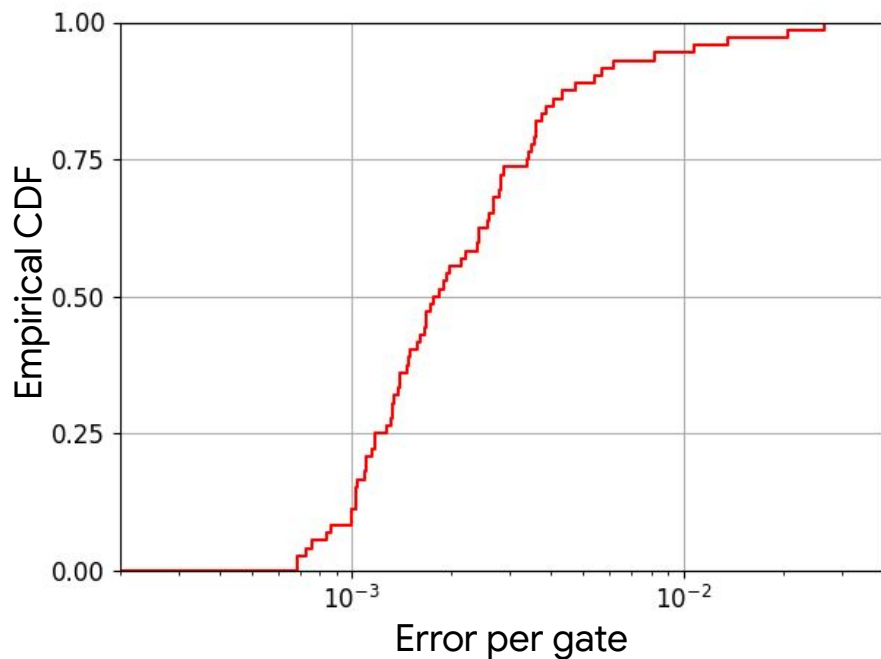
High decoherence error
High total error

qubit #3

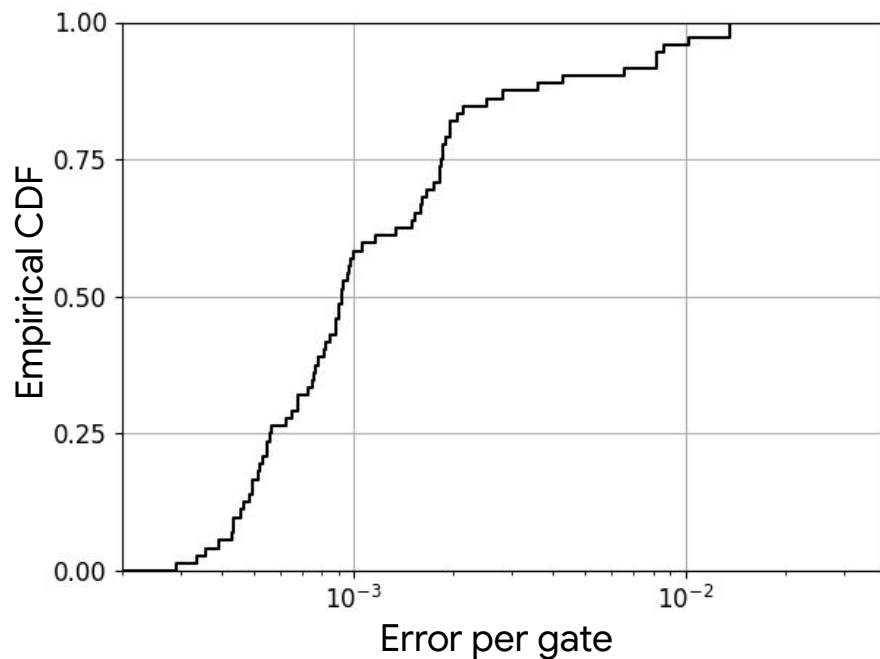


Empirical CDF: for measuring improvements

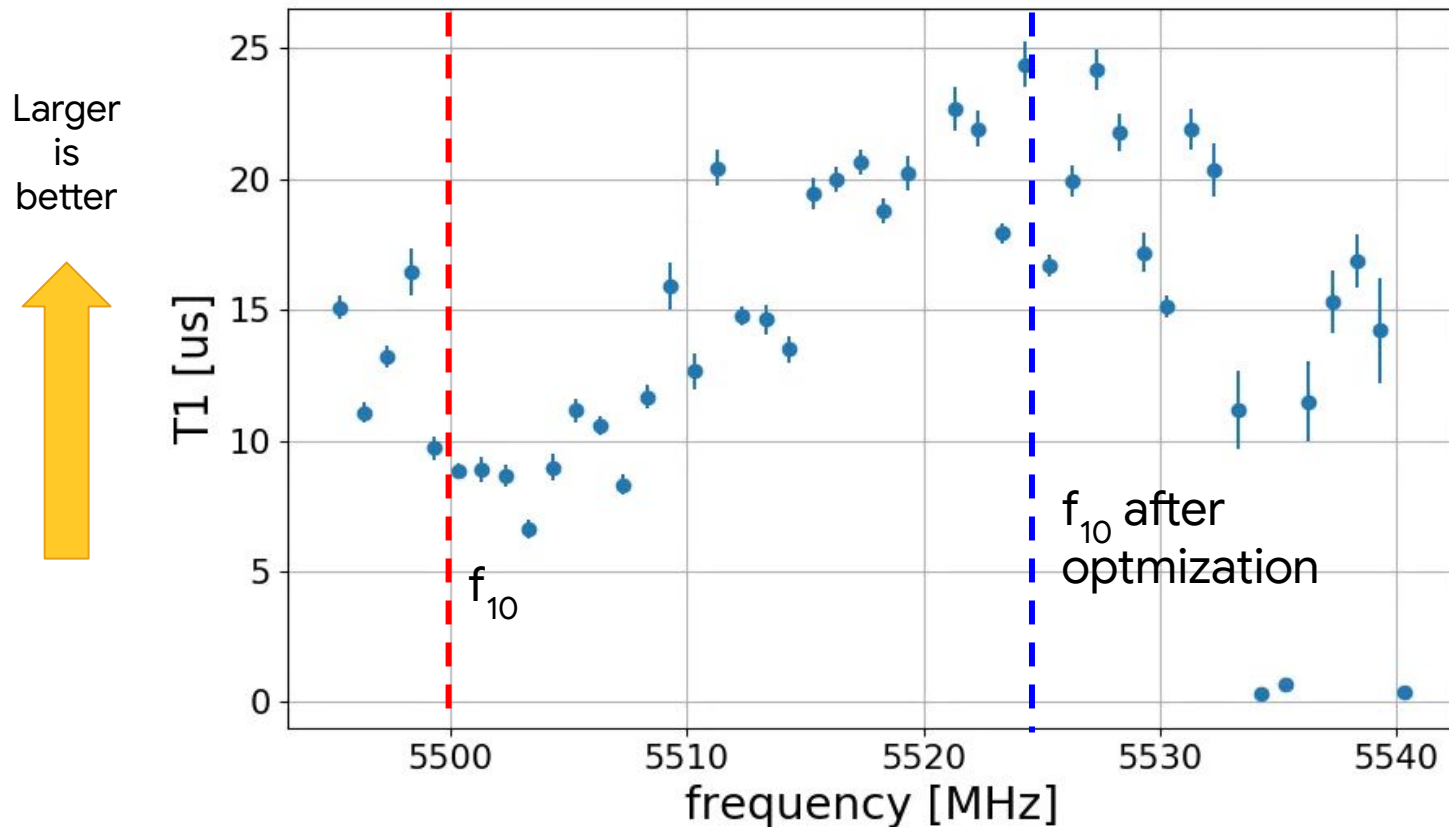
Total Error



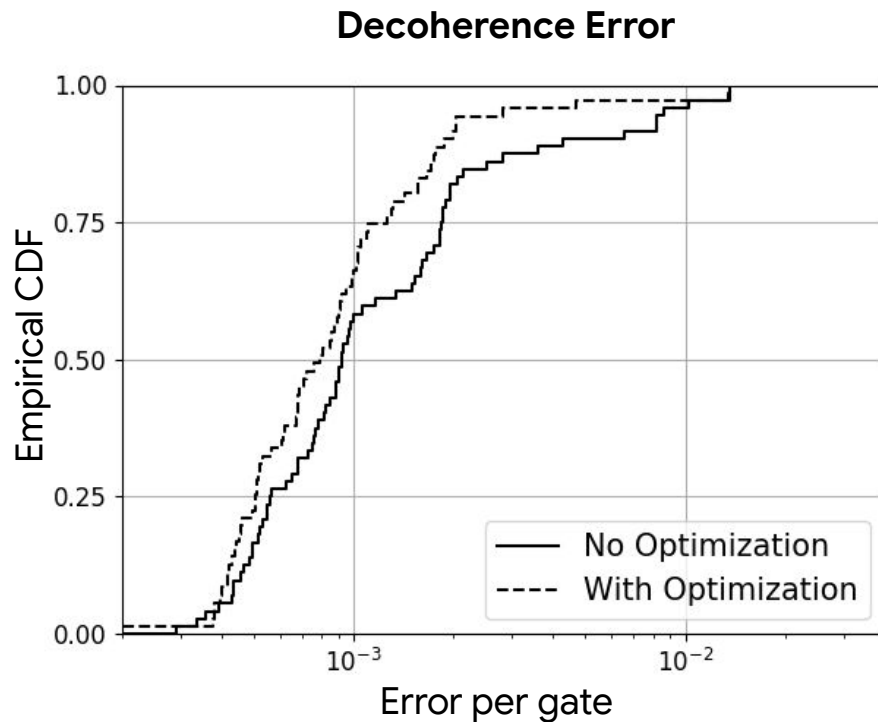
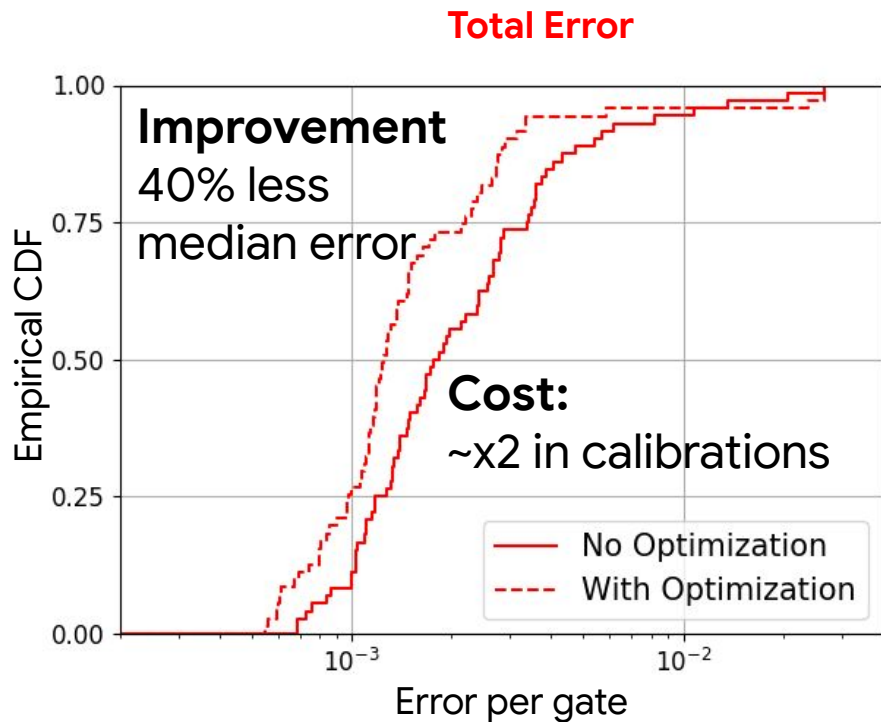
Decoherence Error



Calibration Study: Frequency Optimization



Fidelity improvements from frequency optimization



Experiments

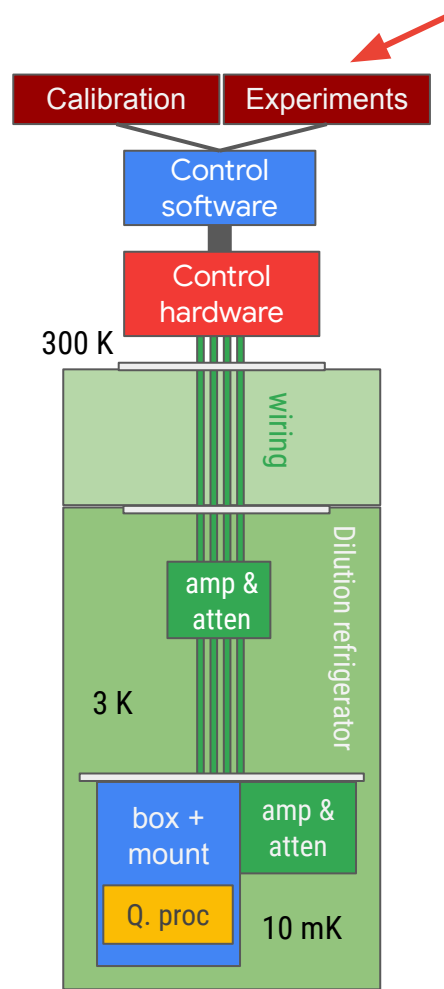
Noise study

Error/control study

Algorithm study

Sampling from random quantum circuit

etc.



Pursuit of quantum supremacy



Quantum supremacy

QUANTUM COMPUTING AND THE ENTANGLEMENT FRONTIER

arXiv:1203.5813

JOHN PRESKILL

*Institute for Quantum Information and Matter
California Institute of Technology
Pasadena, CA 91125, USA*

We therefore hope to hasten the onset of the era of *quantum supremacy*, when we will be able to perform tasks with controlled quantum systems going beyond what can be achieved with ordinary digital computers. To realize that dream, we must overcome the formidable enemy of *decoherence*, which makes typical large quantum systems behave classically. So another question looms over the subject:

*Is controlling large-scale quantum systems merely **really, really hard**, or is it **ridiculously hard**?*

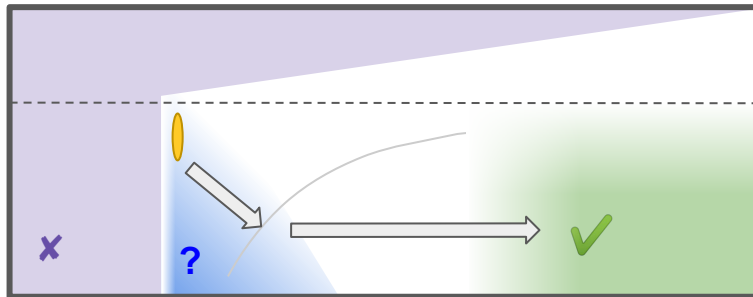


Quantum supremacy

Find **one** problem and demonstrate supremacy with real quantum hardware.

- A test of both quantity (number of qubits) and quality (fidelity).
- The problem itself does not need to have real world applications.

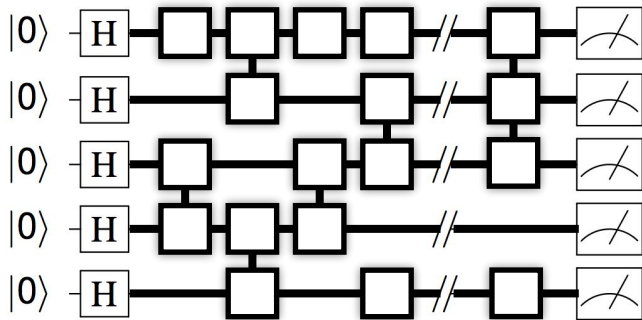
It's like a **beam test** on detectors.



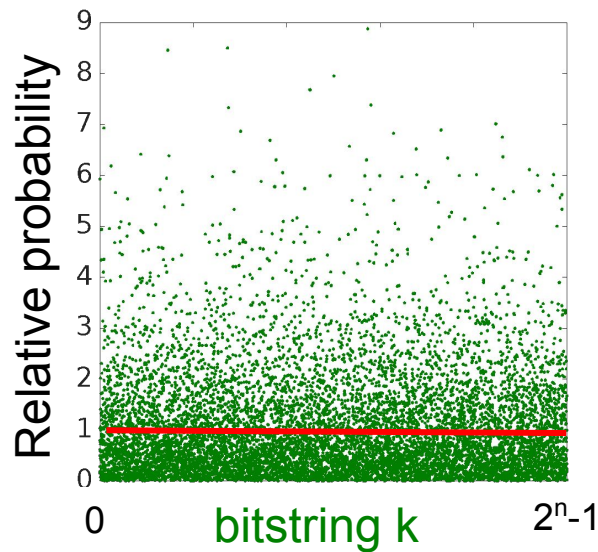
My personal take: "Before claiming that you can fly, can you show that you can run instead of just walking?"

The problem Google picked: quantum sampling

Problem: Given a random quantum circuit of n qubits and depth m , sample M bitstrings according to the probability distribution of the final state.



$$|0\rangle^{\otimes n} \mapsto H^{\otimes n} |0\rangle^{\otimes n} = \left(\frac{|0\rangle + |1\rangle}{\sqrt{2}} \right)^{\otimes n} \mapsto U \left(\frac{|0\rangle + |1\rangle}{\sqrt{2}} \right)^{\otimes n} = \sum_{i=1}^{2^n} c_i |x_i\rangle$$
$$p_U(x_i) = |c_i|^2$$



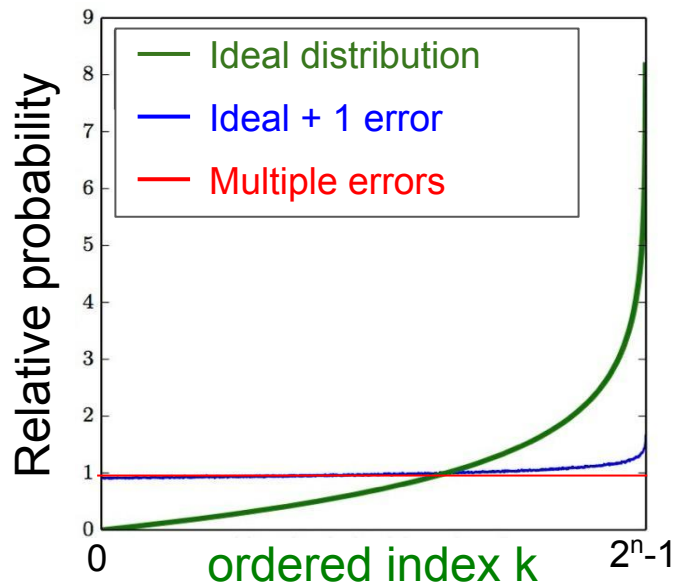
Quantum sampling: theory

$\text{Prob}(k) \sim \text{Porter-Thomas distribution}$ when error = 0 (ideal).

$$P(p) \propto e^{-Dp}$$

D = dimension of Hilbert space = 2^n

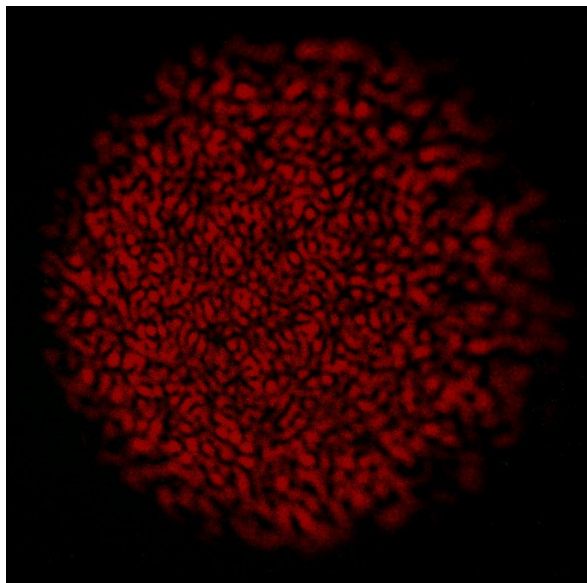
Decoherence error destroys it
~ uniform distribution



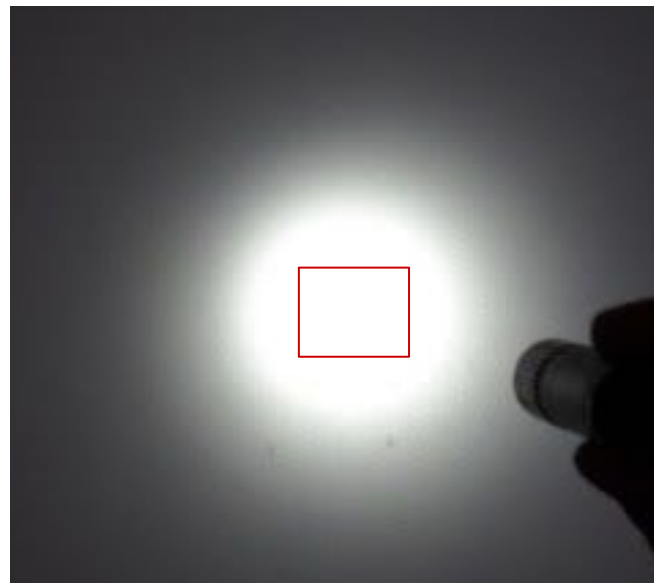
S. Boixo et al. Nature Physics **14**, 595–600 (2018), arXiv:1608.00263



Intuition: coherence test

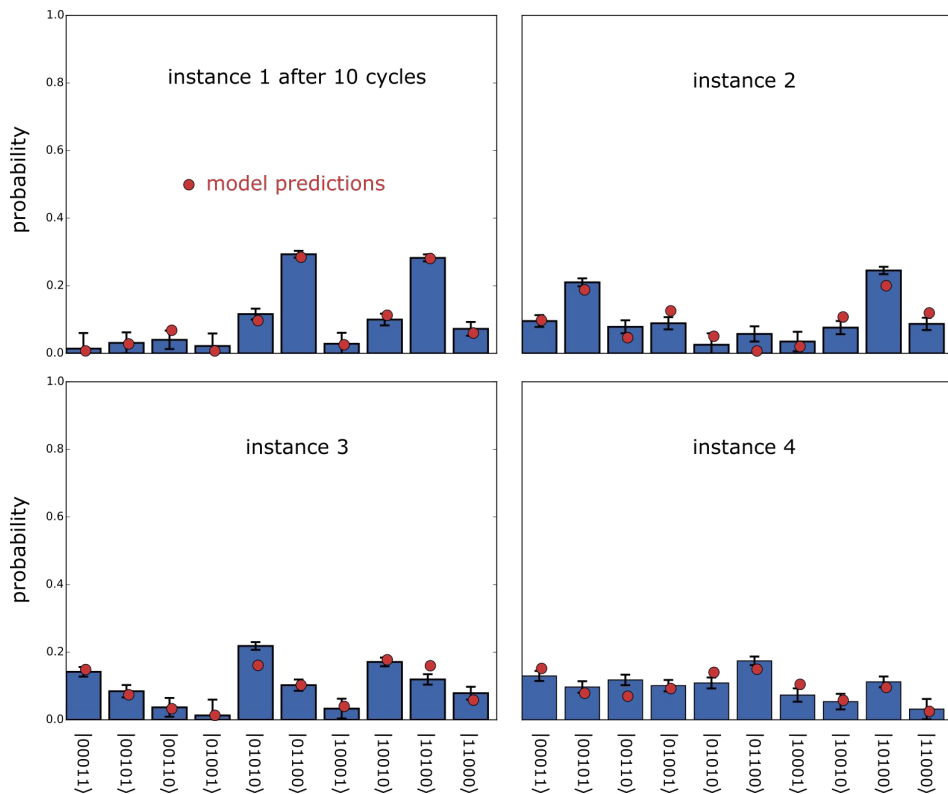


Coherent quantum interference: speckles



Incoherent classical light

Experimental Results with 5 qubits



Looks good qualitatively!

Quantitatively?



Cross-entropy benchmark (XEB)

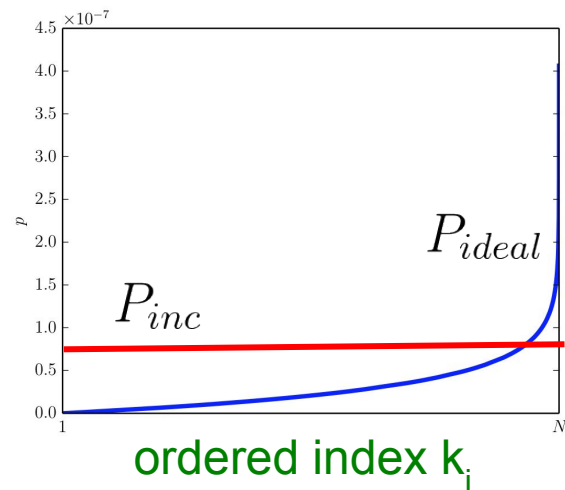
Cross entropy between 2 distributions p and q :

$$S(p(k), q(k)) \equiv - \sum_i p(k_i) \log q(k_i)$$

Fidelity
$$F = \frac{S(P_{inc}, P_{ideal}) - S(P_{expt}, P_{ideal})}{S(P_{inc}, P_{ideal}) - S(P_{ideal}, P_{ideal})}$$

$$F = \begin{cases} 0, & \text{if } P_{expt} = P_{inc} \\ 1, & \text{if } P_{expt} = P_{ideal} \end{cases}$$

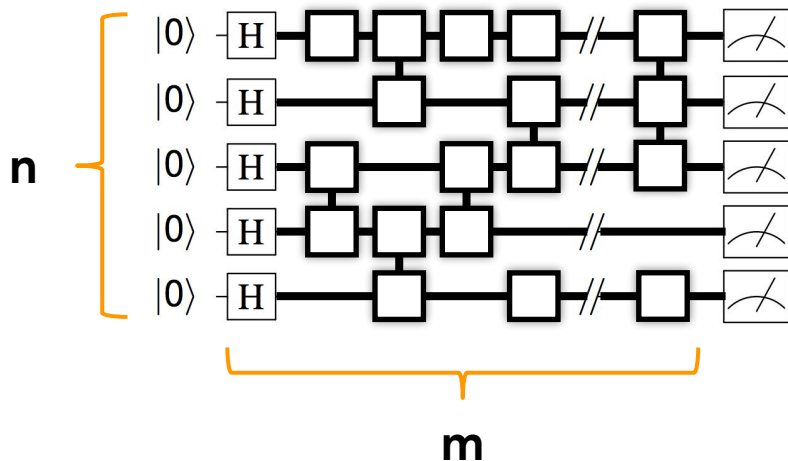
from classical simulation
of ideal circuit



Likelihood ratio yields similar results

The quantum supremacy question

Given a random quantum circuit with n qubits and depth m ,
what's the amount of computation (core * hours) needed for a classical computer
to sample M bitstrings from a quantum computer with fidelity F ?



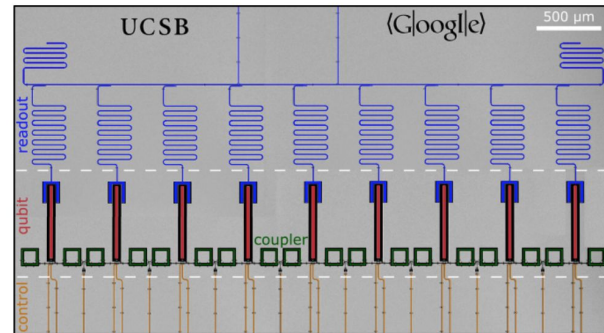
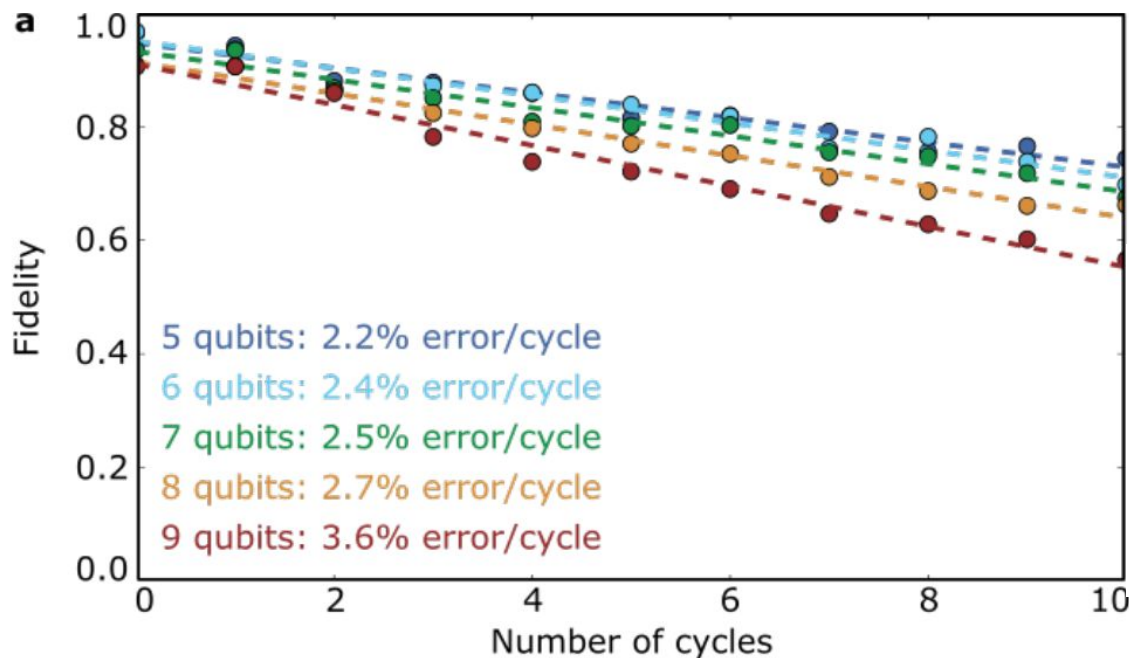
Expect:

For large enough n and m with a decent F , this is out of reach for classical computers.

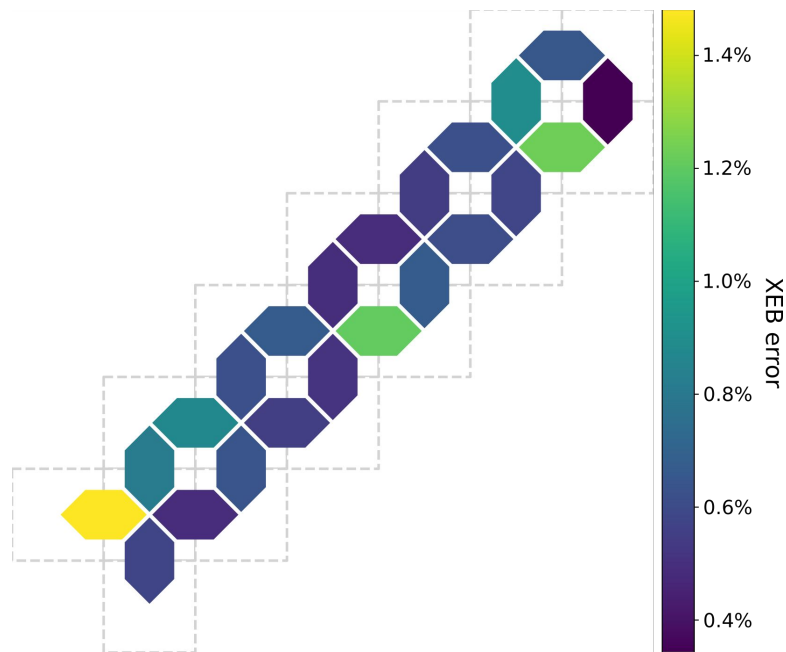
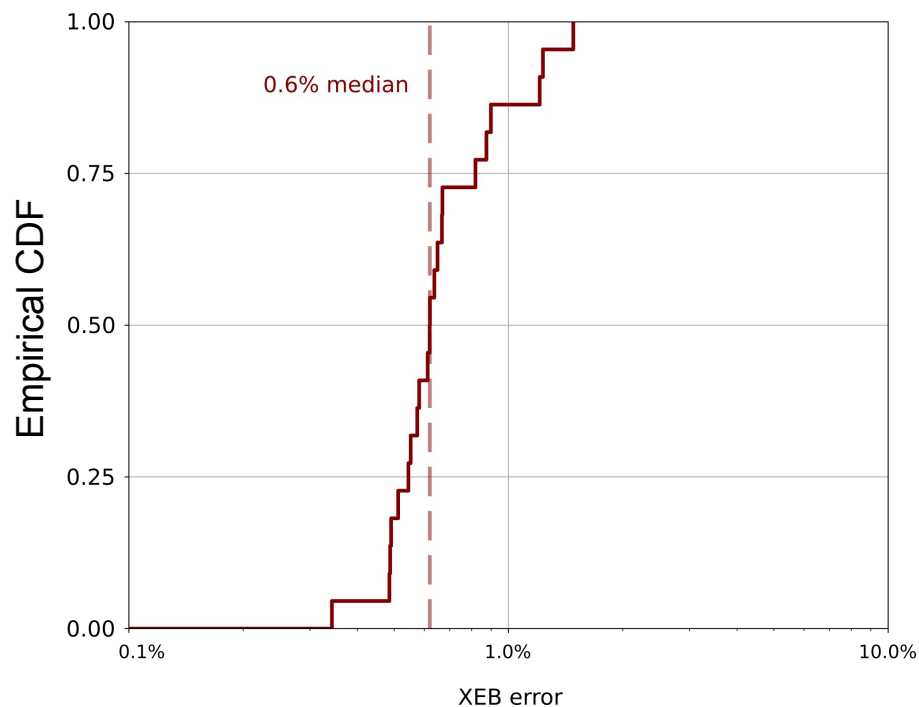
How good is your quantum computer hardware?

Data from 9-qubit experiments

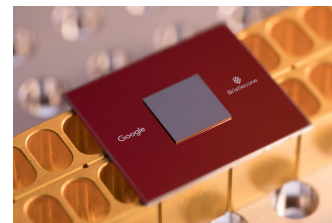
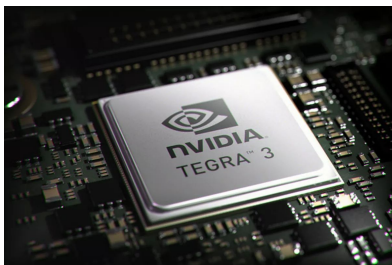
"A blueprint for demonstrating quantum supremacy with superconducting qubits", Science **13** Apr 2018 | arXiv:1709.06678



Two-qubit gate errors from an 18-qubit chip



Classical computing power vs. quantum



Simulation on Summit

Establishing the Quantum Supremacy Frontier with a 281 Pflop/s Simulation

Benjamin Villalonga^{1,2,3,*}, Dmitry Lyakh^{4,5†}, Sergio Boixo^{6,‡}, Hartmut Neven^{6,+}, Travis S. Humble^{4,§},
Rupak Biswas^{1,×}, Eleanor G. Rieffel^{1,¶}, Alan Ho^{6,||}, and Salvatore Mandrà^{1,7,⊥}

¹ Quantum Artificial Intelligence Lab. (QuAIL), NASA Ames Research Center, Moffett Field, CA 94035, USA

² USRA Research Institute for Advanced Computer Science (RIACS), 615 National, Mountain View, California 94043, USA

³ Institute for Condensed Matter Theory and Department of Physics, University of Illinois at Urbana-Champaign, Urbana, IL 61801, USA

⁴ Quantum Computing Institute, Oak Ridge National Laboratory, Oak Ridge, TN, USA

⁵ Scientific Computing, Oak Ridge Leadership Computing, Oak Ridge National Laboratory, Oak Ridge, TN, USA

⁶ Google Inc., Venice, CA 90291, USA

⁷ Stinger Ghaffarian Technologies Inc., 7701 Greenbelt Rd., Suite 400, Greenbelt, MD 20770

<https://arxiv.org/abs/1905.00444>



Estimation for a hypothetical 49 qubit QC

		Runtime (hours)			Energy cost (MWh)		
Circuit size	Target fidelity (%)	Electra	Summit	QPU	Electra	Summit	QPU
$7 \times 7 \times (1 + 40 + 1)$	0.5	59.0	2.44	0.028	96.8	21.1	4.2×10^{-4}

↑
49 qubits @
depth 40

↑
 $O(10^2)$ advantage

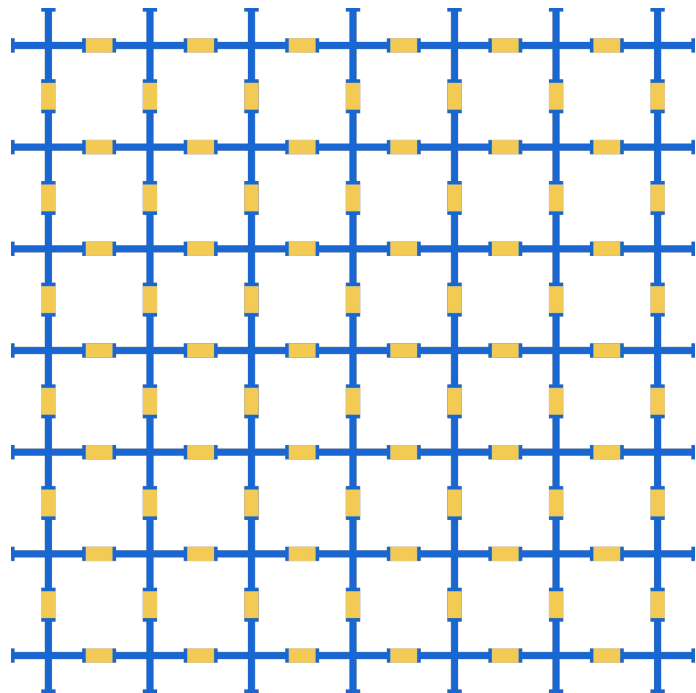
↑
 $O(10^5)$ advantage

<https://arxiv.org/abs/1905.00444>



Projection for quantum supremacy

Supremacy ~49 qubits & depth ~12



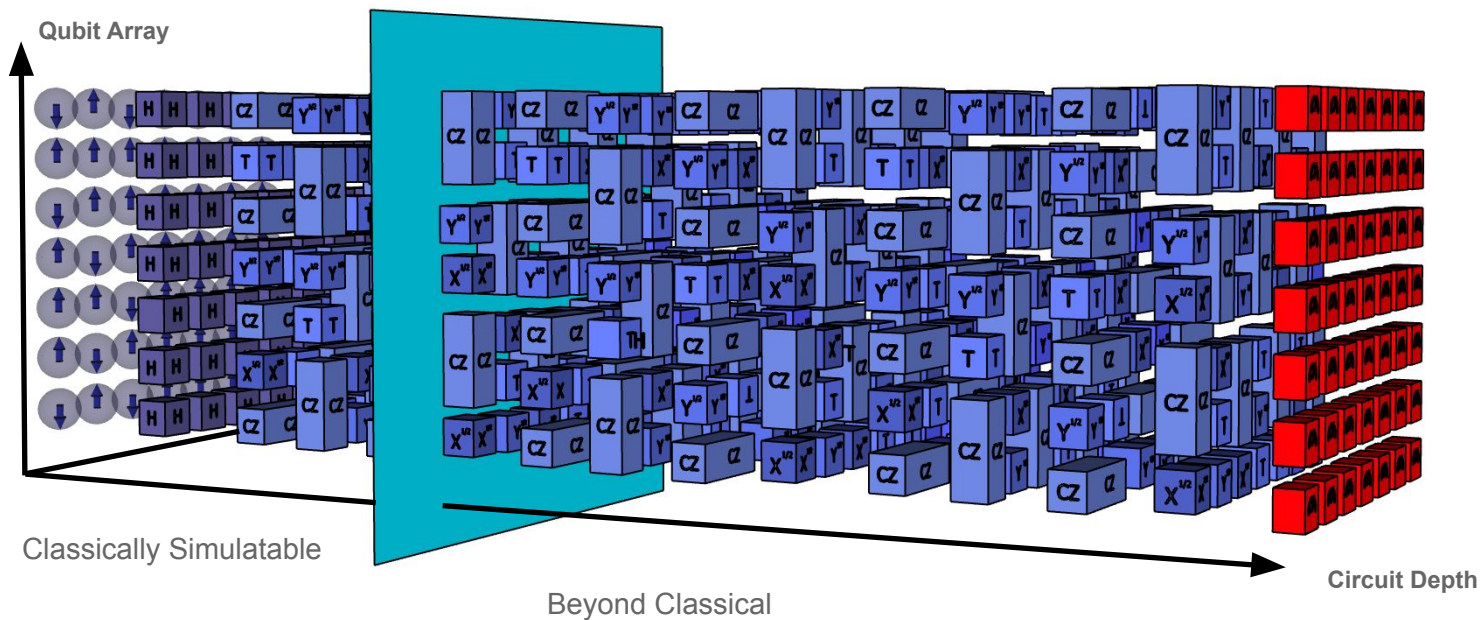
Error

1-Qubit gate fidelity	99.9%	0.1%
2-Qubit gate fidelity	99.2%	0.8%
Readout fidelity	97.0%	3%
Projected supremacy fidelity	1.6%	

Measurements needed for 5-sigma
supremacy: $M \sim 10^5$



Established Frontier of Quantum Computation



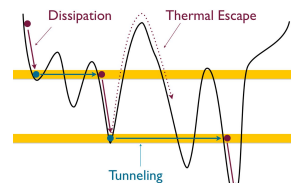
Collaboration opportunities

Google Academic Funding

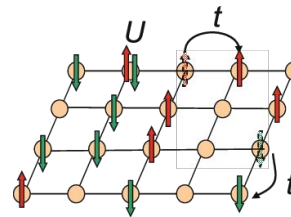
Faculty Research Awards	Focus Awards
1 year funding	2 - 3 years
1 graduate student	1+ graduate student
Collaborate with Google researchers	
Potential access to hardware	
8 awarded in 2018	
Application deadline: 10/1 5am JST	



Better hardware



Better algorithm



First applications



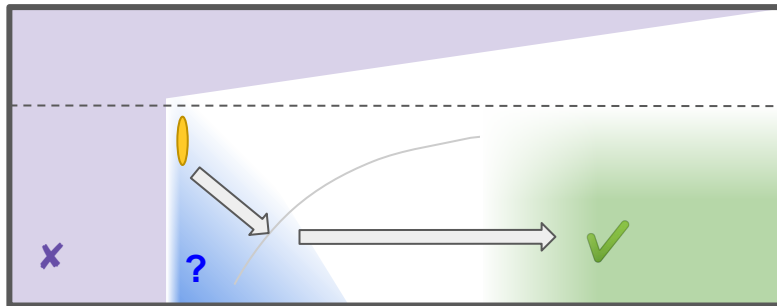
Conclusions

Quantum computing will grow as hardware becomes more capable

Google is attempting to reach quantum supremacy

Primary challenge: good coherence at larger scale / implement error correction

Collaboration opportunities





Google AI Quantum

